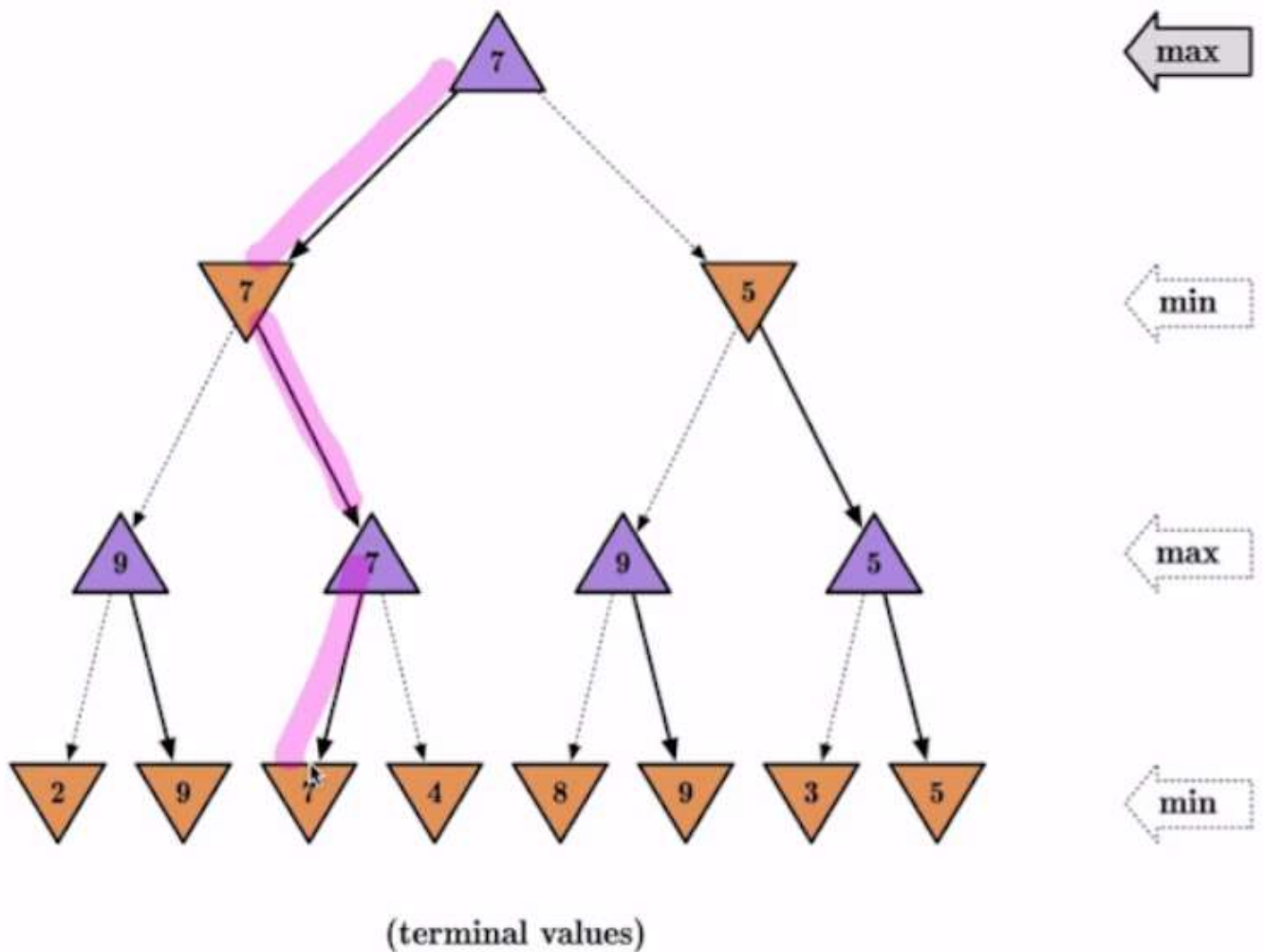


計算機程式設計 (二) MiniProject3

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Tree Search - Minimax



Tree Search Optimization - AlphaBeta pruning

我們知道root Max要做決定的話，要取 $\max(3, Z, 2)$ 但是由於 $Z = \min(2, X, Y) \leq 2 < 3$ ，所以我們不care Z多少了，因為對我們要取max來說沒貢獻了。所以不必explore X Y就可以知道 root Max要取 $\max(3, \text{DONT_CARE}, 2) = 3$ 這樣馬上就省略了一個subtree需要去explore!

