

P 3.1

25g fat 32g protein.

$$x = 1\text{g fat} + 2\text{g protein}$$

$$y = 5\text{g fat} + 1\text{g protein.}$$

$$\left(\begin{array}{cc|c} 1 & 5 & 25 \\ 2 & 1 & 32 \end{array} \right).$$

$x \quad y.$

$$\underset{\sim}{R_2 \rightarrow R_2 - 2R_1} \left(\begin{array}{cc|c} 1 & 5 & 25 \\ 0 & -9 & -18 \end{array} \right).$$

$$\underset{\sim}{R_2 \rightarrow -\frac{1}{9}R_2} \left(\begin{array}{cc|c} 1 & 5 & 25 \\ 0 & 1 & 2 \end{array} \right).$$

$$\underset{\sim}{R_1 \rightarrow R_1 - 5R_2} \left(\begin{array}{cc|c} 1 & 0 & 15 \\ 0 & 1 & 2 \end{array} \right).$$

$x \quad y.$

should eat 15 units of x and
2 units of y

$$P3.3) a) \begin{pmatrix} -1 & -2 & | & -2 \\ 3 & 3 & | & 0 \end{pmatrix}$$

$$R_2 \rightarrow \frac{1}{3}R_2 \sim \begin{pmatrix} -1 & -2 & | & -2 \\ 1 & 1 & | & 0 \end{pmatrix}$$

$$R_1 \leftrightarrow R_2 \sim \begin{pmatrix} 1 & 1 & | & 0 \\ -1 & -2 & | & -2 \end{pmatrix}$$

$$R_2 \rightarrow R_2 + R_1 \sim \begin{pmatrix} 1 & 1 & | & 0 \\ 0 & -1 & | & -2 \end{pmatrix}$$

$$R_2 \rightarrow -R_2 \sim \begin{pmatrix} 1 & 1 & | & 0 \\ 0 & 1 & | & 2 \end{pmatrix} \sim \begin{pmatrix} 1 & 0 & | & -2 \\ 0 & 1 & | & 2 \end{pmatrix}$$

$(-2, 2)$

P3.3b).

$$\begin{pmatrix} 1 & -1 & -2 & | & 1 \\ -2 & 3 & 3 & | & -1 \\ -1 & 0 & 1 & | & 2 \end{pmatrix}.$$

$$R_2 \rightarrow R_2 + 2R_1 \sim \begin{pmatrix} 1 & -1 & -2 & | & 1 \\ 0 & 1 & -1 & | & 1 \\ -1 & 0 & 1 & | & 2 \end{pmatrix}.$$

$$R_3 \rightarrow R_3 + R_1 \sim \begin{pmatrix} 1 & -1 & -2 & | & 1 \\ 0 & 1 & -1 & | & 1 \\ 0 & -1 & -1 & | & 3 \end{pmatrix}.$$

$$R_3 \rightarrow R_3 + R_2 \sim \begin{pmatrix} 1 & -1 & -2 & | & 1 \\ 0 & 1 & -1 & | & 1 \\ 0 & 0 & -2 & | & 4 \end{pmatrix}.$$

$$R_3 \rightarrow -\frac{1}{2}R_3 \sim \begin{pmatrix} 1 & -1 & -2 & | & 1 \\ 0 & 1 & -1 & | & 1 \\ 0 & 0 & 1 & | & -2 \end{pmatrix}.$$

$$R_2 \rightarrow R_2 + R_3 \sim \begin{pmatrix} 1 & -1 & -2 & | & 1 \\ 0 & 1 & 0 & | & -1 \\ 0 & 0 & 1 & | & -2 \end{pmatrix}$$

$$\sim \begin{pmatrix} 1 & 0 & -2 & | & 0 \\ 0 & 1 & 0 & | & -1 \\ 0 & 0 & 1 & | & -2 \end{pmatrix}$$

$$\sim \begin{pmatrix} 1 & 0 & 0 & | & -4 \\ 0 & 1 & 0 & | & -1 \\ 0 & 0 & 1 & | & -2 \end{pmatrix}$$

$$c) \left(\begin{array}{ccc|c} 2 & -2 & 3 & 2 \\ 1 & -2 & -1 & 0 \\ -2 & 2 & 2 & 1 \end{array} \right)$$

$$R_1 \rightarrow R_1 - R_2 \sim \left(\begin{array}{ccc|c} 1 & 0 & 4 & 2 \\ 1 & -2 & -1 & 0 \\ -2 & 2 & 2 & 1 \end{array} \right)$$

$$R_2 \rightarrow R_2 - R_1 \sim \left(\begin{array}{ccc|c} 1 & 0 & 4 & 2 \\ 0 & -2 & -5 & -2 \\ -2 & 2 & 2 & 1 \end{array} \right)$$

$$R_3 \rightarrow R_3 + 2R_2 \sim \left(\begin{array}{ccc|c} 1 & 0 & 4 & 2 \\ 0 & -2 & -5 & -2 \\ 0 & 2 & 10 & 5 \end{array} \right)$$

$$R_3 \rightarrow R_3 + R_2.$$

$$\sim \begin{pmatrix} 1 & 0 & 4 & | & 2 \\ 0 & -2 & -5 & | & -2 \\ 0 & 0 & 5 & | & 3 \end{pmatrix}$$

