

Machine Learning 2021 Homework 3 電機4C 洪愷尹 0710851

1 Support Vector Machine (SVM)

- ▼ [1] Use the principal component analysis (PCA) to reduce the dimension of images to $d = 2$

```
✓ 0 秒
▶ class PCA_2D:
    def __init__(self, dim, x_train):
        pca_2d = PCA(n_components=dim)
        self.transformed_data = pca_2d.fit_transform(x_train)
        self.normalization = (self.loading...ed_data - np.mean(self.transformed_data)) / np.std(self.transformed_data)
        self.components_ = pca_2d.components_

    def get_transformed_data(self):
        return self.transformed_data
    def get_transformed_data_with_normalization(self):
        return self.normalization
    def get_components(self):
        return self.components_
```

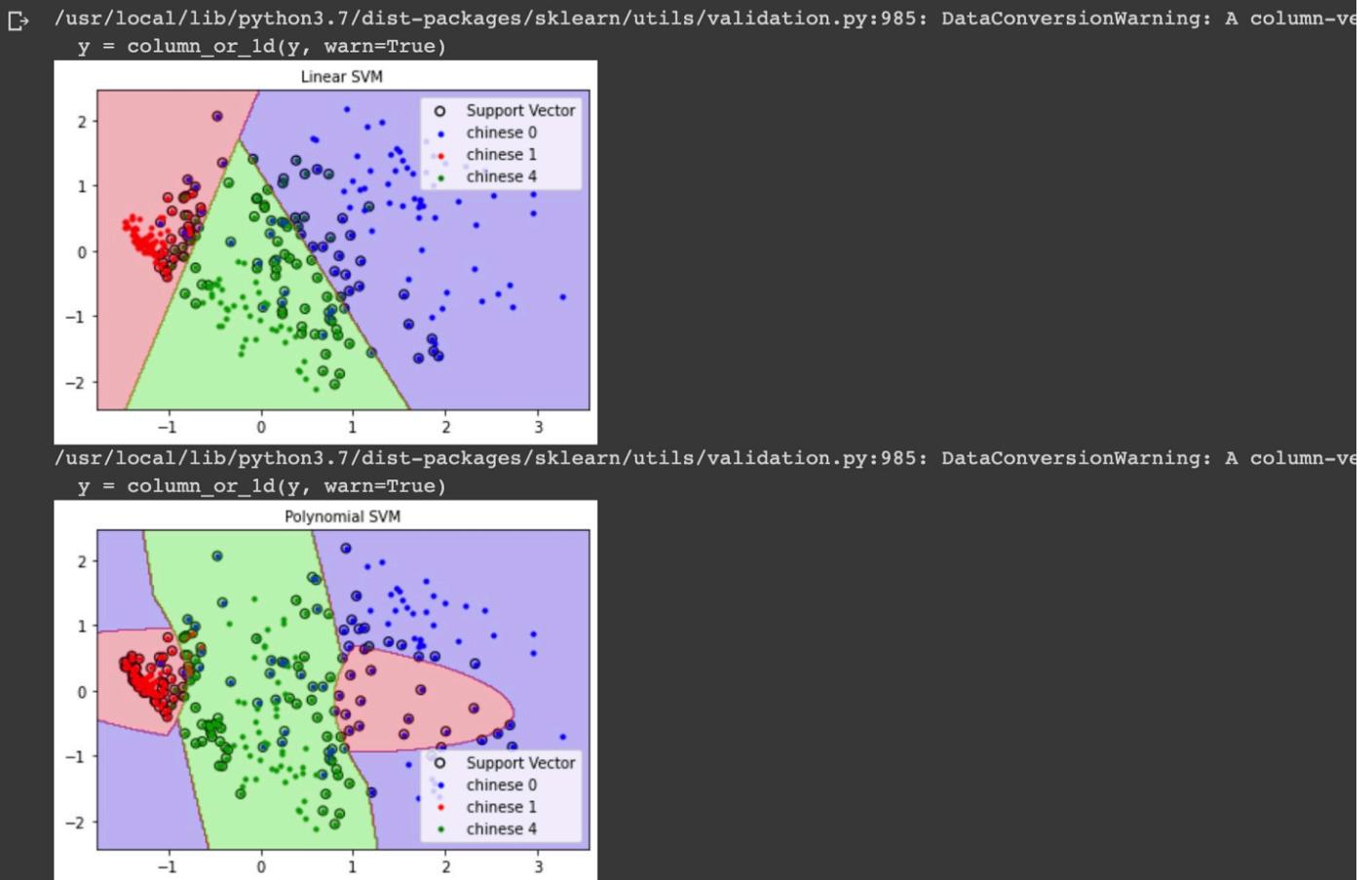
```
✓ 0 秒
[47] pca_2d = PCA_2D(2, x_train)
     x_data = pca_2d.get_transformed_data_with_normalization()
     t_data = t_train
```