alpha-beta pruning仍然是一個minimax演算法 (DFS)，但是添加了pruning的機制。我們需要多兩個輔助變數：

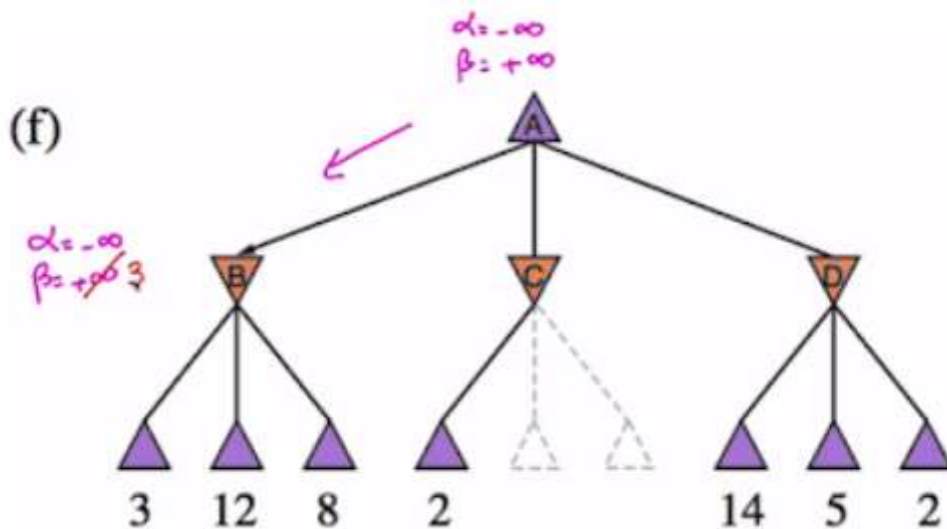
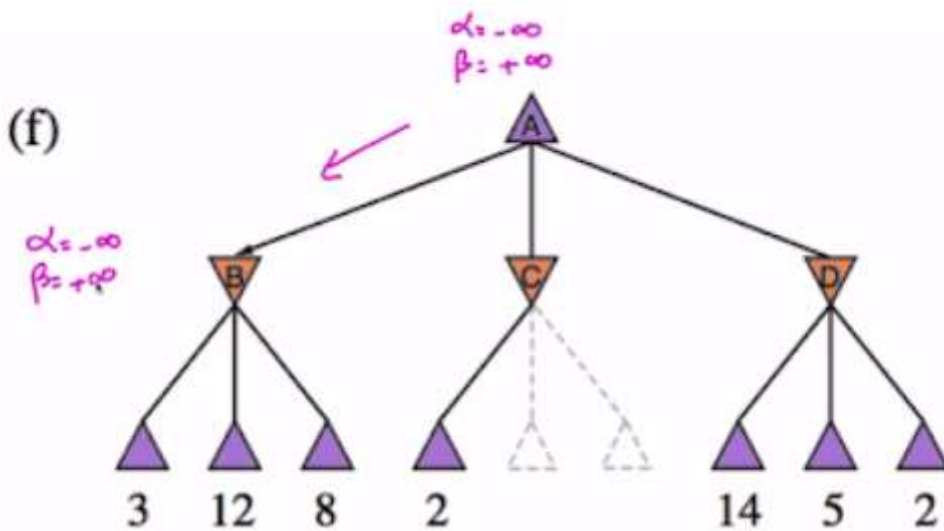
- alpha - 目前Max可做的move的最大utility score，所以初始化要是 $-\text{INF}$ ，只能被Max node update
- beta - 目前Min可做的move的最小utility score，所以初始化要是 $+\text{INF}$ ，只能被Min node update

