

# Introduction to Data Assimilation, Subgrid-Scale Parameterization and Predictability

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# Class Outline

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Concept of the class

- 1) Introductory lecture (~30mins)
- 2) Exercise: Coding of new method covered in lecture (~60mins)

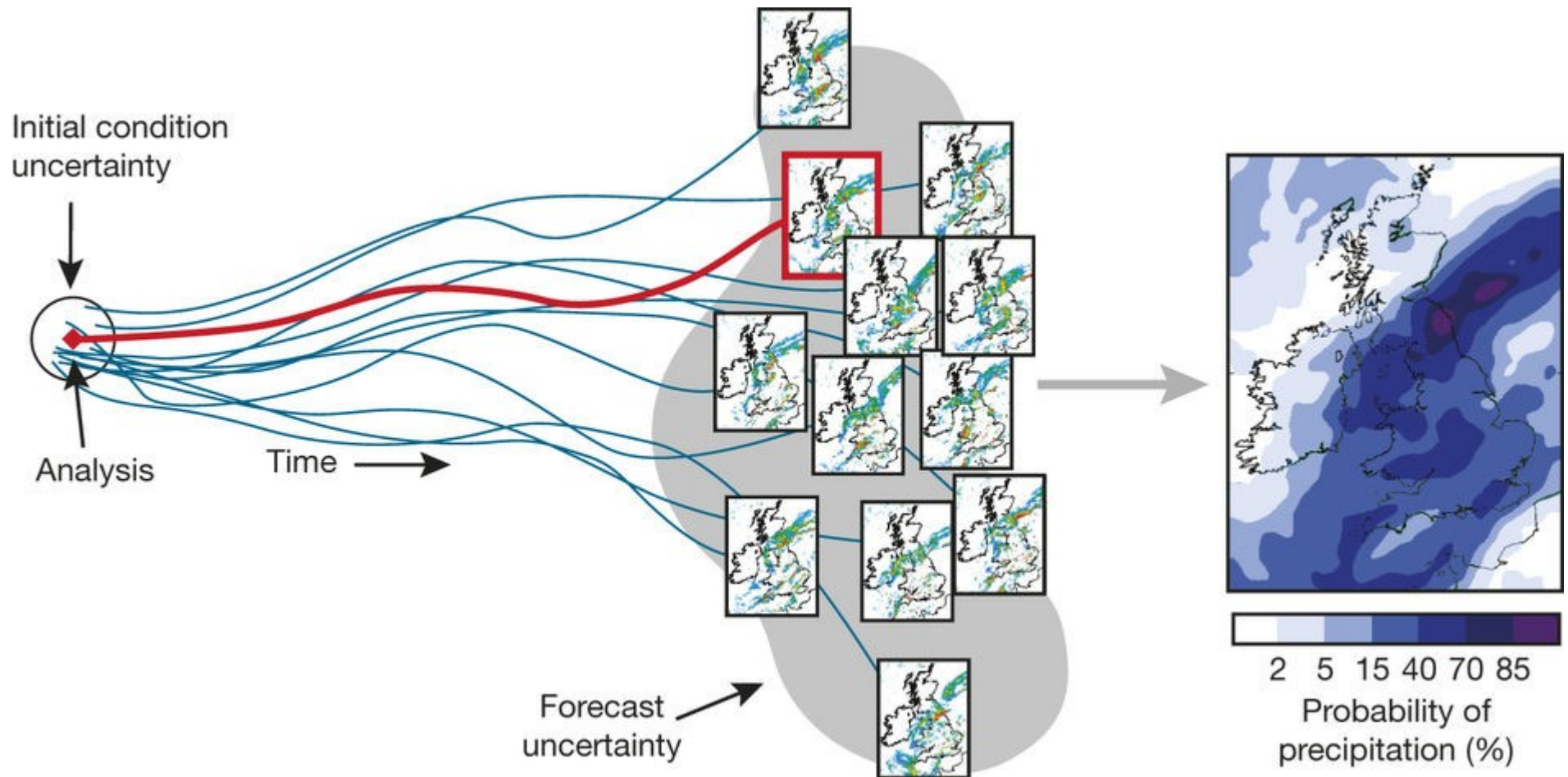
Exam: Writing of report covering all exercises

# Predictability

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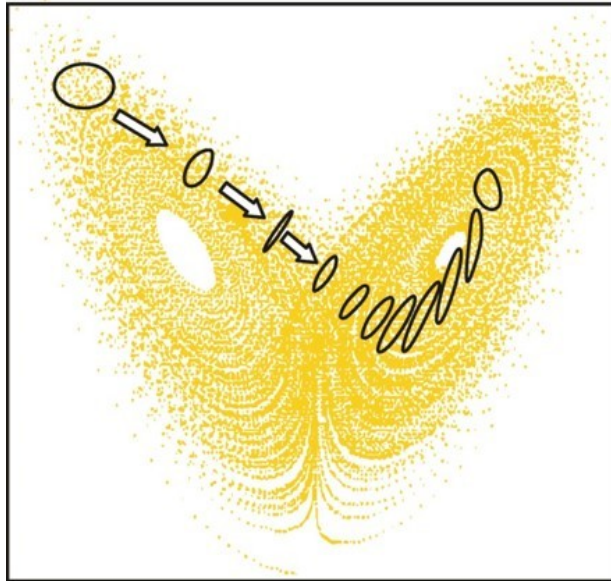
# Predictability