- [2] Analyze the difference between two decision approaches (one-versus-the-rest and one- versus-one). Decide which one you want to choose and explain why you choose this approach.

Answer

1. **One-versus-the-rest** 跟 **One-versus-one** 都是二元分類器應用在多類別問題上的策略。
2. **One-versus-the-rest**: 選取一類當作+1類，其餘當作-1類，利用二元分類器得到一個decision hyperplane，然後輪流將每一類別都當過+1類。比如：本題有三類，所以在train階段會得到3個分類器，在test階段時，選取三個分類器中分數最高的那一類當作決策。
3. **One-versus-one**: 一次只做兩個類別的分類，兩兩pk，直到兩兩都配對分類完成。train階段會得到3個分類器，在test階段時，選取得到最多票數的那類當作判斷決策。
4. 本次使用One-versus-one的策略，因為SVM在這個策略下比較不會犧牲掉樣本數比較少的類別。

- [3-4] Use the principle values projected to top two eigenvectors obtained from PCA, and build a SVM with linear kernel to do multi-class classification. Then, plot the corresponding decision boundary and show the support vector.



- ▼ [5] Please discuss the difference between (3) (4).

Discussion

1. 由Linear SVM 跟 Polynomial SVM 結果來觀察，可以發現線性的Kernel對於這次的挑選的3個中文字分類表現比較好。
2. Polynomial Kernel 跟 Linear Kernel 投影的維度分別是(3, 2)，由結果論這次的分類器利用比較低的維度，也就是2維來分類效果較佳！

2 Gaussian Mixture Model (GMM)

▼ [1] Please build a K-means model by minimizing J loss.

```
✓ 0 秒
  class K_Means:
      def __init__(self, data, K=3, iteration=100) -> None:
          self.K = K
          self.iteration = iteration
          self.eye = np.eye(K)
          #initialize means and rnk
          self.means = data[np.random.choice(len(data), self.K, replace=False)] # without replacement
          self.rnk = np.ones([len(data), self.K]) #(252150,3)

      def minimize_J_loss(self, data):
          for iter in range(self.iteration):
              error = np.sum((data[:, None] - self.means)**2, axis=2)
              rnk = self.eye[np.argmin(error, axis=1)]

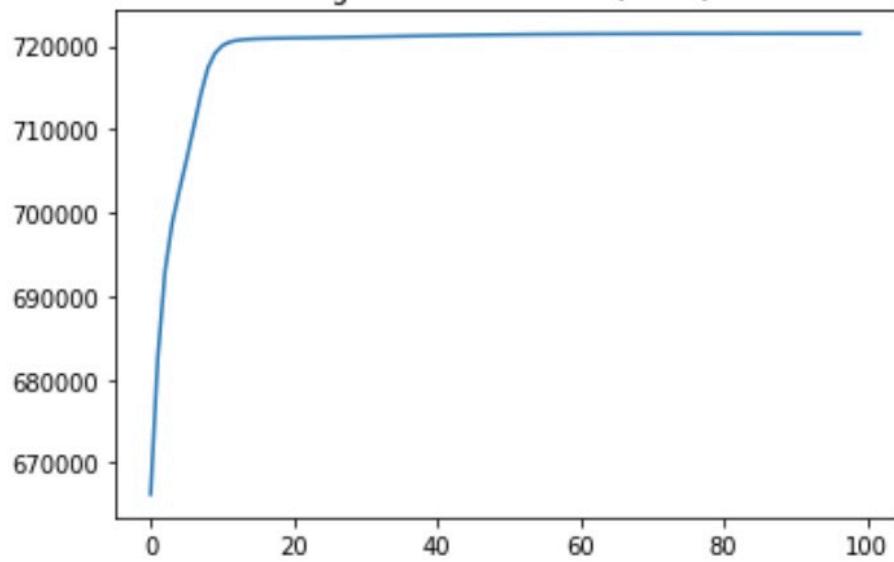
              if np.array_equal(rnk, self.rnk):
                  break
              else:
                  self.rnk = rnk

          #re-calculate k means
          self.means = np.sum(rnk[:, :, None] * data[:, None], axis=0) / np.sum(rnk, axis=0)[:, None]
```