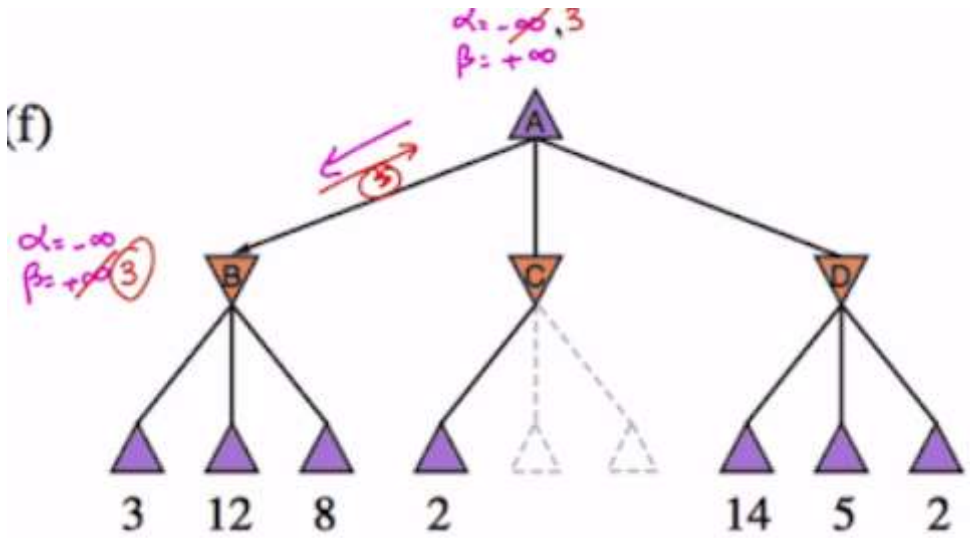
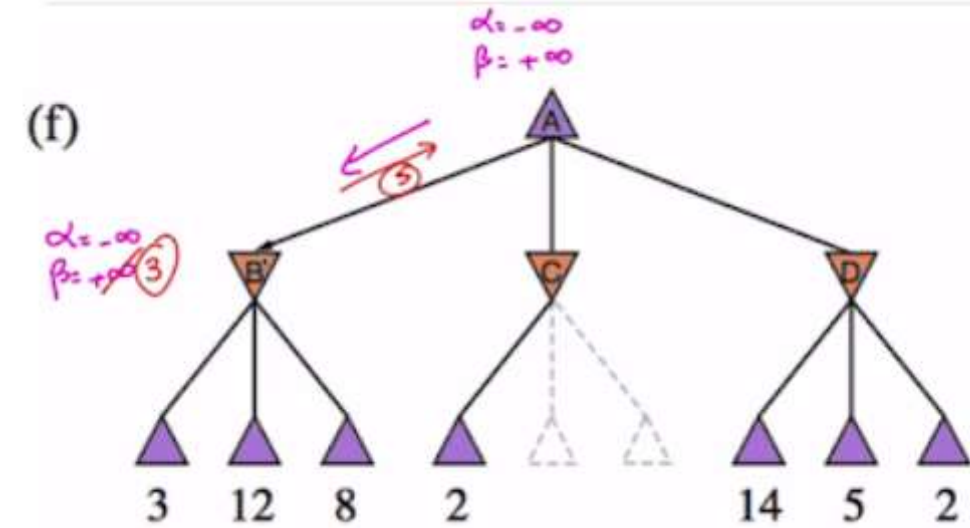
- 當 $\alpha \geq \beta$ 的時候，代表 pruning 發生