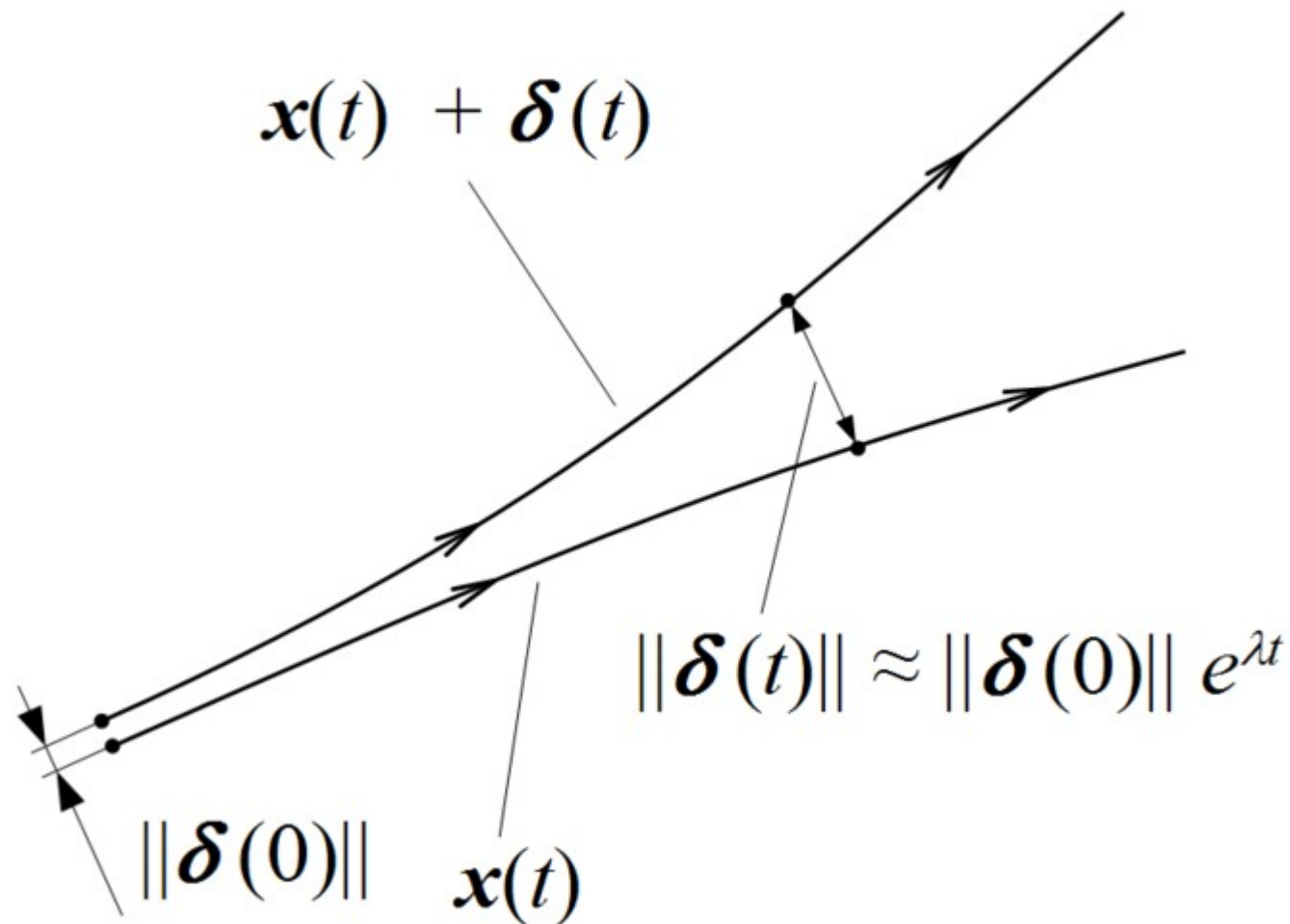
# Predictability

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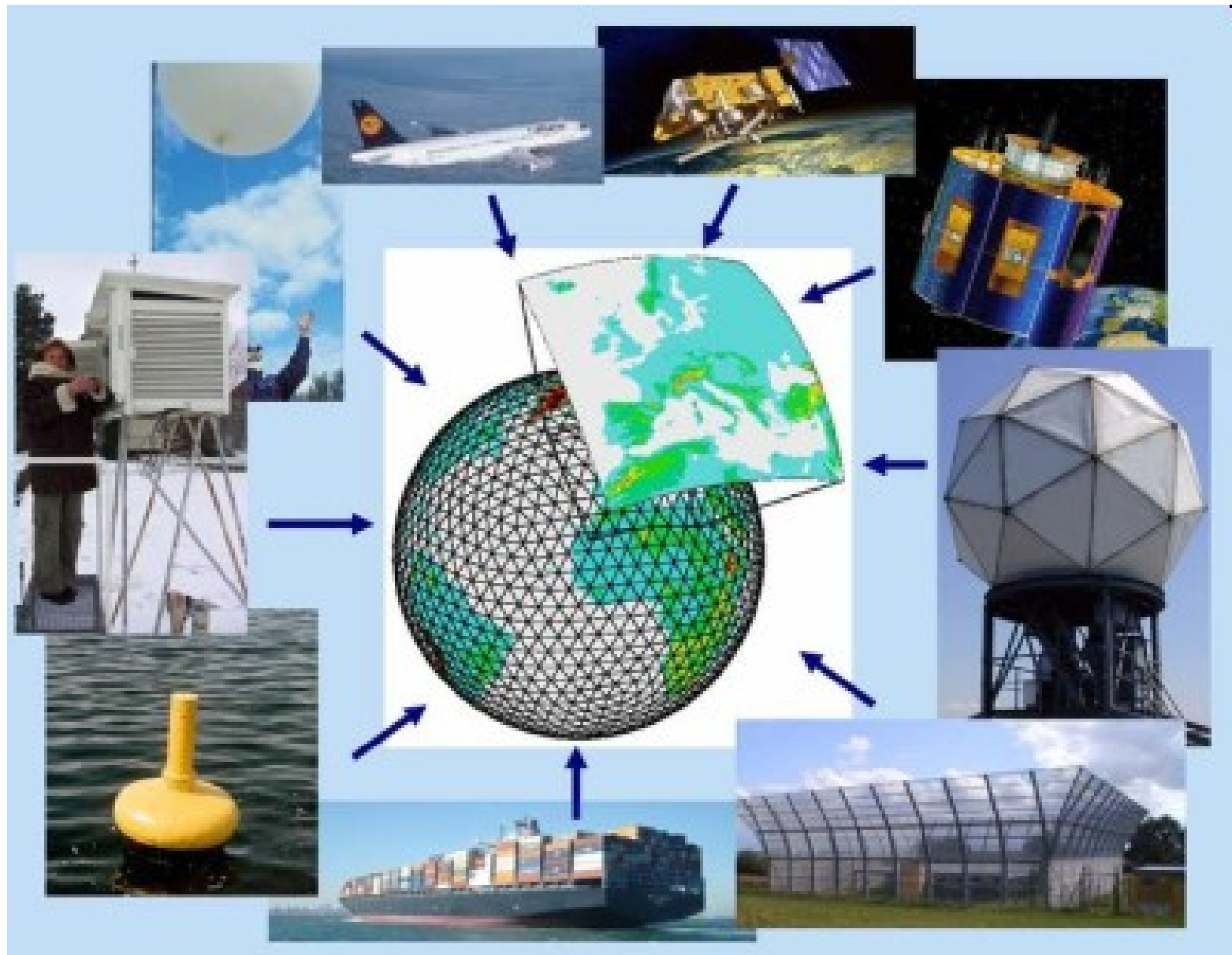
# Predictability

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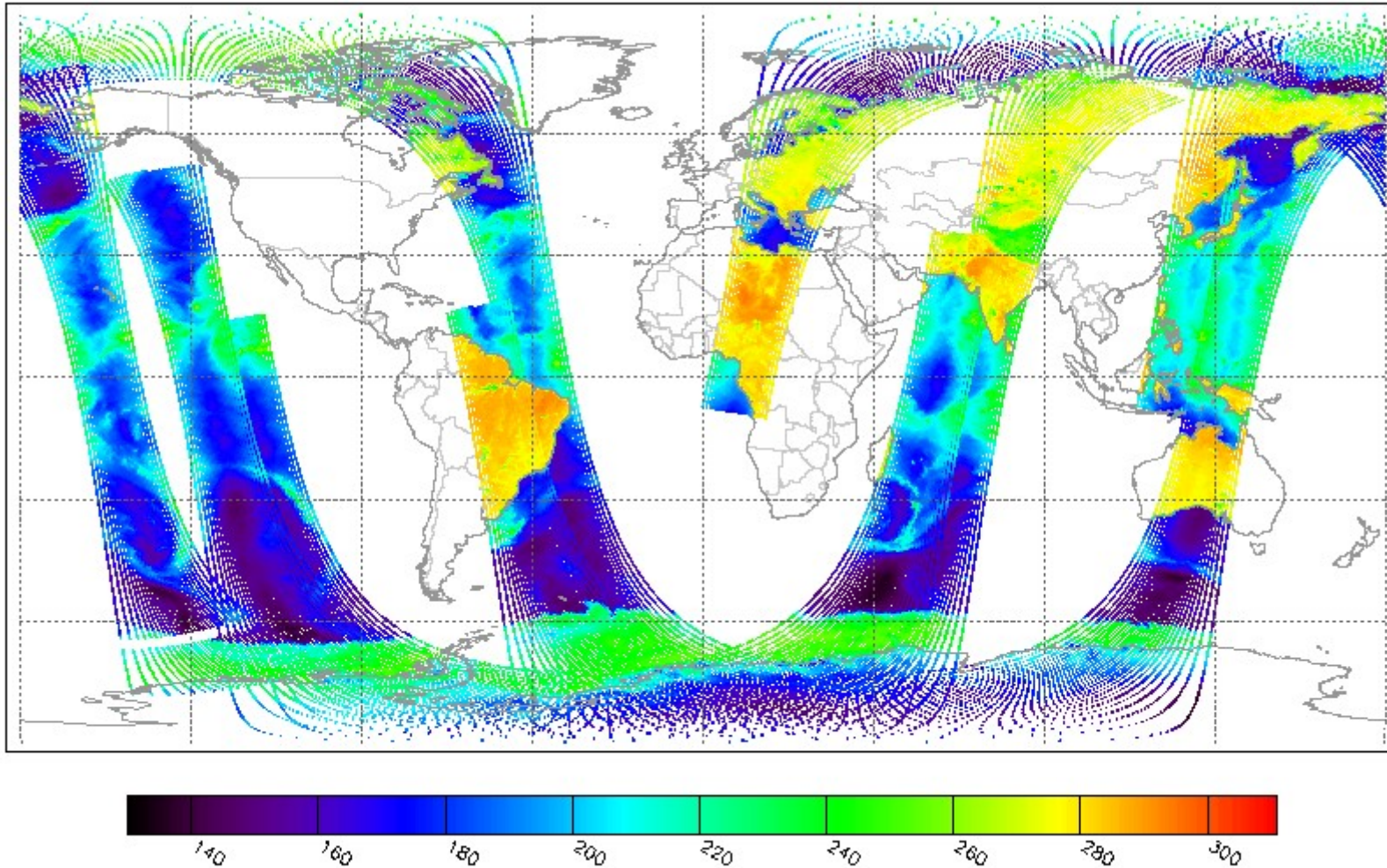
# Data Assimilation