Original



Log likelihood of GMM (k = 3)





GMM K = 3



K_means K = 3

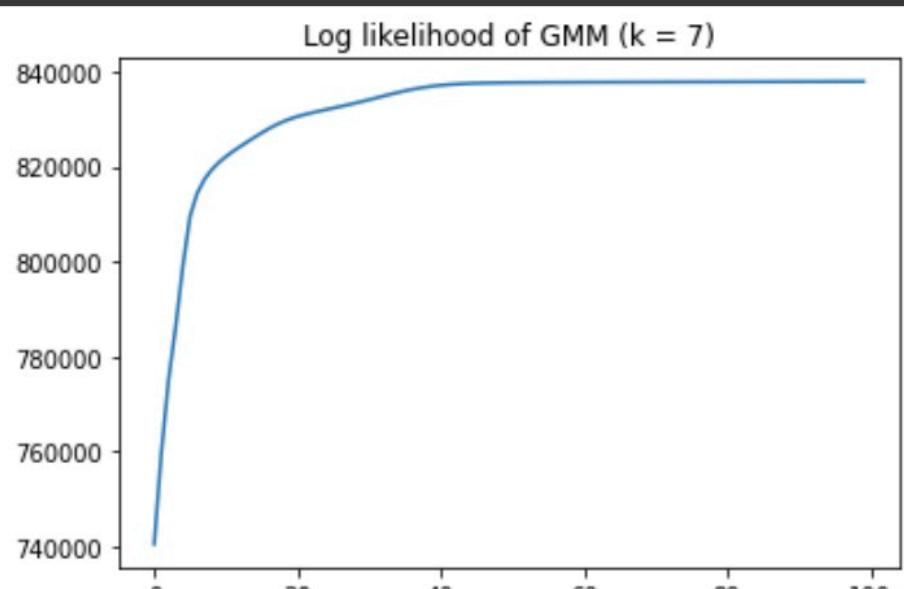
	R	G	B
0	177	186	189
1	35	31	18
2	106	118	77

GMM K = 3

	R	G	B
0	175	188	198
1	20	16	12
2	101	109	73



...