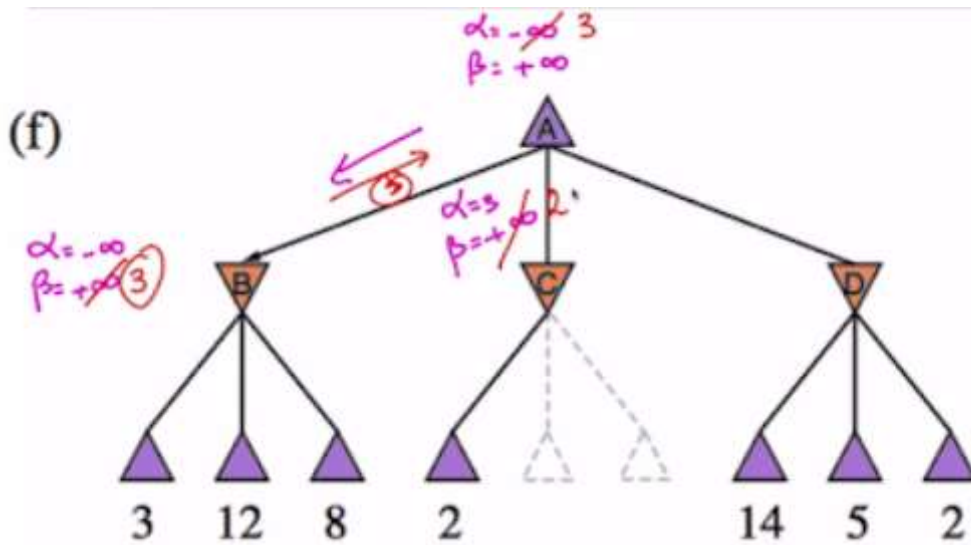
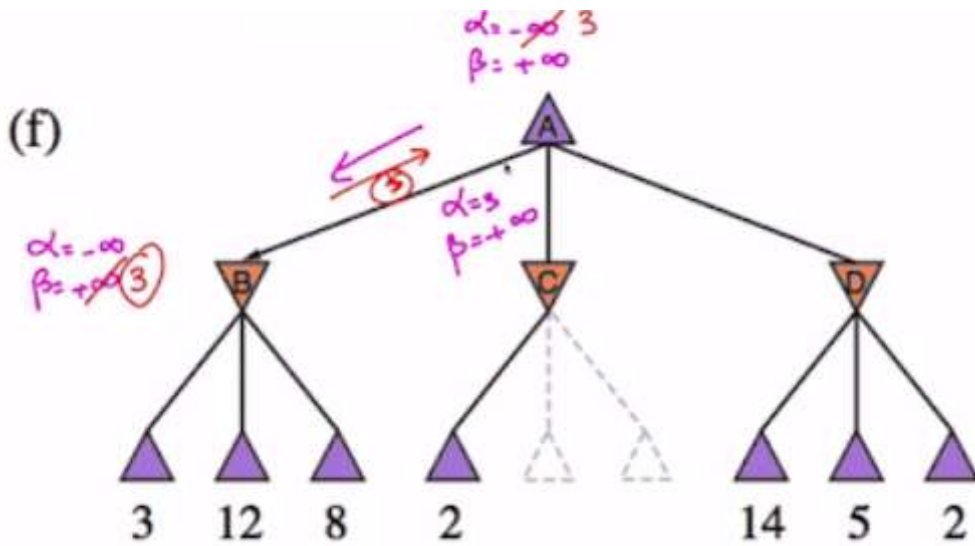
對一個 min node 來說，它看到目前的 parent max node 的 α/β 值，而這個 min node 只能藉由其 children 的 utility score 來 update β 值。如果它發現 $\alpha \geq \beta$ ，由於此 min node 能回傳的 utility score 最大也只能是目前的 β ，意即此 min node 再也無法提供其 parent max node 大於目前 α 值的 utility score，所以剩下的所 unexplored 的 children 都可以 prune 掉不看了。

同理，對一個 max node 來說，它看到目前的 parent min node 的 α/β 值，而這個 max node 只能藉由其 children 的 utility score 來 update α 值。如果它發現 $\beta \leq \alpha$ ，由於此 max node 能回傳的 utility score 最小也只能是目前的 α ，意即此 max node 再也無法提供其 parent min node 小於目前 β 值的 utility score，所以剩下的所 unexplored 的 children 都可以 prune 掉不看了。