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# Data Assimilation

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# Data Assimilation

Observation coverage

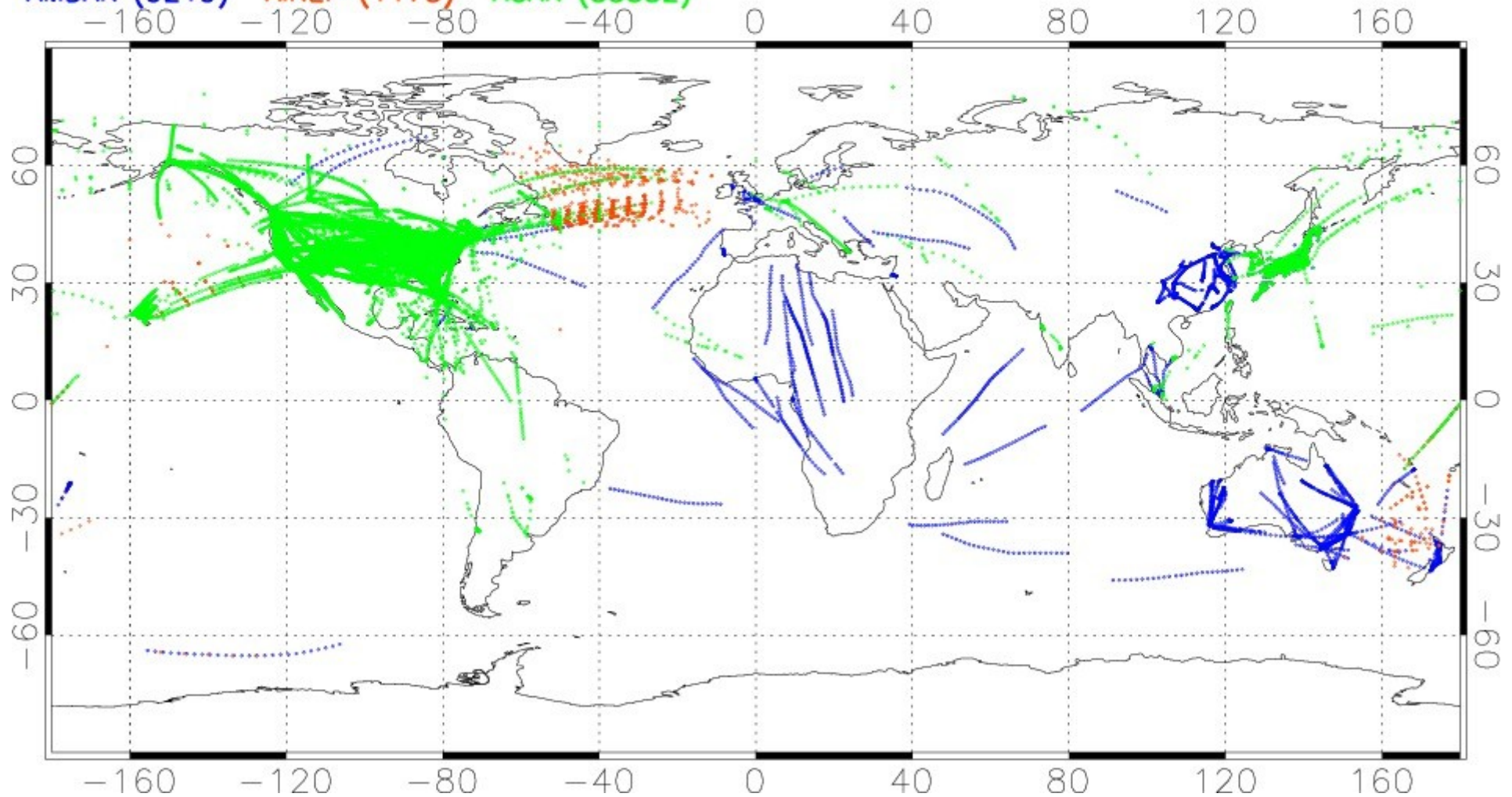
ass

Aircraft data

Date of Analyses: 2014050800

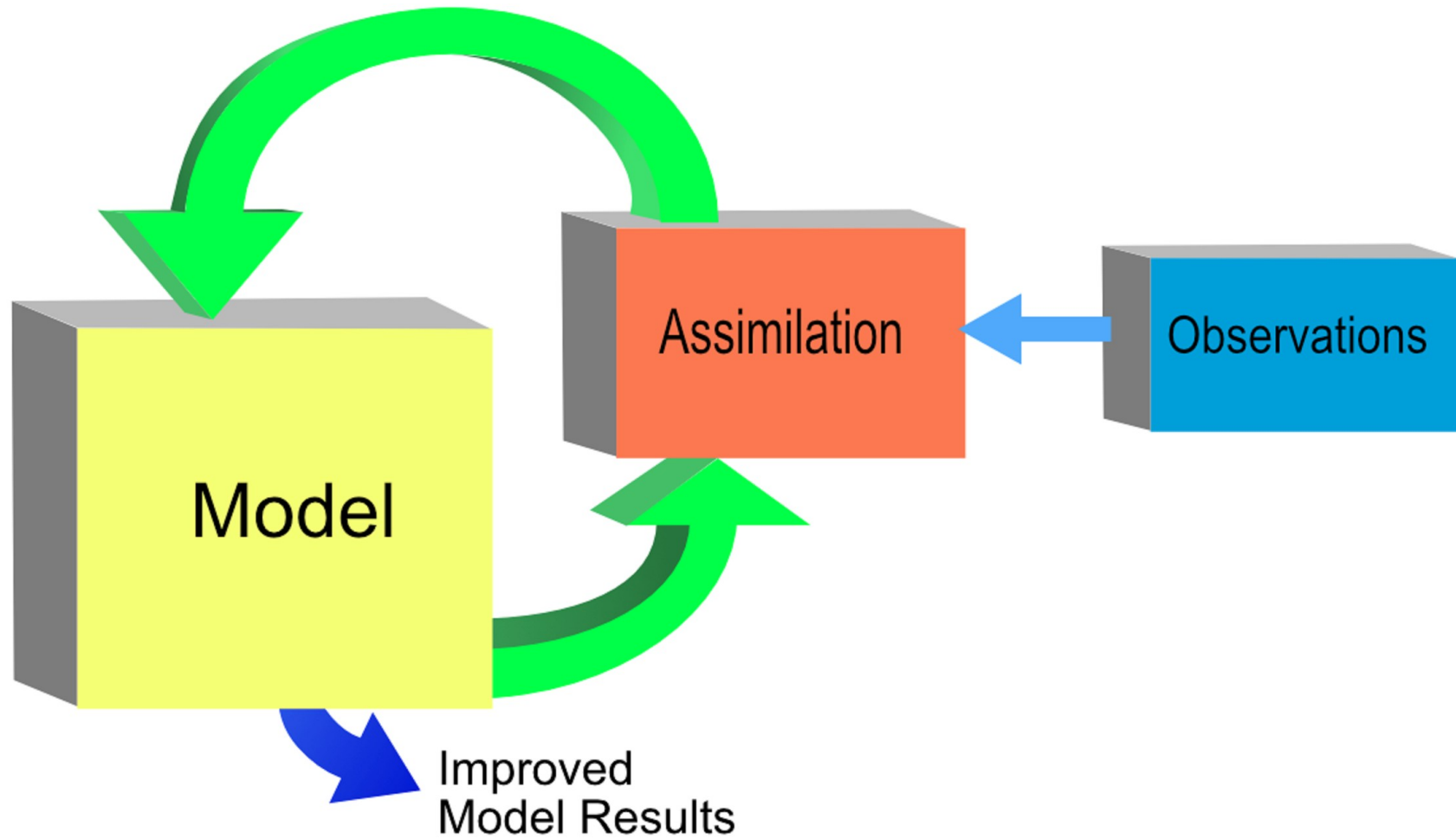
TIME : 22:30 – 01:29

AMDAR (9219) AIREP (1175) ACAR (55352)

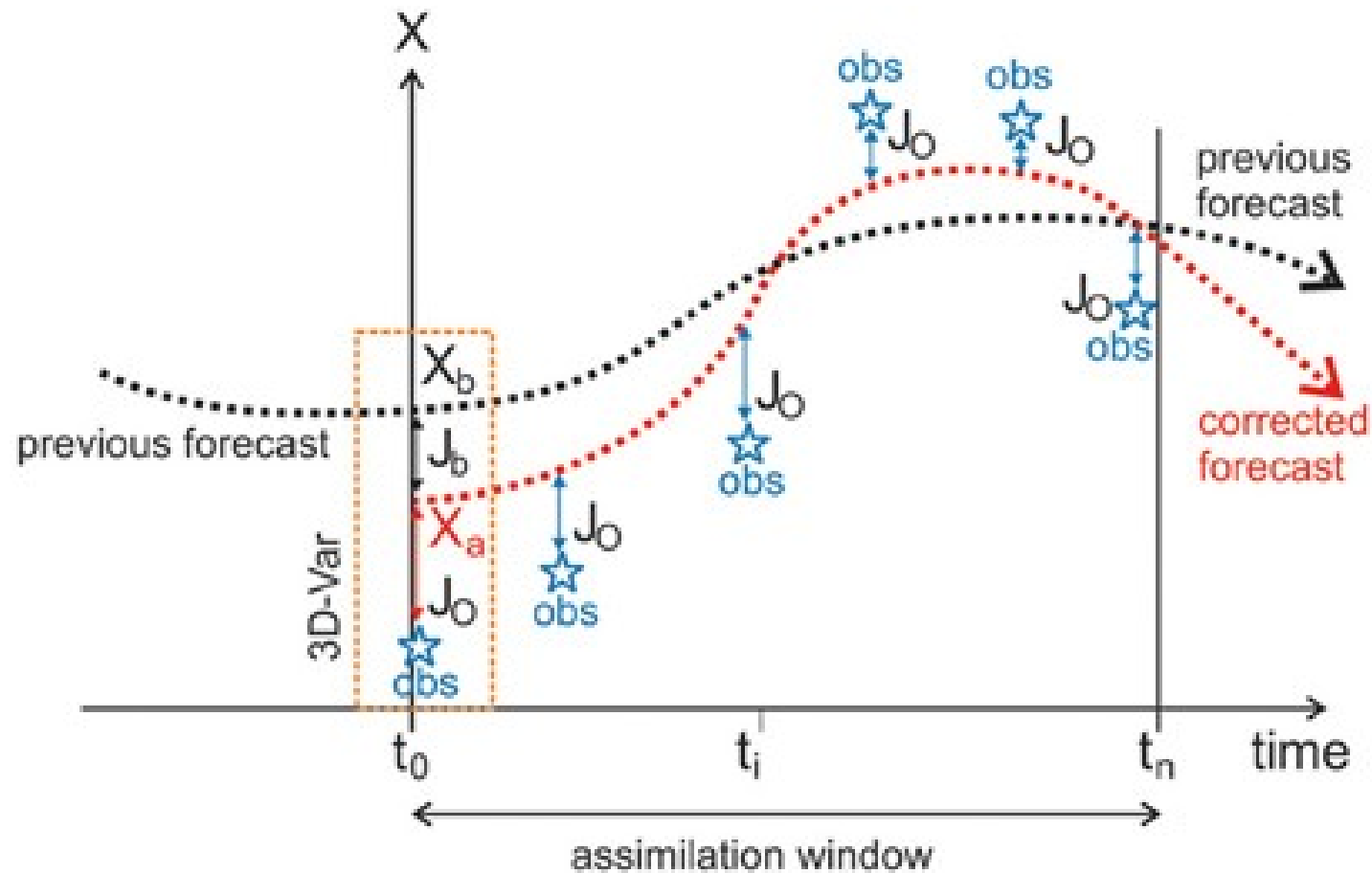


# Data Assimilation

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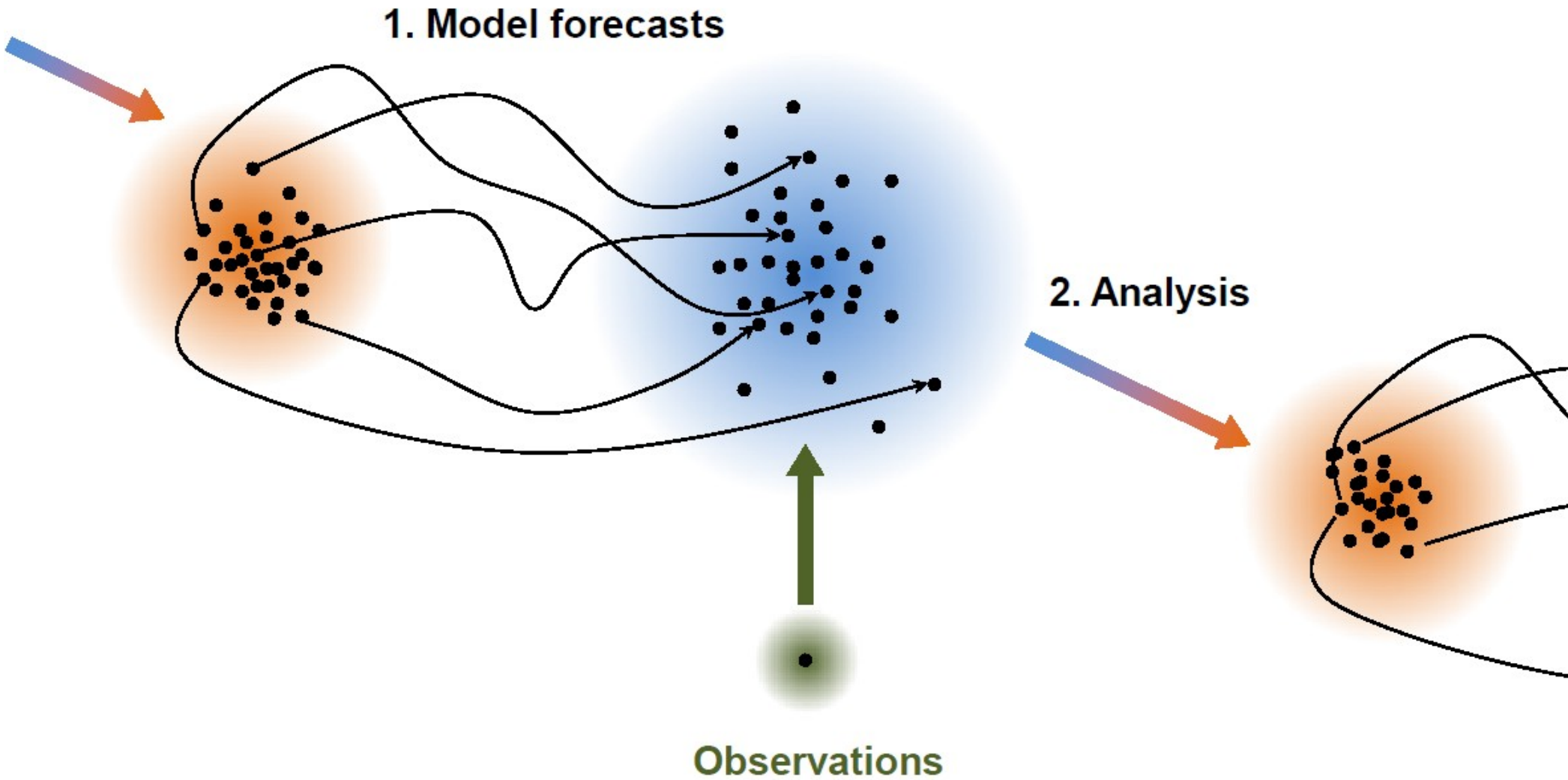


