

# Offline Imitation from Observation via Primal Wasserstein State Occupancy Matching





https://t.ly/yKi9V

their embedding

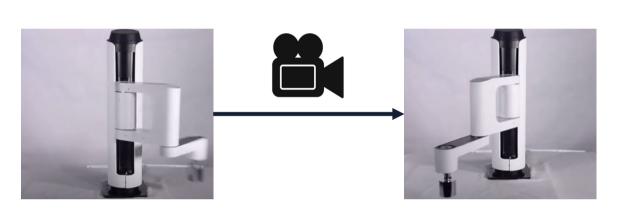
# ILLINOIS

# Motivation

Goal: Offline imitation Learning from Observation (LfO)

## Why from observations?

• Expert data are expensive, and action could be missing





Learning from video

Embodiment difference

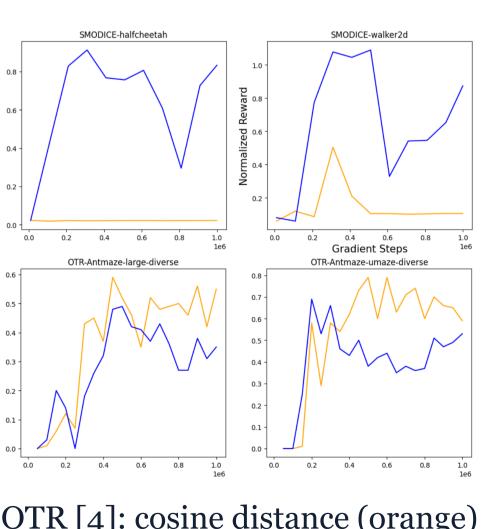
• Learning with few expert states + non-expert, mixedquality state-action data with unknown optimality

# Why Wasserstein distance?

- Prior works mostly use *f*-divergences, ignoring geometric distributions
- e.g., minimize state(-pair) occupancy KL [1, 2]

## Why Primal Wasserstein?

- Most Wasserstein-based methods use Rubinstein dual, which limits underlying distance metric to be Euclidean
- Underlying metric is crucial to Wasserstein-based offline imitation; selecting a good metric is important
- PWIL [3] uses only a surrogate of primal distance



#### OTR [4]: cosine distance (orange) vs. Euclidean (blue)

#### **Key Papers**

[1] Y. J. Ma et al. Smodice: Versatile offline imitation learning via state occupancy matching. In ICML, 2022. [2] G. hyeong Kim et al. Lobsdice: Offline learning from observation via stationary distribution correction estimation. In NeurIPS, 2022.

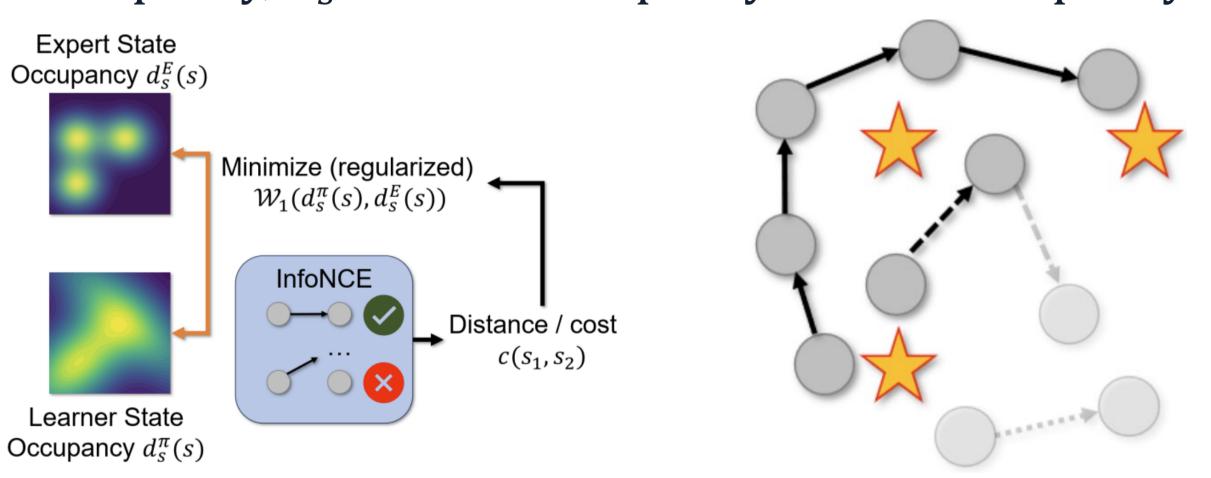
[3] R. Dadashi et al. Primal wasserstein imitation learning. In ICLR, 2021. [4] Y. Luo et al. Optimal Transport for offline imitation learning. In ICLR, 2023.

