Neural Networks – Part II

PHYS 250 (Autumn 2018) – Lecture 16

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Outline

1. *Reminders*
   - Reminders from Lecture 15
2. *Historical perspective*
   - Brief History of Machine Learning Generally
   - Brief History of Neural Networks
3. *Structure of Neural Networks*
   - Single layer perceptron
   - Training a single layer perceptron
   - Training a Multi-Layer Perceptron (MLP)

Reminders from last time

We embarked on a whirlwind introduction to neural networks.

Neural networks and machine learning

- **Context and perspective**
  - We discussed the general issue of training computers to **discover, identify, and analyze patterns** of interest in datasets
  - Categorized tasks that make use of this idea: **classification, regression, generation, clustering, anomaly detection**
- **Neural networks as a tool**
  - Introduced both the **modeling** perspective as well as the **biological** perspective on what a neural network achieves
  - Described the **structure and function** of a neuron
  - Began discussing the **mathematical properties** of a neural network

Today we will build our own networks! But first, I just wanted to follow-up on some points and questions from last time.

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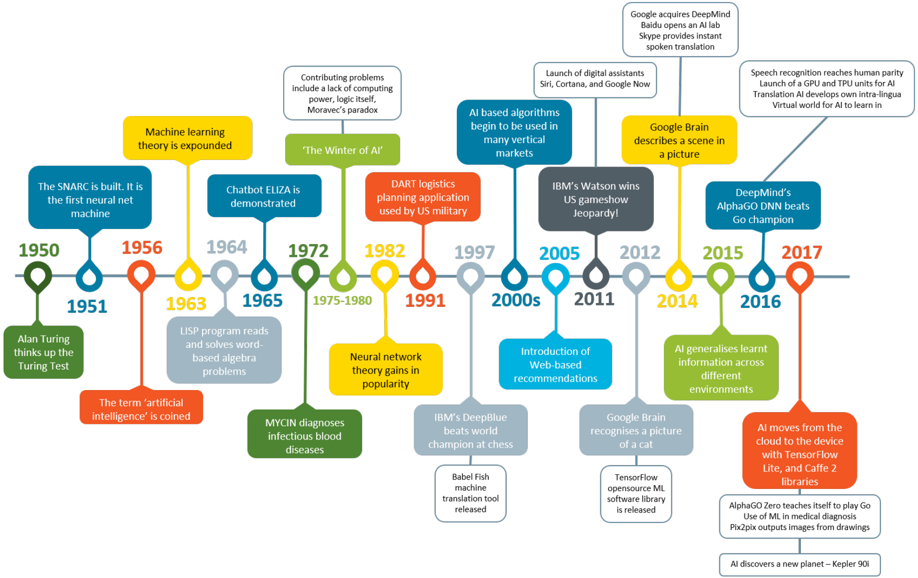
Brief history of machine learning

Taken from Harry Ide on InnovationLaboratory.com (18 May 2018):



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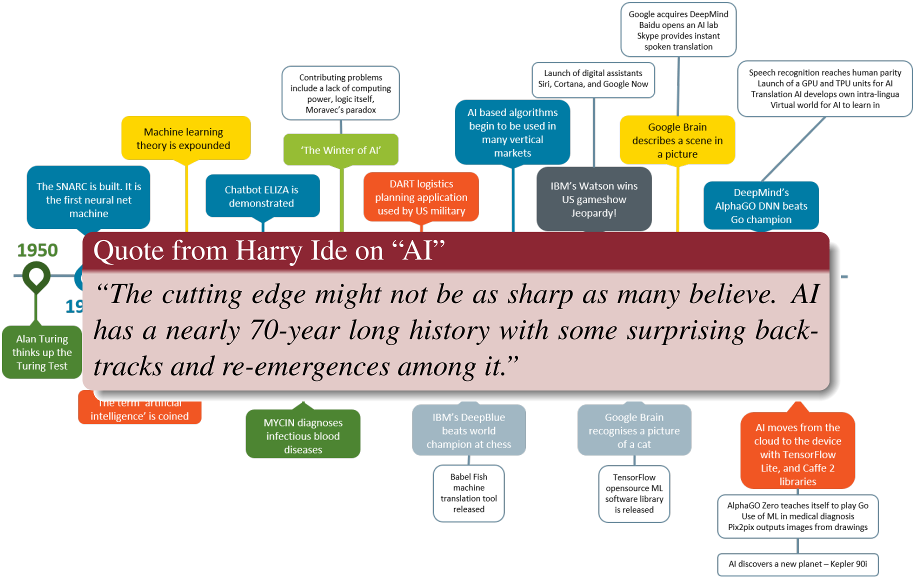
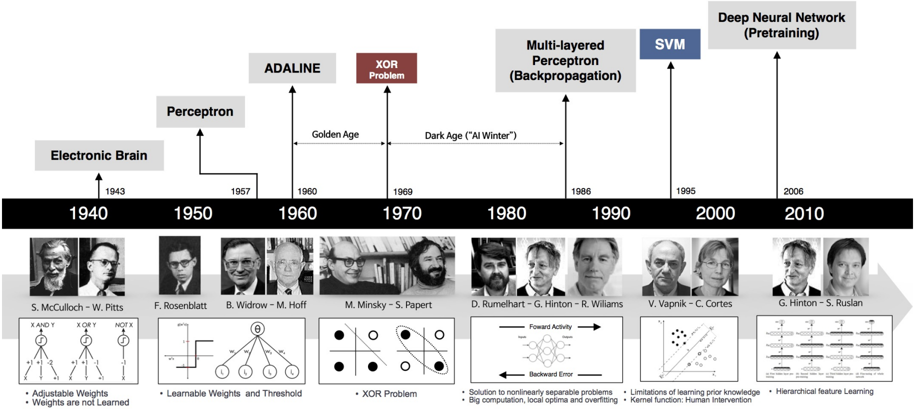


Quote from Harry Ide on "AI"

"The cutting edge might not be as sharp as many believe. AI has a nearly 70-year long history with some surprising back-tracks and re-emergences among it."