# Data Assimilation



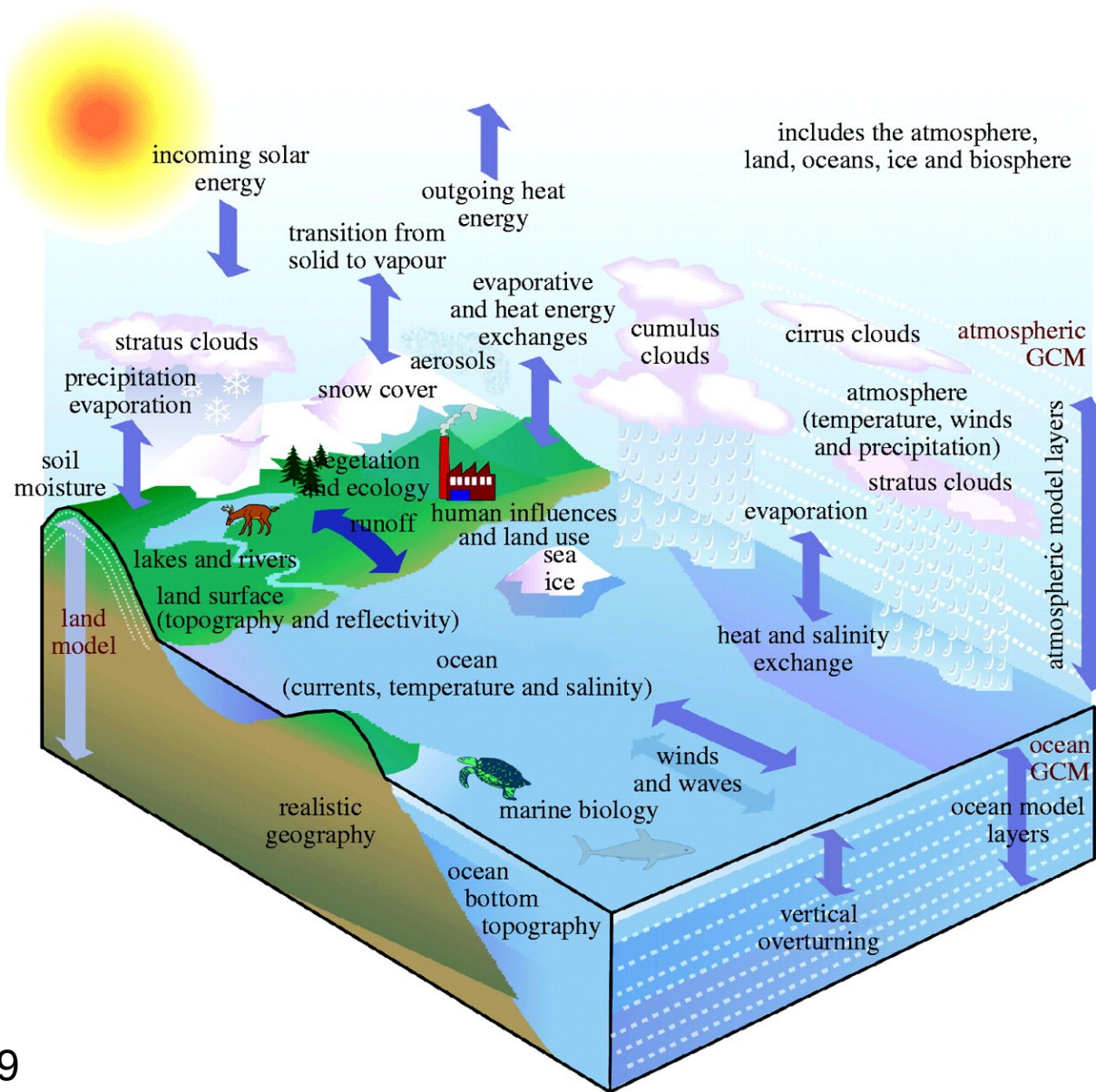
# Data Assimilation

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# Climate Models

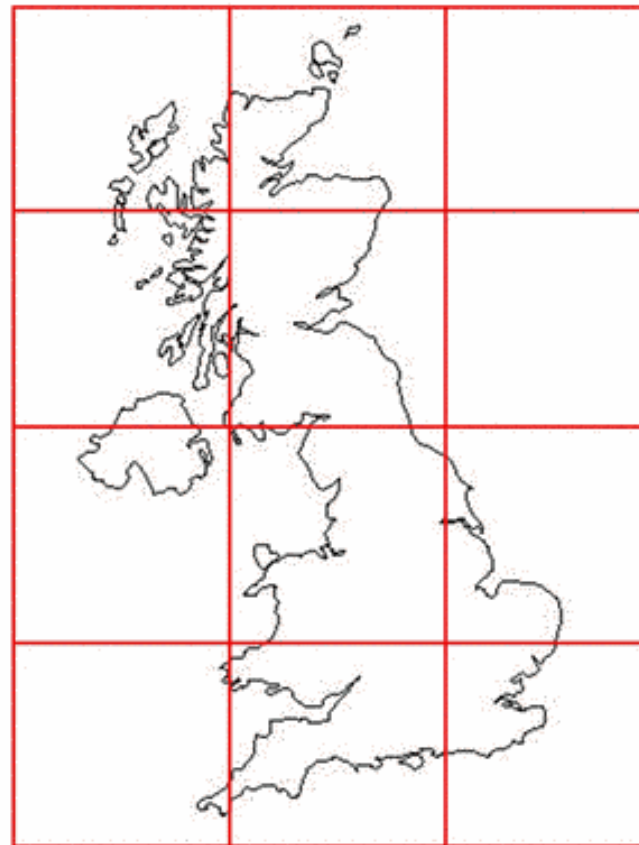


Washington et al. 2009

# Climate Models

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Typical grid for climate simulation:



← grid boxes

- GCMs **cannot resolve** many of the **most important processes** in the climate system

# Climate Models

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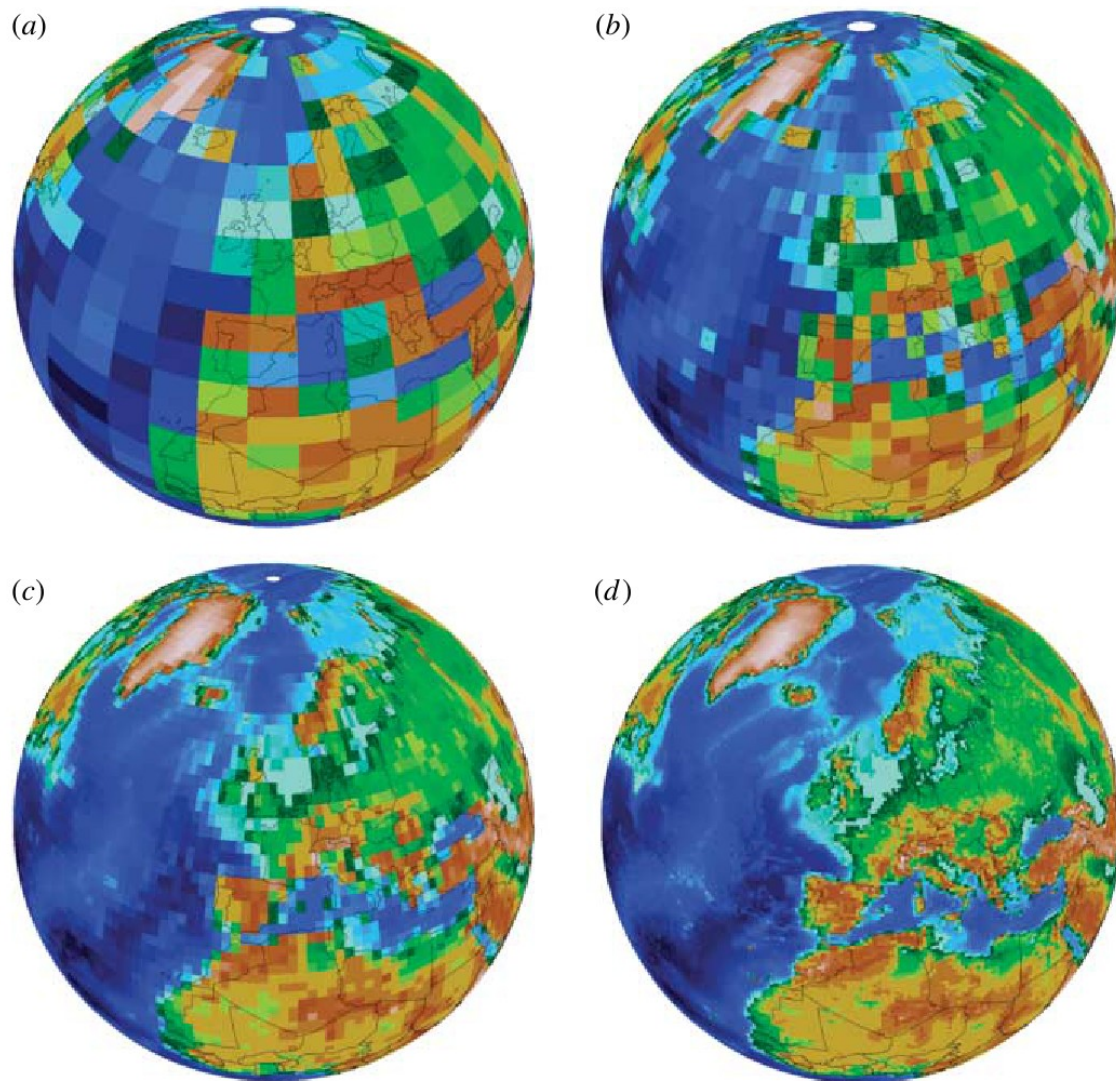


Figure 2. Horizontal resolution of the contemporary atmospheric and ocean climate model components. An approximate resolution of (a) 500 km, (b) 300 km, (c) 150 km and (d) 75 km.

