Feature of the Newly Defined Helicity

The self helicity of the current-carrying field

$$H_{\mathrm{cj}} = \int_{\Omega} (\mathbf{A}_{\mathrm{c}} - \mathbf{A}_{\mathrm{p1}}) \cdot (\mathbf{B}_{\mathrm{c}} - \mathbf{B}_{\mathrm{p1}}) \mathrm{d}^{3} \vec{x}$$

 The mutual helicity of the current-carrying field and referenced field

$$H_{\rm cpj} = 2 \int_{\Omega} \mathbf{A}_{\rm p1} \cdot (\mathbf{B}_{\rm c} - \mathbf{B}_{\rm p1}) \mathrm{d}^3 \vec{x}$$

- \mathbf{B}_{p1} is very small -> small \mathbf{A}_{p1} -> small \mathbf{H}_{CPJ} and $\mathbf{H}_{cj} \sim \mathbf{H}_{j}$
- $H_{cr} \sim H_{cj} = H_j$

Applications