Brief history of neural networks

Taken from this talk on SlideShare:



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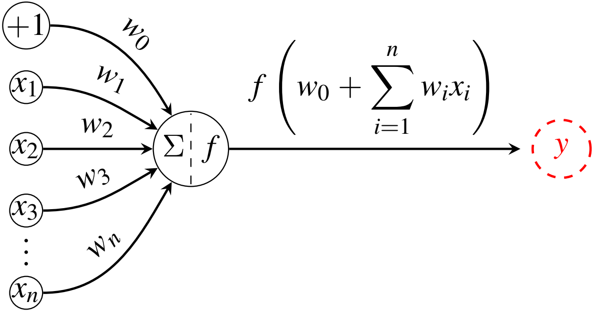
Single layer perceptron

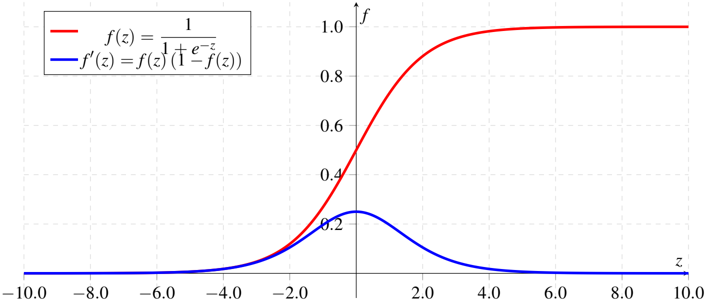


- $\vec{x} = (x_1, x_2, \cdots, x_n)$ **is an input feature vector of length** n

  i.e. the attributes of the data, e.g. voltages
- $\vec{w} = (w_1, w_2, \cdots, w_n)$ **is the weight vector with** w_0 **reserved as a bias**
  - becomes a matrix for multiple layers
- Σ **indicates summation (or matrix mult.):** $z = \sum w_i x_i$ $(x_0 = 1)$
- f **is the activation function, or non-linearity:** $f(z)$
- $y = f(z)$ **is the output**

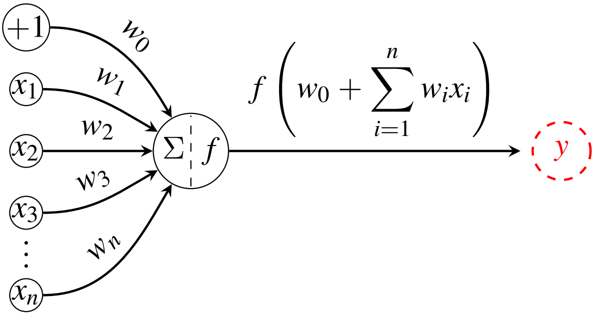
Sigmoid as activation function

As we discussed, a typical function for a **single layer perceptron** is the **sigmoid**.



Here, we plot both the function itself, as well as its derivative, since that will be important when evaluating the **backpropagation** of weights in order to update the neural network.

Training a single layer perceptron

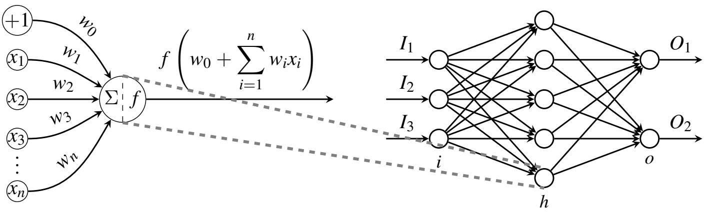


Given j objects $\vec{x}_j$ in dataset, each with **known values of f**, d_j

- **Calculate the output:** $y_j = f(\vec{w} \cdot \vec{x}_j)$
- **Determine the error:** $\epsilon_j = d_j - y_j$
- **Update the weights:** $w_i^{\text{new}} = w_i + r(\epsilon_j \cdot \vec{x}_j)_i$

Choosing the learning rate r is where the derivative is used. It's not important for the single-layer perceptron, but is **essential** for a network.

Multi-layer perceptron (MLP)



Given j objects $\vec{I}_j$ in dataset, each with features $\vec{I} = (I_1, I_2, \cdots, I_n)$ and **known outputs $\vec{d}_j$ at each output node o**, $\vec{d} = (d_1, d_2, \cdots, d_o)$

- **Calculate the h outputs of hidden layer:** $v_h = f(\sum_i w_{ih} I_i)$
- **Calculate the o outputs of output layer:** $y_o = f(\sum_h w_{ho} v_h)$
- **Determine the error at output each node o:** $\epsilon_o = d_o - y_o$
- **Determine the total error for data object j:** $\mathcal{E}_j = \frac{1}{2} \sum_o \epsilon_o^2$
- **Determine change in weights for output neuron y_o:** $\Delta w_{oh} = -\eta \frac{\partial \mathcal{E}}{\partial z_o} v_h = \eta \epsilon_o f'(z_o)$

LeCun, Bengio, Hinton, “Deep learning”

Nature volume 521, pages 436-444 (28 May 2015)