

# Josephus - Factorial

① a)  $4! = 4 \cdot 3 \cdot 2 \cdot 1 = \boxed{24}$

b)  $5! - 6!$

$5! - 6 \cdot 5!$

$5!(1 - 6)$

$120 \cdot (-5) = \boxed{-600}$

c)  $9! = 362.880 = \boxed{504}$

$6! \cdot 720$

$6! = 720$

$9! = 9 \cdot 8 \cdot 7 \cdot 6!$

$9! = 504 \cdot 720 = 362.880$

d)  $\frac{98!}{100!} = \frac{1}{9 \cdot 900}$

$100! = 100 \cdot 99! = 9.900$

②  $\frac{1}{m!} - \frac{m}{(m+1)!}$

③  $\frac{(m!)^2 - (m-1)! \cdot m!}{(m-1)! \cdot m!} = m-1 \text{ (A)}$

④  $\frac{(m+2)! \cdot (m-2)!}{(m+1)! \cdot (m-1)!} = 4 \text{ (A)}$

⑤  $\frac{(m+1)! - m!}{(m+1)!} = \frac{7}{m+1}$   $\frac{(n+1)! \cdot m \cdot (n-1)! - m(m+1)!}{(m+1)!} = \frac{7}{m+1}$

$\frac{(m+1)! [(n-1) \cdot n - n]}{(m+1)!} = \frac{7}{m+1}$   $\frac{n^2 - n + n}{1} = \frac{7}{m+1}$   $n^2 = 7$   $m=0$

⑥  $(m-1)! [(n+1)! - m!] = (m!)^2 \text{ (D)}$

⑦  $\frac{m! + (m-1)!}{(m+1)! - m!} = \frac{6}{25}$   $m=5 \text{ (C)}$

⑧  $21! - 221 \text{ (D)}$