Washington et al. 2009

# Climate Models

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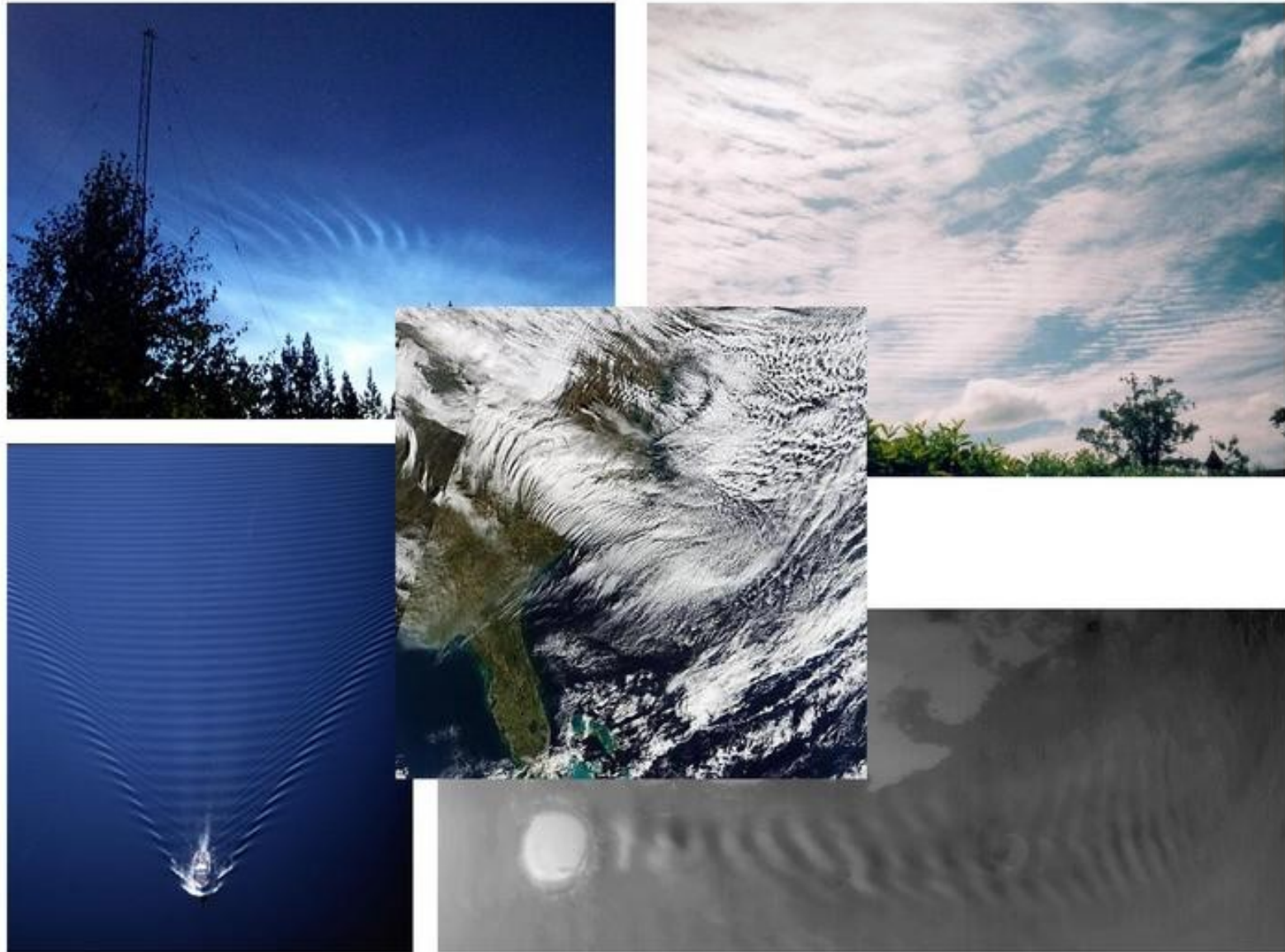
Physical Processes which need to be parameterized:

- Clouds
- Radiation
- Gravity Waves
- Convection
- Air-sea interaction
- Land surface-air interaction
- Turbulence
- Boundary-Layer Processes
- and many more



# Subgrid-Scale Processes

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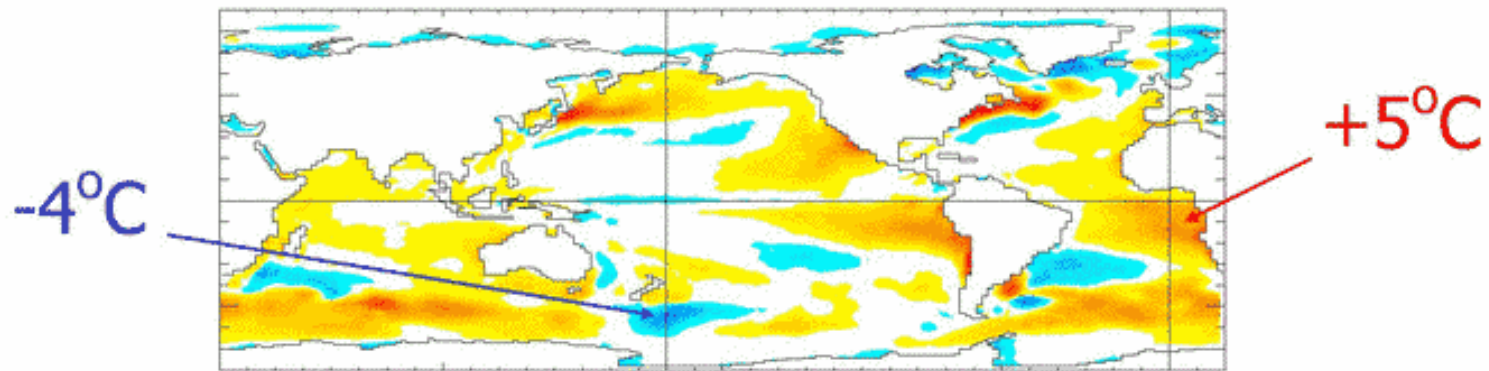
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Source: Paul Williams

# Subgrid-Scale Processes

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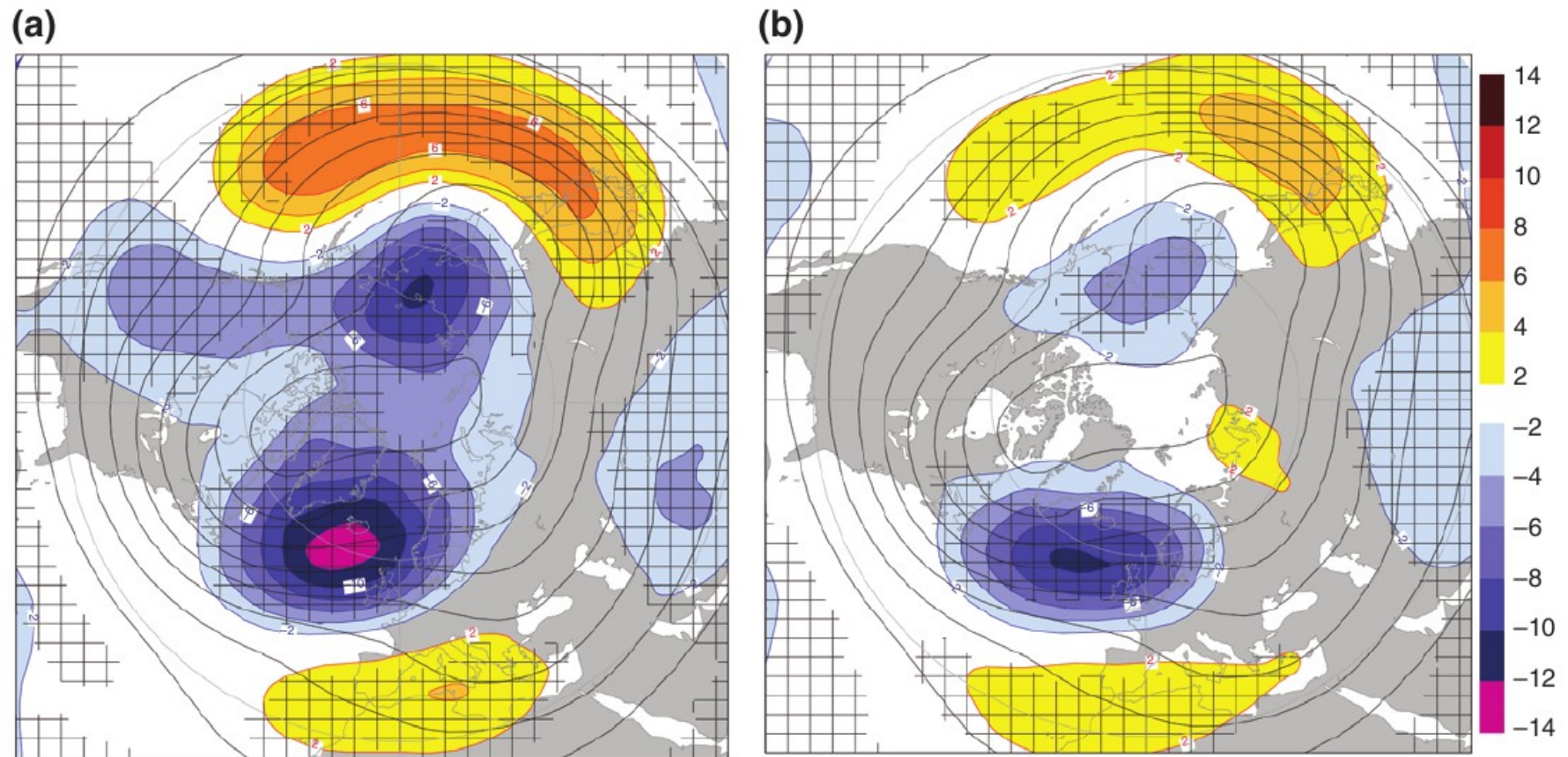
Systematic climate biases result:



*“to understand and characterise the important unresolved processes... in the climate system” is a “high priority area for action” (IPCC, 2001)*



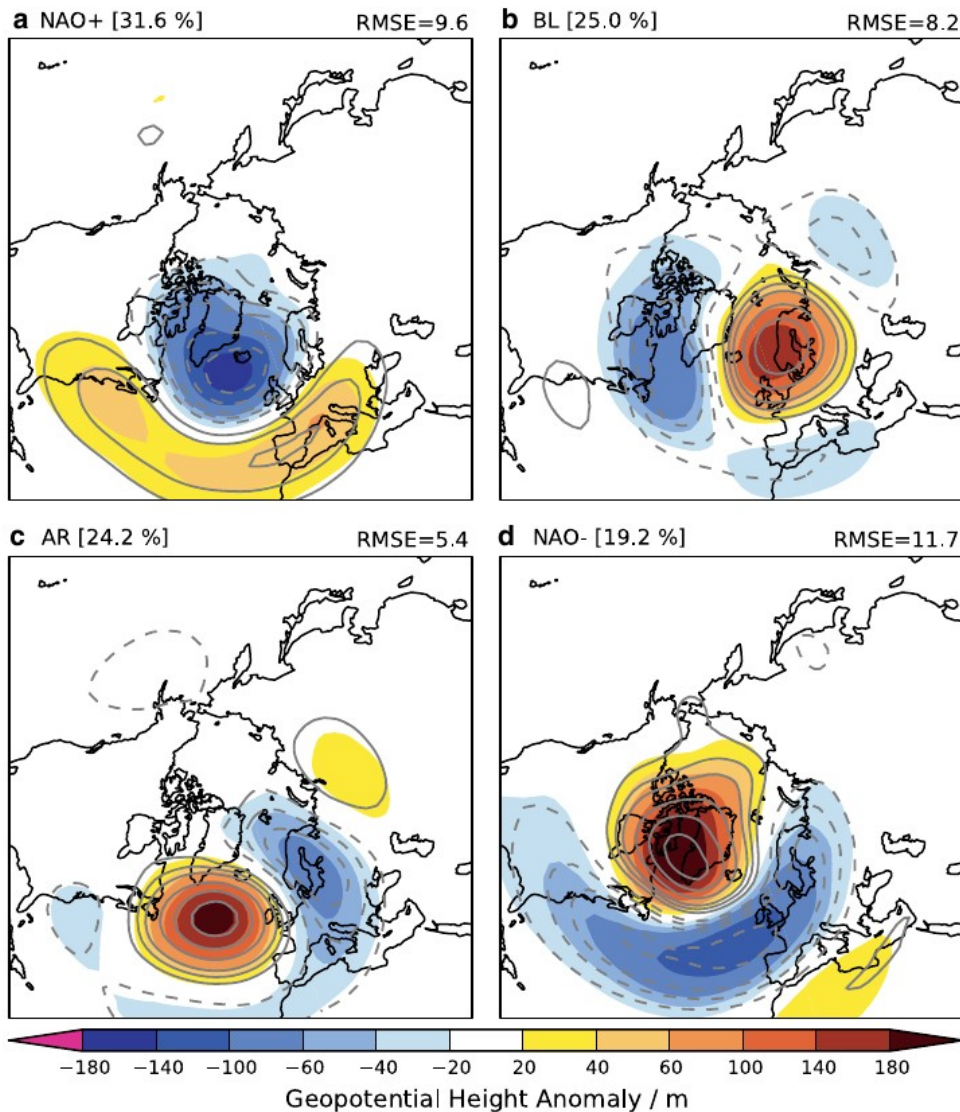
# Subgrid-Scale Processes



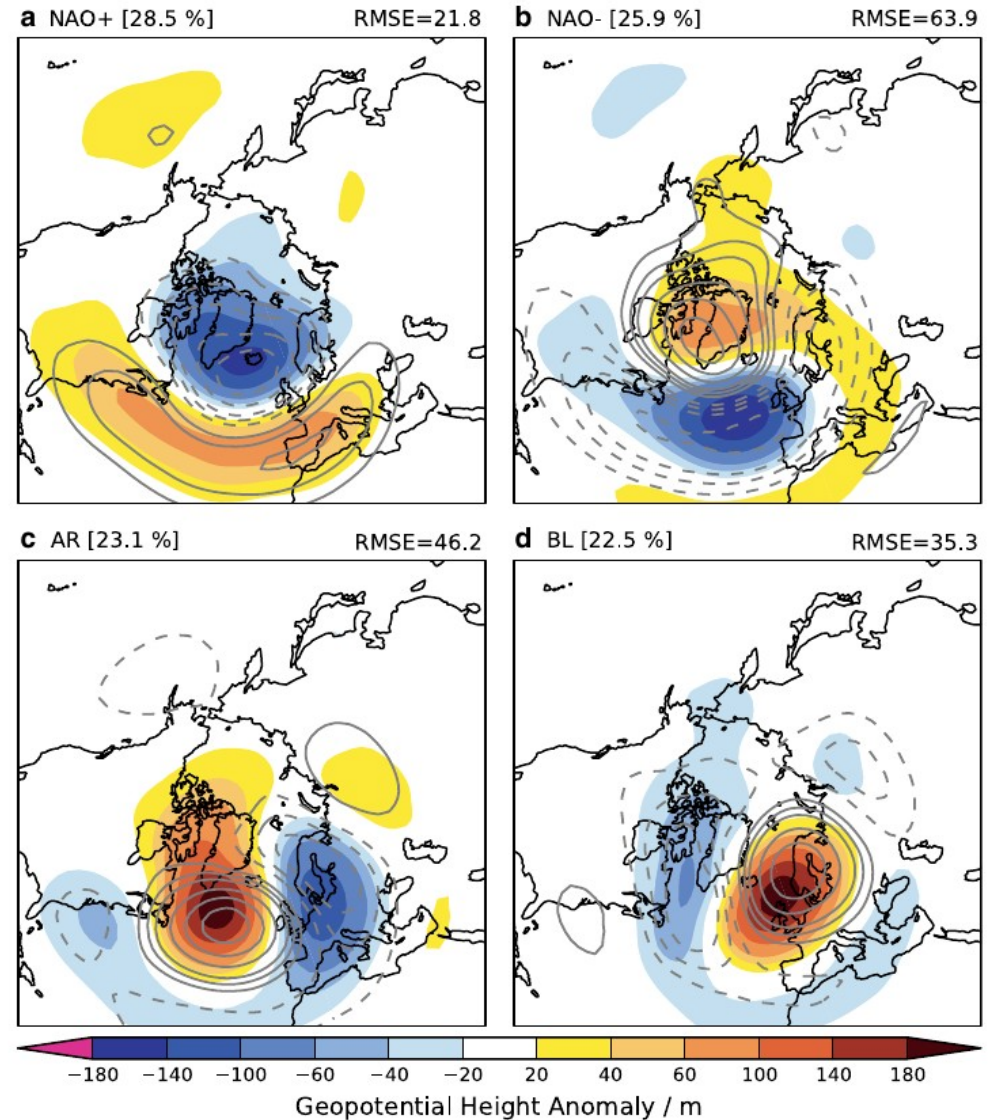
**FIGURE 2** | Mean systematic error of 500 hPa geopotential height fields (shading) for extended boreal winters (December–March) of the period 1962–2005. Errors are defined with regard to the observed mean field (contours), consisting of a combination of ERA-40 (1962–2001), and operational ECMWF analyses (2002–2005). (a) Systematic error in a numerical simulation with the ECMWF model IFS, version CY32R1, run at a horizontal resolution of  $T_L 95$  (about 210 km) and 91 vertical levels. (b) Systematic error in a simulation with a stochastic kinetic-energy backscatter scheme. Significant differences at the 95% confidence level based on a Student's  $t$ -test are hatched (after Berner et al.<sup>124</sup>).