K_means K = 7

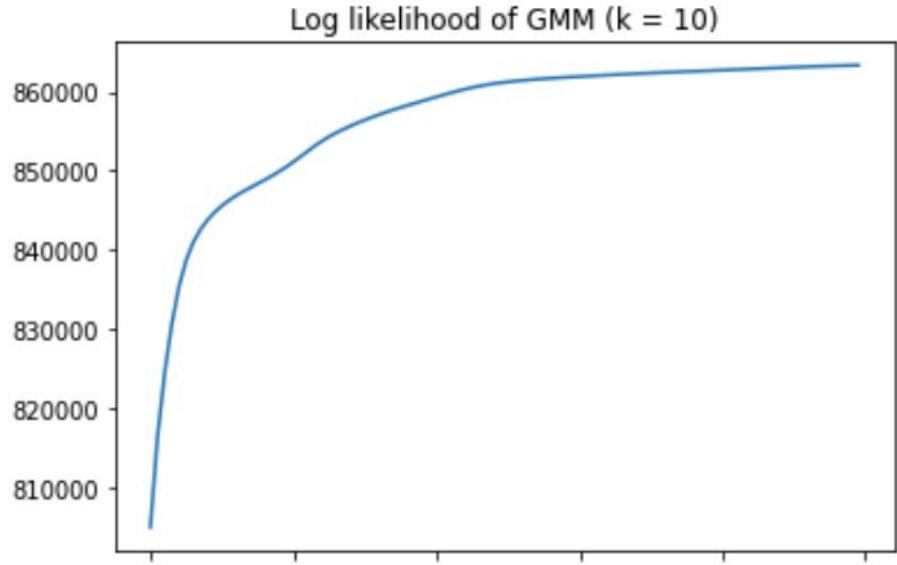


GMM K = 7



```
K_means K = 7
      R      G      B
0   112    124    81
1   163    174   177
2    82     99    51
3   208    217   227
4    18     14     9
5   138    145   122
6    60     52    31
```

```
GMM K = 7
      R      G      B
0   100    126    73
1   151    156   157
2    74     77    54
3   194    207   221
4    16     13     9
5   160    144   119
6    83     43    28
```