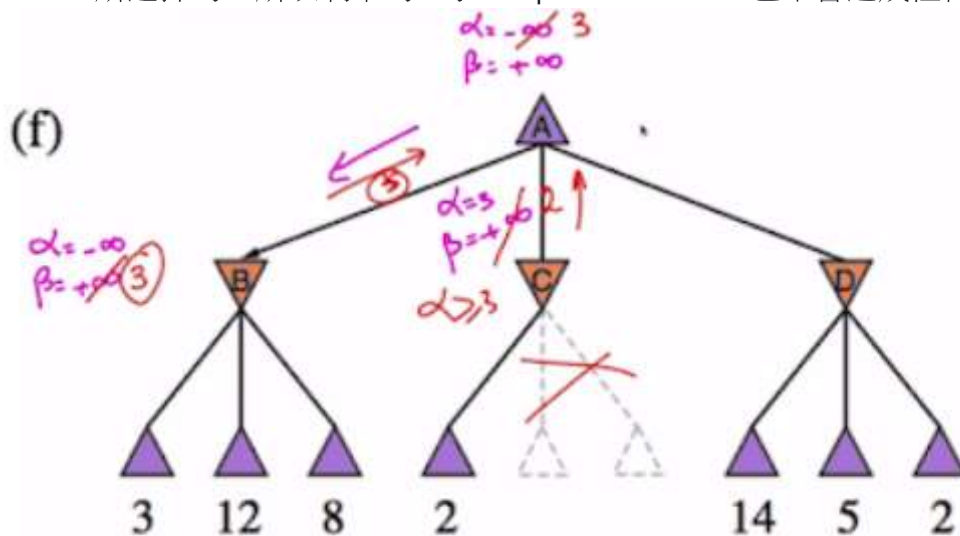
流程



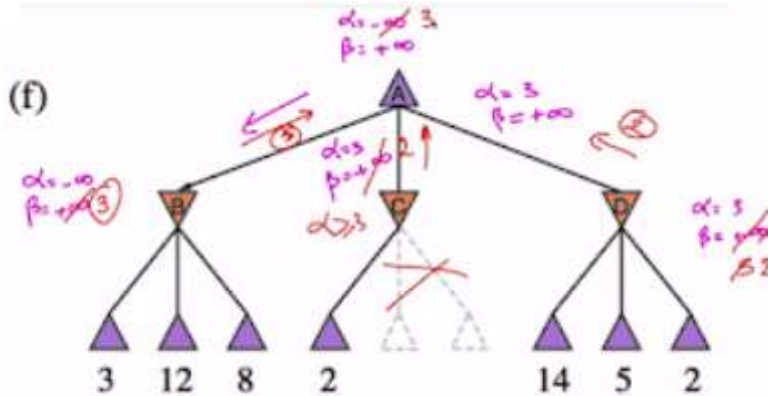
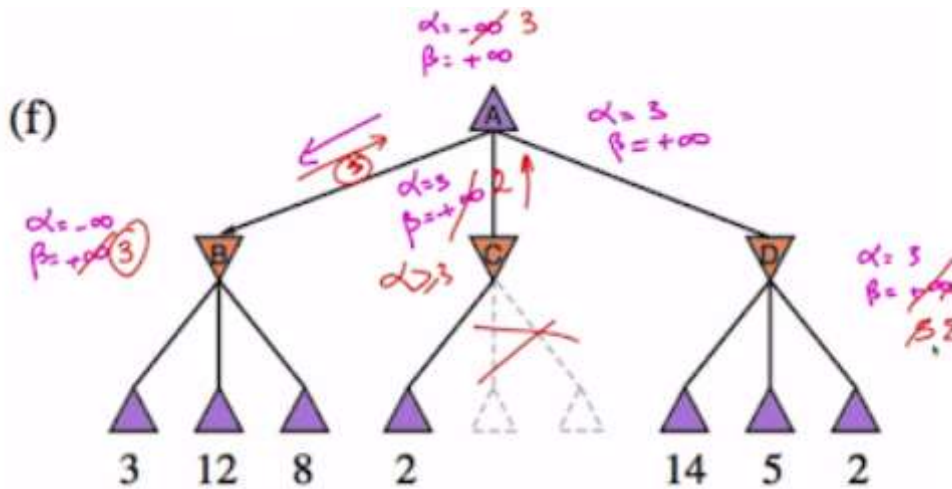
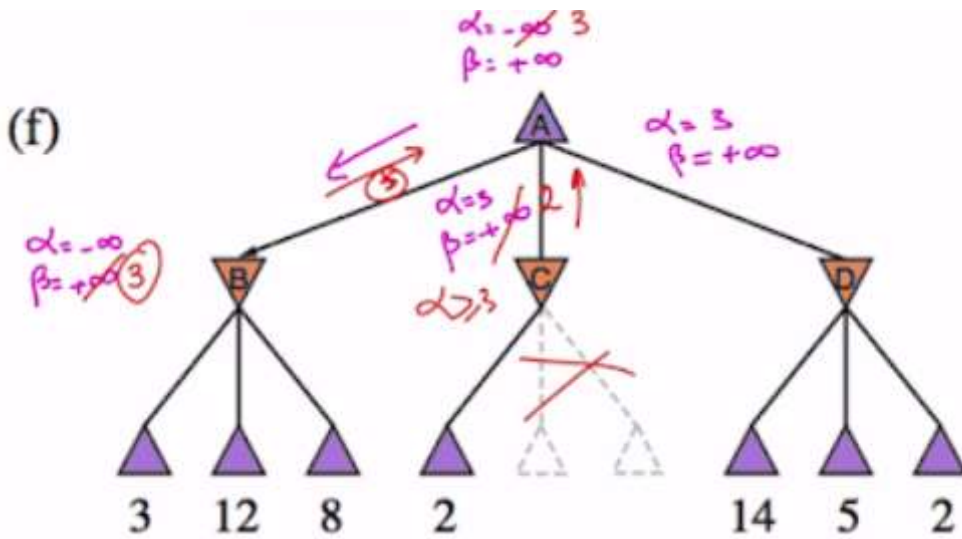