# Subgrid-Scale Processes

T1279



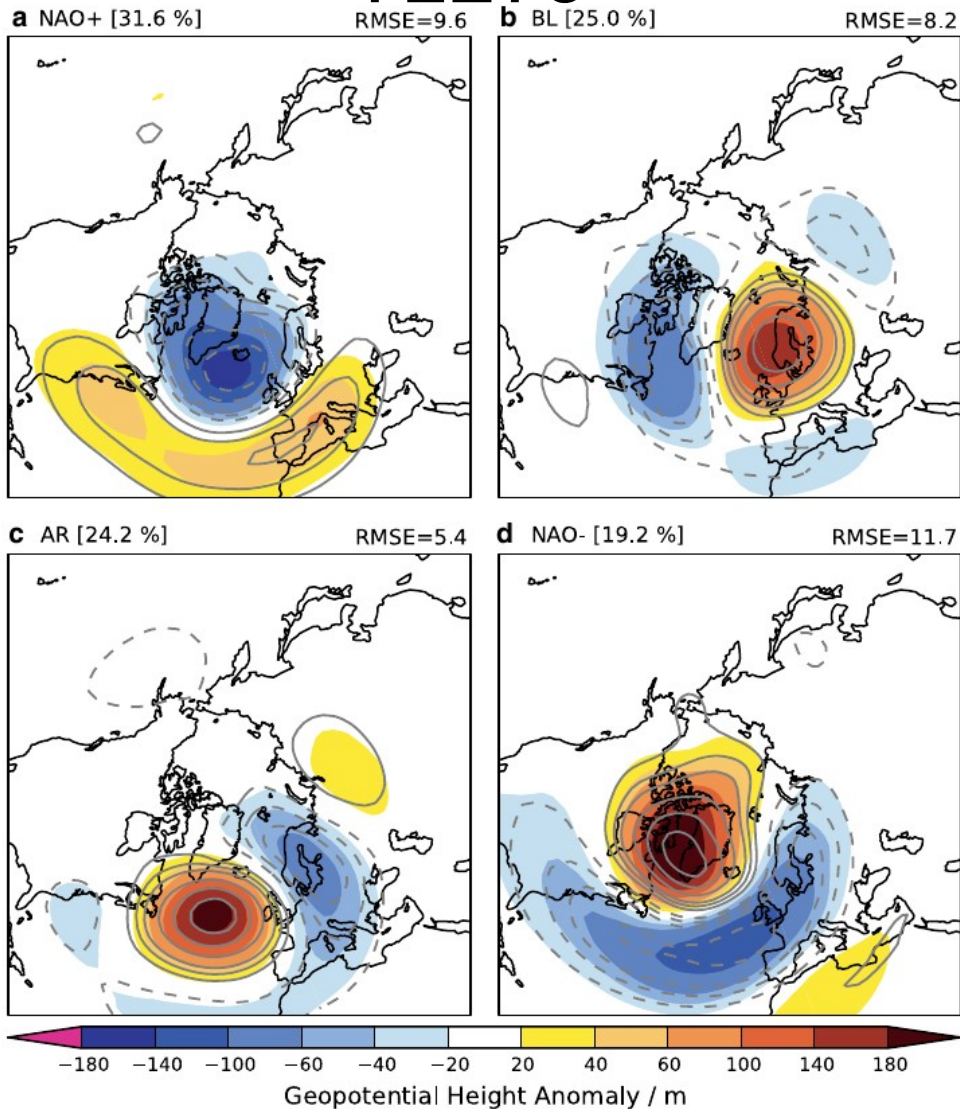
T159



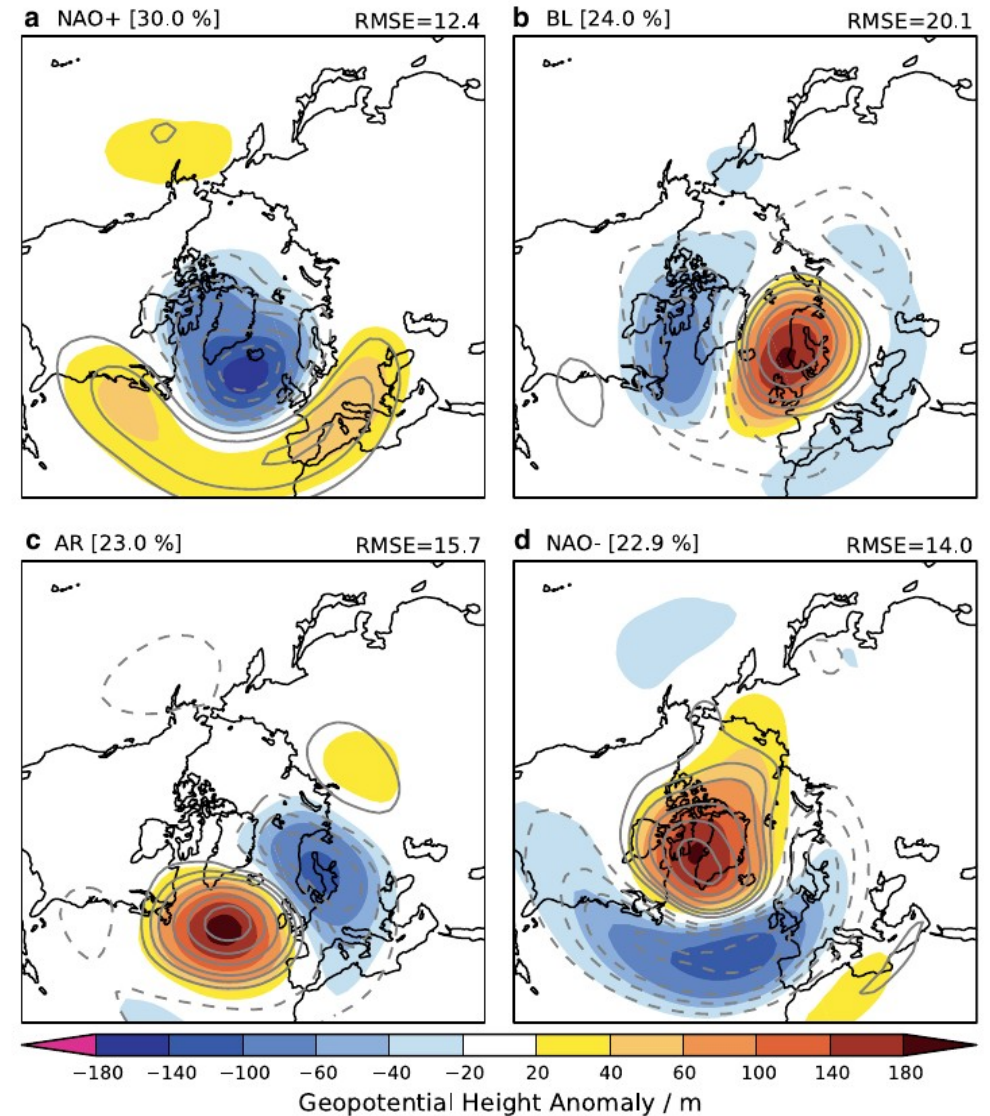


# Subgrid-Scale Processes

T1279



T159, Stochastic Physics



# Subgrid-Scale Processes

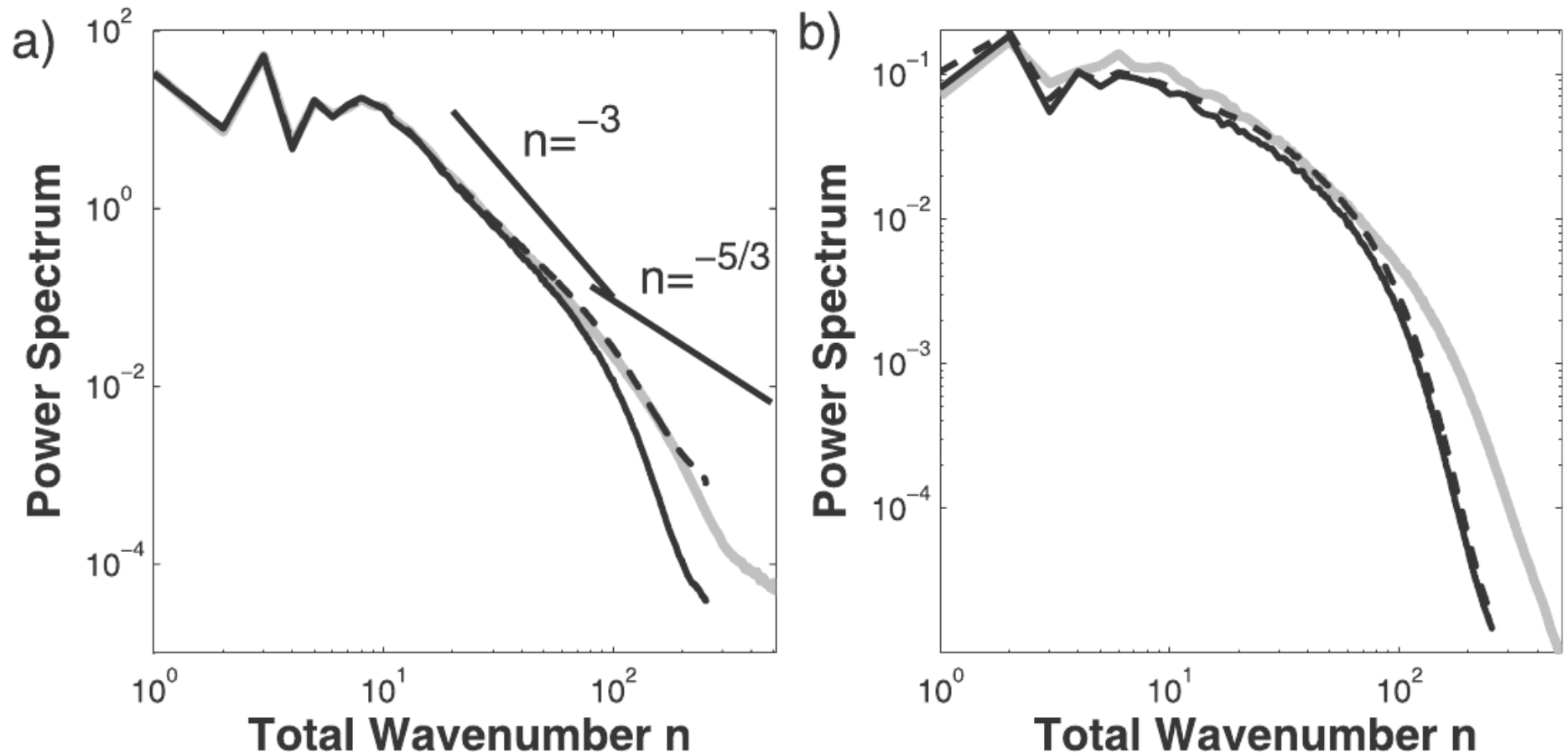


FIG. 6. Kinetic energy spectra for the (a) rotational and (b) divergent component of the flow for T<sub>L</sub>511 analysis (gray solid), forecasts with the operational ensemble configuration (OPER; black solid), and the ensemble system with stochastic backscatter (SSBS-FULLDISS; black dashed). Lines denote power-law behavior with slopes of  $-3$  and  $-5/3$ .

