## Frequency response measurement

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## **Equations**

Digitizer: amplitude D(f), gain G(f). ACDC: DC voltage U, gain  $\Delta(f)$ . Source: Amplitude Z(f,t).

Given equations:

$$D(f,t) = Z(f,t) \cdot G(f) \tag{1}$$

$$U(f,t) = Z(f,t) \cdot \Delta(f) \tag{2}$$

Assuming:

$$t_H \approx t_L \implies Z|t_H = Zt_L$$
 (3)

Then:

$$D(f) = Z(f) \cdot G(f) \tag{4}$$

$$U(f) = Z(f) \cdot \Delta(f) \tag{5}$$

Measurements:

$$G_H = \frac{D_H}{Z_H}, \quad G_L = \frac{D_L}{Z_L}$$

$$Z_H = \frac{U_H}{\Delta_H}, \quad Z_L = \frac{U_L}{\Delta_L}$$
(6)

$$Z_H = \frac{U_H}{\Delta_H}, \quad Z_L = \frac{U_L}{\Delta_L} \tag{7}$$

Combining the equations:

$$\frac{G_H}{G_L} = \frac{D_H \cdot \Delta_H}{U_H} \cdot \frac{U_L}{D_L \cdot \Delta_L} \tag{8}$$

DC offset is not result of measurement and processing!

AC-DC measurements:

$$\Delta_L = 1 + \delta(f) \tag{9}$$

$$U_{\rm AC_{in}} = U_{\rm DC_{in}} \cdot (1 + \delta \cdot 10^{-1})$$
 (10)

With:

$$\delta_{792} = \frac{U_{\text{out}_{AC}} - U_{\text{out}_{DC}}}{n \cdot U_{\text{out}_{DC}}} \tag{11}$$