<下圖發生Pruning> 因為 min node C 發現了目前($\alpha = 3$) \geq ($\beta = 2$)，這表示Min node C最大的utility score只能是2（因為C只能從children中選擇 ≤ 2 的utility score），而對root Max A來說，既然child C最大只能回傳utility = 2，但是目前已經有找到一個utility score = 3 = α 了，那C這個node是不會被 root Max A所選擇的，所以剩下的C的unexplored children也不會造成任何影響了，可以放心的



prune掉。



```
int minimax(Point p, array<array<int, SIZE>, SIZE> board,
            int player, int depth, bool isMaximizingPlayer, int alpha, int beta)
{
    if (depth == 3){
        int h = set_heuristic(board, player);
        return h;
    }
    if (isMaximizingPlayer){
        int bestValue = NEG_INF;
        vector<Point> valid_spots = get_valid_spots(board, player);
        for(Point c : valid_spots){
            array<array<int, SIZE>, SIZE> newBoard = copyBoard(board);
            put_disc(c, newBoard, player);
```

```

        int value = minimax(p, newBoard, player, depth+1, false, alpha, beta);
        bestValue = max(bestValue, value);
        alpha = max(alpha, bestValue);
        if (beta <= alpha)
            break;
    }
    return bestValue;
}
else{
    int bestValue = POS_INF;
    vector<Point> valid_spots = get_valid_spots(board, player);
    for(Point c : valid_spots){
        array<array<int, SIZE>, SIZE> newBoard = copyBoard(board);
        put_disc(c, newBoard, player);

        int value = minimax(p, newBoard, player, depth+1, true, alpha, beta);
        bestValue = min(bestValue, value);
        beta = min(beta, bestValue);
        if (beta <= alpha)
            break;
    }
    return bestValue;
}
}
}

```

Heuristic function

1. 計算落子分數以及frontier分數

p = 計算地圖位置分數比後，在跟據落子點計算分數權重 f = 計算每一個空的位置，那個空位置旁邊的棋子是誰的，希望不要是自己的，因為這樣容易被別人吃掉，把空位置旁邊的棋子稱為 frontier_disc，所以評分函數， $f = (-1) * (\text{my_front_discs} - \text{opp_front_discs})$

```

int X1[] = {-1, -1, 0, 1, 1, 1, 0, -1};
int Y1[] = {0, 1, 1, 1, 0, -1, -1, -1};
int V[8][8] = {
    {2000, -300, 11, 8, 8, 11, -300, 2000},
    {-300, -700, -4, 1, 1, -4, -700, -300},
    {11, -4, 2, 2, 2, 2, -4, 11},
    {8, 1, 2, -3, -3, 2, 1, 8},
    {8, 1, 2, -3, -3, 2, 1, 8},
    {11, -4, 2, 2, 2, 2, -4, 11},
    {-300, -700, -4, 1, 1, -4, -700, -300},
    {2000, -300, 11, 8, 8, 11, -300, 2000}
};

// Piece difference, frontier disks and disk squares
for (int i=0; i<8; i++){
    for (int j=0; j<8; j++){
        if (board[i][j] == player){
            d += V[i][j];
        }
    }
}