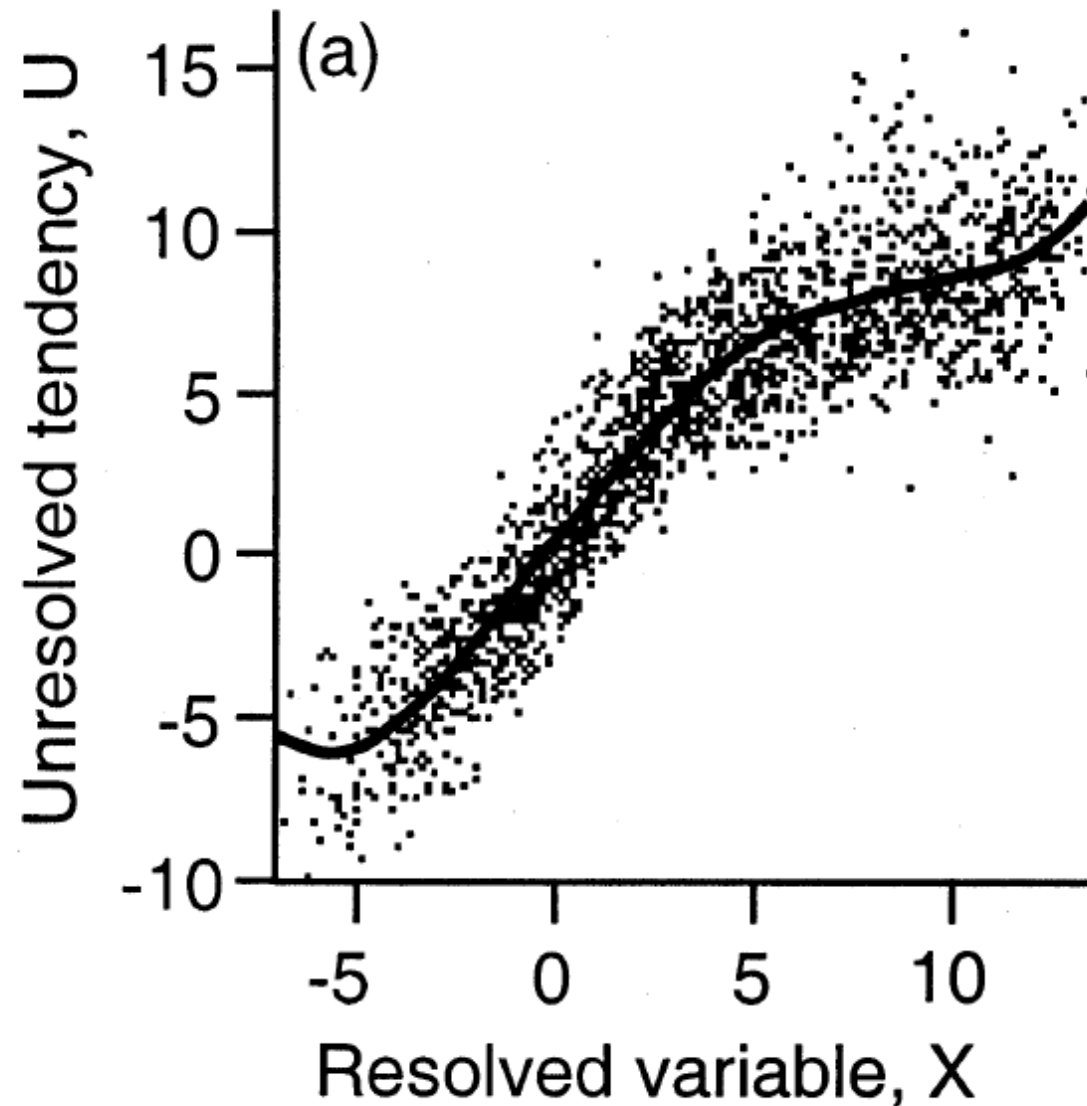
# Subgrid-Scale Processes

TABLE 4. Impact of stochastic backscatter scheme and reduced initial perturbations (SSBS-FULLDISS) when compared to OPER for NH and SH extratropics and tropics. Probabilistic skill scores are the BSS, ROC area, ISS, RPSS, percentage of outliers, and rank histogram at 48 h (RH48). Symbols represent the following impacts: +++ = very strong positive impact at all forecast lead times; ++ = strong positive impact at all forecast lead times; + = positive impact at all forecast lead times; ○ = neutral impact; – = negative impact all forecast lead times; ◁ = negative impact for shorter but positive impact for longer forecast lead times; ▷ = positive impact for shorter but negative impact for longer forecast lead times.

| Score      | Threshold      | NH        |           |           | SH        |           |           | Tropics   |           |           |
|------------|----------------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|-----------|
|            |                | $Z_{500}$ | $u_{850}$ | $T_{850}$ | $Z_{500}$ | $u_{850}$ | $T_{850}$ | $Z_{500}$ | $u_{850}$ | $T_{850}$ |
| BSS        | $> +1.5\sigma$ | +         | +         | +         | +         | +         | +         | ++        | ++        | ++        |
|            | $< -1.5\sigma$ | +         | +         | +         | +         | +         | +         | ++        | ++        | ++        |
| ROC        | $> +1.5\sigma$ | +         | +         | +         | +         | +         | +         | +         | +         | +         |
|            | $< -1.5\sigma$ | +         | +         | +         | +         | +         | +         | +         | +         | +         |
| ISS        | $> +1.5\sigma$ | ++        | ++        | ++        | +         | +         | +         | ++        | ++        | ++        |
|            | $< -1.5\sigma$ | ++        | ++        | ++        | +         | +         | +         | ++        | ++        | ++        |
| RPSS       |                | +         | +         | +         | +         | +         | +         | ++        | ++        | ++        |
| % outliers |                | +         | ++        | ◁         | +         | +         | ◁         | +         | ++        | ++        |
| RH48       |                | ++        | +         | +         | +         | +         | ○         | +         | +         | +         |

# Subgrid-Scale Processes

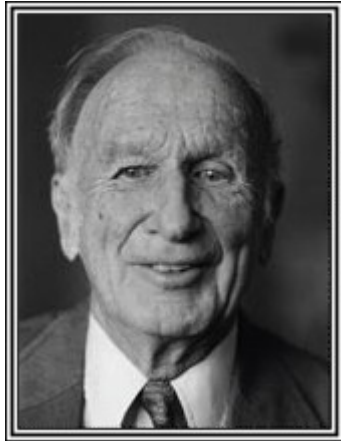
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# Lorenz 1996 Model

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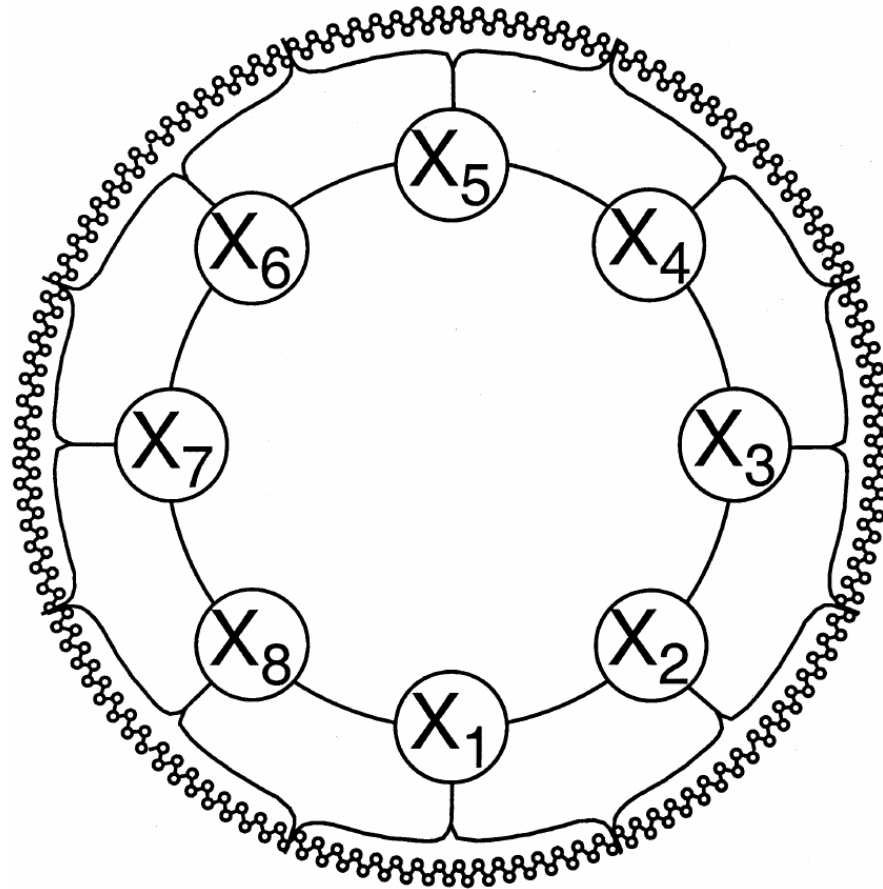
Edward N. Lorenz  
1917 – 2008

$$\frac{dX_k}{dt} = -X_{k-1}(X_{k-2} - X_{k+1}) - X_k + F - \frac{hc}{b} \sum_{j=J(k-1)+1}^{kJ} Y_j; \quad k = 1, \dots, K \quad (1a)$$

$$\frac{dY_j}{dt} = -cbY_{j+1}(Y_{j+2} - Y_{j-1}) - cY_j + \frac{hc}{b} X_{\text{int}[(j-1)/J]+1}; \quad j = 1, \dots, JK. \quad (1b)$$

# Lorenz 1996 Model

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# Exercise

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Write code for Lorenz96 model  
using a 4<sup>th</sup> order Runge-Kutta scheme

$$\frac{dX_k}{dt} = -X_{k-1}(X_{k-2} - X_{k+1}) - X_k + F - \frac{hc}{b} \sum_{j=J(k-1)+1}^{kJ} Y_j; \quad k = 1, \dots, K \quad (1a)$$

$$\frac{dY_j}{dt} = -cbY_{j+1}(Y_{j+2} - Y_{j-1}) - cY_j + \frac{hc}{b} X_{\text{int}[(j-1)/J]+1}; \quad j = 1, \dots, JK. \quad (1b)$$

F=10, h=c=b=1, K=8, J=6

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$$k_1 = f(z_n)$$

$$k_2 = f(z_n + d/2 k_1)$$

$$k_3 = f(z_n + d/2 k_2)$$

$$k_4 = f(z_n + d k_3)$$

$$z_{n+1} = z_n + \frac{d}{6} (k_1 + 2k_2 + 2k_3 + k_4)$$

d: time step size

Runge-Kutta Scheme