# **Formulation**

### **Primal problem:**

min  $\mathcal{W}(d_S^{\pi}, d_S^{E})$  + KL regularizers s.t.  $\pi$  is feasible

•  $\mathcal{W} = 1$ -Wasserstein distance,  $d_s^E$  is the expert's state occupancy,  $d_{S}^{\pi}$  is state occupancy of learner's policy  $\pi$ 



Wasserstein Optimization

Weighted Behavior Cloning

Contrastive learning for distance metric: weighted sum of reward R(s) by binary discriminator and a distance learned by InfoNCE based on reachability

States adjacent in a trajectory should have close embeddings, and vice versa

### Solve in the Lagrange dual space:

- Single-level convex optimization (logsumexp+linear) with Fenchel dual over Lagrange dual variables  $\lambda$
- Theoretical guarantee: equivalent to SMODICE with certain choice of coefficient for regularizers, and distance  $c(s_i, s_i)$  that is independent of  $s_i$

Learning Policy: weighted behavior cloning

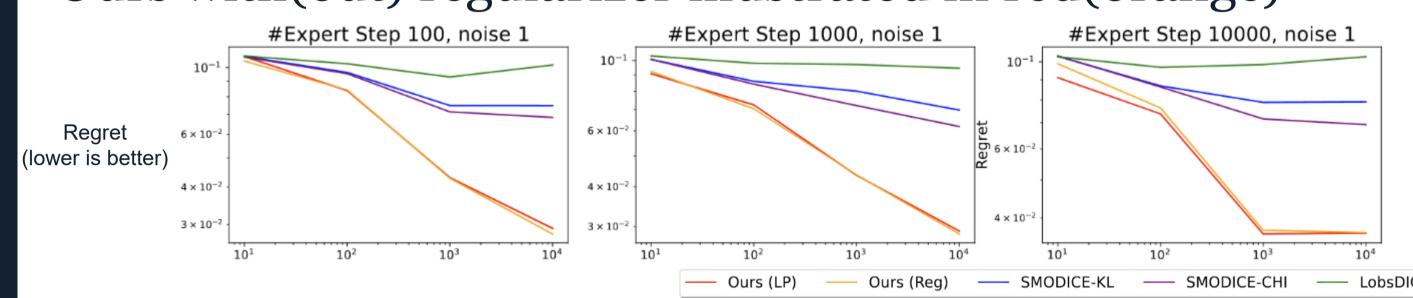
• weight  $w(s_i, a_i, s_k) \propto \exp(\limsup function of \lambda)$ 

# Results

#### Tabular MDP

Optimized with CVXPY

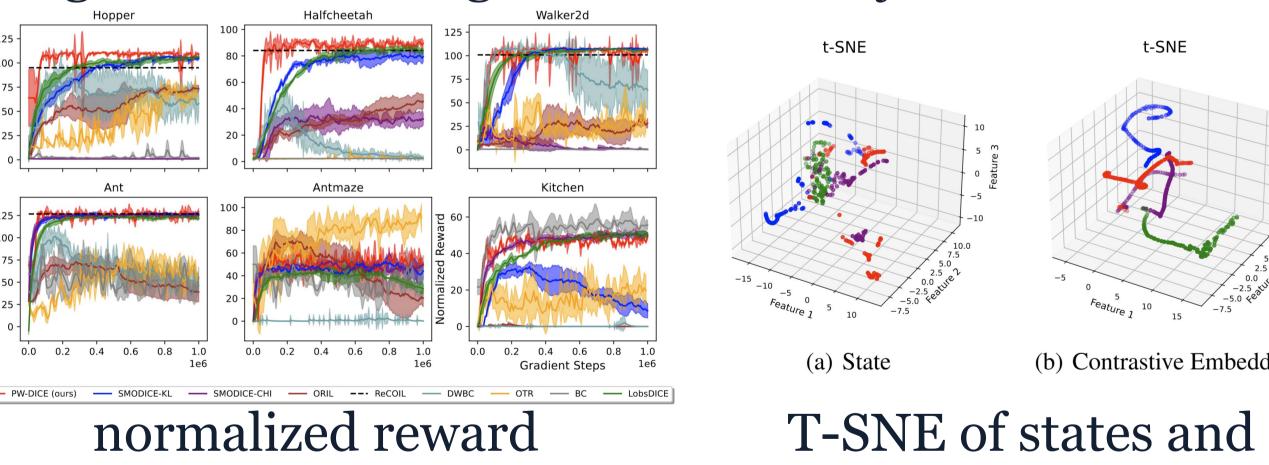
Ours with(out) regularizer illustrated in red(orange)



### **Mujoco Environments**

Optimized with neural network

Our results illustrated in red outperform baselines and bring state embeddings in the same trajectories close



# Conclusion

Our key contribution:

(higher is better)

- Shed light on importance of used distance metric
- A novel LfO method generalizing, outperforming and removing theoretical assumption [1] of prior work
- Limitation:
  - Biased estimation of logsumexp in objective