K_means K = 10



GMM K = 10

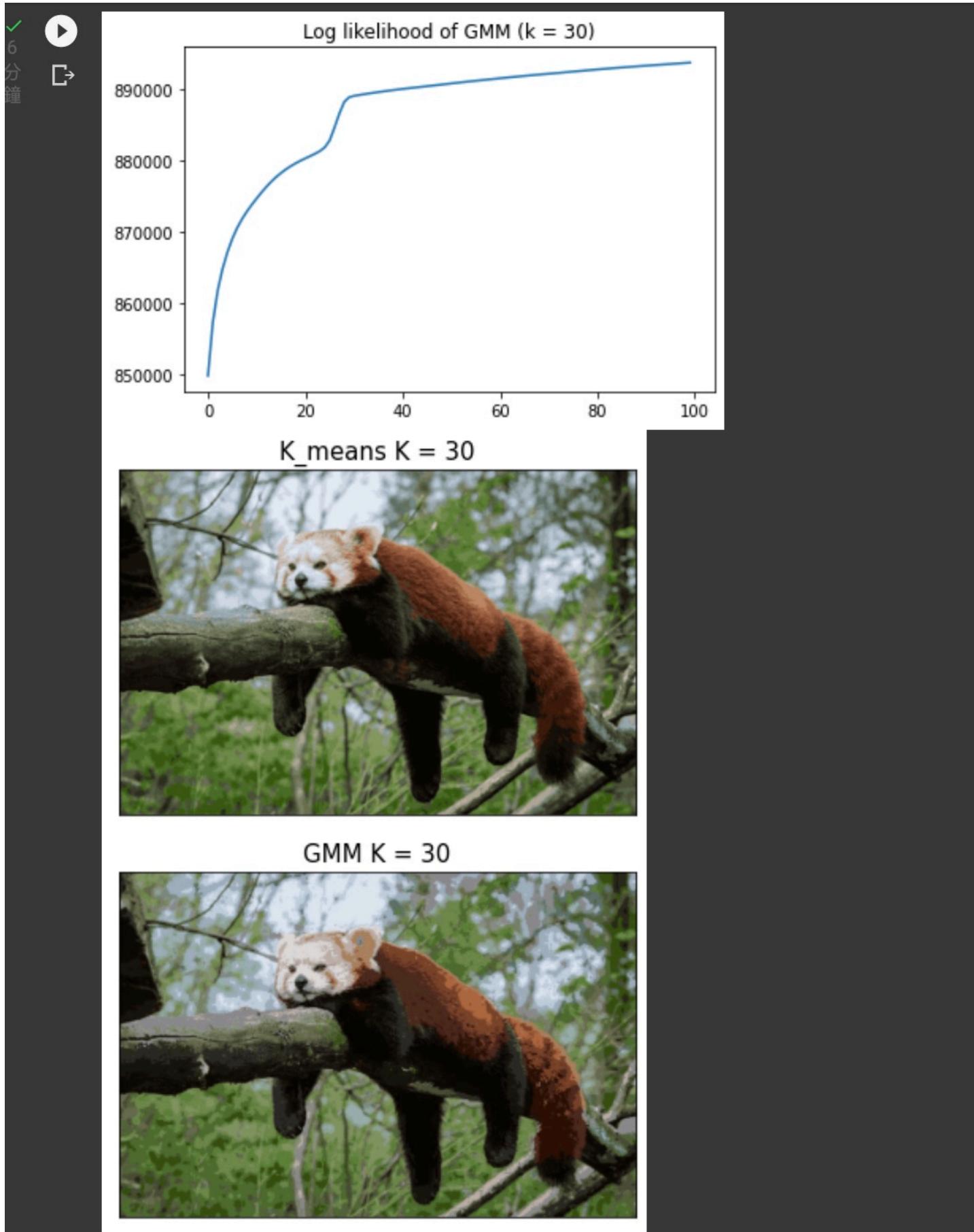


K_means K = 10

	R	G	B
0	212	220	230
1	72	93	44
2	97	117	69
3	144	155	146
4	50	44	28
5	110	60	40
6	172	183	189
7	123	136	101
8	173	115	81
9	17	12	8

GMM K = 10

	R	G	B
0	207	219	232
1	74	76	55
2	90	120	58
3	158	175	185
4	24	19	14
5	82	43	27
6	155	149	146
7	123	140	113
8	175	123	88
9	7	5	4



分鐘	R	G	B
0	106	112	81
1	22	16	10
2	228	235	244
3	88	97	71
4	176	166	150
5	92	47	30
6	99	114	105
7	124	128	103
8	161	100	69
9	209	217	228
10	46	48	32
11	124	70	46
12	62	62	48
13	75	82	56
14	153	169	175
15	144	151	126
16	186	201	214
17	32	29	22
18	188	136	99
19	94	127	55
20	8	6	4
21	133	153	95
22	208	194	184
23	168	184	194
24	112	139	75
25	120	136	131
26	57	91	18
27	139	154	155
28	76	109	40
29	61	28	12

GMM K = 30			
	R	G	B
0	105	106	79
1	14	10	5
2	219	229	240
3	85	99	61
4	139	139	140
5	78	42	32
6	95	114	107
7	120	127	101
8	173	105	65
9	219	216	216
10	43	42	29
11	122	67	43
12	45	43	40
13	74	78	53
14	154	175	173
15	139	147	127
16	192	206	220
17	25	20	15
18	170	129	94
19	92	128	57
20	6	5	4
21	129	149	97
22	189	175	167
23	158	175	188
24	110	137	75
25	123	139	130
26	54	80	17
27	142	164	151
28	78	109	47
29	44	18	7

- [4] Make some discussion about what is crucial factor to affect the output image between K-means and Gaussian mixture model (GMM), and explain the reason.

Discussion

1. K Means 跟 GMM 都是cluster model.

2. 最大的差別是，GMM是有covariance的考量在裡面，其中decision boundary是橢圓形的; K Means的boundary則是圓形的。

3. 從上述(2)跟結果來看，可以發現GMM的結果在將浣熊與背景分離上效果比較好，但是在細節毛紋上K means的結果比較好，這跟GMM是soft cluster 利用高斯分佈有關。