Caffeine and Memory A brief analysis

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Introduction

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 This will study the relationship between whether a person has just drank caffeine or not and their ability to improve on a memory test.
- I conjecture there is an association between people who drank caffeine before a memory test and people who improved on a memory test.

First, 80 people were randomly selected from the Island of Puama between the ages of 20 - 50 and given a DMA test. The next day, participants where split into two groups using random assignment. One group drank 250ml of caffeinated coffee before taking the DMA test again, and the other group drank 250ml of decaf coffee.

• Observational units: People from the town of Pauma.

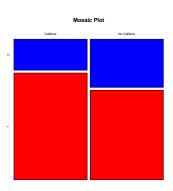
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- Explanatory variable: Whether a person had caffeine or not for the post treatment test (categorical)
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- It was difficult obtaining consent for 80 Islanders, and getting a wide age range.

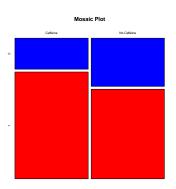
Descriptive Statistics

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There appears to be a minor or no association.

Analysis of Results

Null and alternative hypotheses.

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Since we used random sampling and random assignment, our measurements are a representative sample of people from the town of Pauma.

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- One sided p-value: p = 0.107

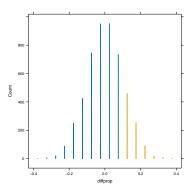
Assuming the null hypotheses, there is a 0.107 probability of achieving this statistic which is greater than 0.05, so we fail to reject the null. We have no evidence that drinking caffeine leads to an improvement in short term memory.

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The mean is 0.001. With our statistic of 31/40 - 26/40 = 0.125, and a standard deviation 0.102, we have a z-score of z = 0.125/0.102 = 1.225

Simulation Based Approach Cont.

With a z-score of 1.225, we have a p-value of 0.110. This is very similar to our theory based approach despite the validity conditions not being met. To find a 95% confidence interval, we take

$$(\hat{p}_t - \hat{p}_c) \pm \sigma = 0.125 \pm 0.102$$

Giving us a confidence interval of [-0.079, 0.329].

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 We are 95% confident that our parameter for the difference of proportions from the treatment and control is within the interval [-0.079, 0.329]. Since this interval contains 0, we fail to reject the null.

Discussion and Critique

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Next I would collect a bigger and more representative sample size. A further study could collect a quantitative response variable to measure memory for more in depth analysis.