Homework Assignment 4 (Due Wednesday, March 9, 2022)

The homework is due at 10.30am in the dropbox on the Course Plus page (you can find the dropbox under the 'Resources' tab in the upper right). For exercises involving R code, please knit a document from your R markdown (Rmd) file. Generate a single pdf file for your entire submission and give it a name that makes it identifiable (calling it 140.615.HW.Number.Lastname.Firstname or similar). Show your work.

1. Suppose I measure some treatment response on a set of 10 mice from strain A, and get these data:

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84 106 99 101 100 99 127 105 101 108
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Suppose I measure the same treatment response on a set of 5 mice from strain B, and get these data:

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56 62 67 81 69
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Calculate a 95% and a 99% confidence interval for the difference in the mean treatment responses of strains A and B, assuming that the standard deviations within the two groups are the same. What is the p-value for the hypothesis test that the means are the same?

- 2. Suppose we wish to estimate the concentration (in $\mu g/ml$) of a specific dose of ampicillin in urine. We recruit 25 volunteers and find that they have a sample mean concentration of 7.0 $\mu g/ml$, and a sample standard deviation 3.0 $\mu g/ml$. Find a 90% confidence interval for the population mean concentration, assuming that the underlying population distribution of concentrations is normal.
- 3. Consider data for some measurement on 6 mice before and after some treatment.

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Mouse 1 2 3 4 5 6

Before 81 101 76 67 125 144

After 138 210 162 105 259 319
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Does the treatment have an effect?

- 4. E.canis infection is a tick-borne disease of dogs that is sometimes contracted by humans. Among infected humans, the distribution of white blood cell counts has an unknown mean μ and an unknown standard deviation σ . In the general population, the mean white blood cell count is $7250/\text{mm}^3$. It is believed that persons infected with E.canis must on average have a lower white blood cell count.
 - (a) What are the null and alternative hypotheses for a one-sided test?
 - (b) For a sample of 15 infected persons, the mean white blood cell count is $\bar{x} = 4767/\text{mm}^3$, and the standard deviation is $s = 3204/\text{mm}^3$. Carry out the one-sided test using a 0.05 significance level.
 - (c) What do you conclude?