```



```

        my_discs++;
    }else if (board[i][j] == get_next_player(player)){
        d -= V[i][j];
        opp_discs++;
    }
    if (board[i][j] != 0){
        for (int k=0; k<8; k++){
            int x = i + X1[k];
            int y = j + Y1[k];
            if (x >= 0 && x < 8 && y >= 0 && y < 8 && board[x][y] == 0){
                if (board[i][j] == player) my_front_discs++;
                else opp_front_discs++;
                break;
            }
        }
    }
}
}
}
p = my_discs - opp_discs;
f = my_front_discs - opp_front_discs;

```

2. 四個角落的佔據

佔據四個角落很重要，所以 c 的權重很大

```

my_discs = opp_discs = 0;
if (board[0][0] == player) my_discs++;
else if (board[0][0] == get_next_player(player)) opp_discs++;
if (board[0][7] == player) my_discs++;
else if (board[0][7] == get_next_player(player)) opp_discs++;
if (board[7][0] == player) my_discs++;
else if (board[7][0] == get_next_player(player)) opp_discs++;
if (board[7][7] == player) my_discs++;
else if (board[7][7] == get_next_player(player)) opp_discs++;
c = 25*(my_discs - opp_discs);

```

3. 靠近四個角落，共12個點盡量不要下

```

my_discs = opp_discs = 0;
if (board[0][0] == 0){
    if (board[0][1] == player) my_discs++;
    else if (board[0][1] == get_next_player(player)) opp_discs++;
    if (board[1][1] == player) my_discs++;
    else if (board[1][1] == get_next_player(player)) opp_discs++;
    if (board[1][0] == player) my_discs++;
    else if (board[1][0] == get_next_player(player)) opp_discs++;
}
if (board[0][7] == 0){
    if (board[0][6] == player) my_discs++;
    else if (board[0][6] == get_next_player(player)) opp_discs++;
}

```

```

    if (board[1][6] == player) my_discs++;
    else if (board[1][6] == get_next_player(player)) opp_discs++;
    if (board[1][7] == player) my_discs++;
    else if (board[1][7] == get_next_player(player)) opp_discs++;
}
if (board[7][0] == 0){
    if (board[7][1] == player) my_discs++;
    else if (board[7][1] == get_next_player(player)) opp_discs++;
    if (board[6][1] == player) my_discs++;
    else if (board[6][1] == get_next_player(player)) opp_discs++;
    if (board[6][0] == player) my_discs++;
    else if (board[6][0] == get_next_player(player)) opp_discs++;
}
if (board[7][7] == 0){
    if (board[6][7] == player) my_discs++;
    else if (board[6][7] == get_next_player(player)) opp_discs++;
    if (board[6][6] == player) my_discs++;
    else if (board[6][6] == get_next_player(player)) opp_discs++;
    if (board[7][6] == player) my_discs++;
    else if (board[7][6] == get_next_player(player)) opp_discs++;
}
l = (-13) * (my_discs - opp_discs);

```

4. 限制對方可以下的步數，自己可以下越多步越好，對方能下的步數越少越好

```

vector<Point> my_discs_vec = get_valid_spots(board, player);
vector<Point> opp_discs_vec = get_valid_spots(board, get_next_player(player));
m = my_discs_vec.size() - opp_discs_vec.size();

```

5. Total heuristic score

```

score = (10 * p) + (2000 * c) + (500 * l) + (60 * m) + (50 * f) + (10 * d);

```

Reference

1. <https://fu-sheng-wang.blogspot.com/2017/02/ai-16-alpha-beta-pruning.html>
2. <https://fu-sheng-wang.blogspot.com/2017/02/ai-15-minimax.html>
3. <https://kartikkukreja.wordpress.com/2013/03/30/heuristic-function-for-reversi-othello/>