$$R_3 \rightarrow \frac{1}{5}R_3$$

$$\sim \begin{pmatrix} 1 & 0 & 4 & | & 2 \\ 0 & -2 & -5 & | & -2 \\ 0 & 0 & 1 & | & \frac{3}{5} \end{pmatrix}$$

$$R_2 \rightarrow R_2 \times -\frac{1}{2}$$

$$\sim \begin{pmatrix} 1 & 0 & 4 & | & 2 \\ 0 & 1 & \frac{5}{2} & | & 1 \\ 0 & 0 & 1 & | & \frac{3}{5} \end{pmatrix}$$

$$R_1 \rightarrow R_1 - 4R_3$$

$$\sim \begin{pmatrix} 1 & 0 & 0 & | & \frac{2}{5} \\ 0 & 1 & 0 & | & 1 \\ 0 & 0 & 1 & | & \frac{3}{5} \end{pmatrix} \text{ s.t. } \underline{\underline{(-\frac{2}{5}, 1, \frac{3}{5})}}$$

$$P3.4a). \left(\begin{array}{cc|c} -1 & -2 & -2 \\ 3 & 6 & 6 \end{array} \right)$$

$$R_2 \rightarrow R_2 + 3R_1 \sim \left(\begin{array}{cc|c} -1 & -2 & -2 \\ 0 & 0 & 0 \end{array} \right).$$

Since we are solving 2 var with

1 eqn,
there are inf sols.

basic var = x_1 .

free: x_2 .

$$x_1 + 2x_2 = 2.$$

Let $x_2 = t$.

$$x_1 = 2 - 2t.$$

a soln x ,

$$x = \begin{pmatrix} x_1 \\ x_2 \end{pmatrix} = \begin{pmatrix} 2 - 2t \\ t \end{pmatrix}$$

$$= \begin{pmatrix} 2 \\ 0 \end{pmatrix} + t \begin{pmatrix} -2 \\ 1 \end{pmatrix}$$

for $\forall t \in \mathbb{R}$

$$b) \begin{pmatrix} 1 & -1 & -2 & | & 1 \\ -2 & 3 & 3 & | & -1 \\ -1 & 2 & 1 & | & 0 \end{pmatrix}$$

$$\begin{matrix} R_2 \rightarrow R_2 + 2R_1 \\ \sim \end{matrix} \begin{pmatrix} 1 & -1 & -2 & | & 1 \\ 0 & 1 & -1 & | & 1 \\ -1 & 2 & 1 & | & 0 \end{pmatrix}$$

$$\begin{matrix} R_3 \rightarrow R_3 + R_1 \\ \sim \end{matrix} \begin{pmatrix} 1 & -1 & -2 & | & 1 \\ 0 & 1 & -1 & | & 1 \\ 0 & 1 & -1 & | & 1 \end{pmatrix}$$

$$\begin{matrix} R_3 \& R_2 \\ \text{these are} \\ \sim \end{matrix} \begin{pmatrix} 1 & -1 & -2 & | & 1 \\ 0 & 1 & -1 & | & 1 \\ 0 & 0 & 0 & | & 0 \end{pmatrix}$$

basic var: x_1, x_2 .

free var: x_3 .

Since a line + since there is 1 free var.

$$\text{let } x_3 = t.$$

$$x_1 - x_2 - x_3 = 1.$$

$$x_2 - x_3 = 1$$

$$\therefore \left\{ \begin{pmatrix} 2 \\ 1 \\ 0 \end{pmatrix} + t \begin{pmatrix} 2 \\ 1 \\ 1 \end{pmatrix} \right. \quad \begin{array}{l} \cancel{x_3 = t} \\ x_2 = \underline{1+t} \end{array}$$

XD copy
why?

$$\begin{aligned} x_1 &= x_2 + x_3 + 1 \\ &= 1 + t + t + 1 \\ &= \underline{\underline{2 + 2t}}. \end{aligned}$$

$$c) \begin{pmatrix} 2 & -2 & 3 & | & 2 \\ 0 & 0 & 5 & | & 3 \\ -2 & 2 & 2 & | & 1 \end{pmatrix}$$

$$R_2 \rightarrow R_1 \times \frac{1}{5} \sim \begin{pmatrix} 1 & -1 & \frac{3}{5} & | & \frac{1}{5} \\ 0 & 0 & 5 & | & 3 \\ -2 & 2 & 2 & | & 1 \end{pmatrix}$$

$$R_3 \rightarrow R_3 + 2R_1 \sim \begin{pmatrix} 1 & -1 & \frac{3}{5} & | & \frac{1}{5} \\ 0 & 0 & 5 & | & 3 \\ 0 & 0 & 5 & | & 3 \end{pmatrix}$$

$$\sim \begin{pmatrix} 1 & -1 & \frac{3}{5} & | & \frac{1}{5} \\ 0 & 0 & 5 & | & 3 \\ 0 & 0 & 0 & | & 0 \end{pmatrix}$$

x_1, x_3 are basic vars.

free: x_2 .

Let $x_2 = t$.

$$x_1 = 1 + x_2 - \frac{3}{5}x_3$$

$$x_2 = t$$

$$x_3 = \frac{3}{5}$$

$$\left\{ \begin{pmatrix} 1 \\ 0 \\ \frac{3}{5} \end{pmatrix} + t \begin{pmatrix} 1 \\ 1 \\ 0 \end{pmatrix}, t \in \mathbb{R} \right\}$$