

3D Game Programming Geometric Transformations

Ming-Te Chi
Department of Computer Science,
National Chengchi University

Outline



Geometric Transformations



Basic transformation

- The coordinates
- Hierarchy transformation



Modeling

- Mesh format / import
- Unity ProBuilder

Transformation Terminology

- Viewing
- Modeling
- Modelview
- Projection
- Viewport



Transformations



Translation

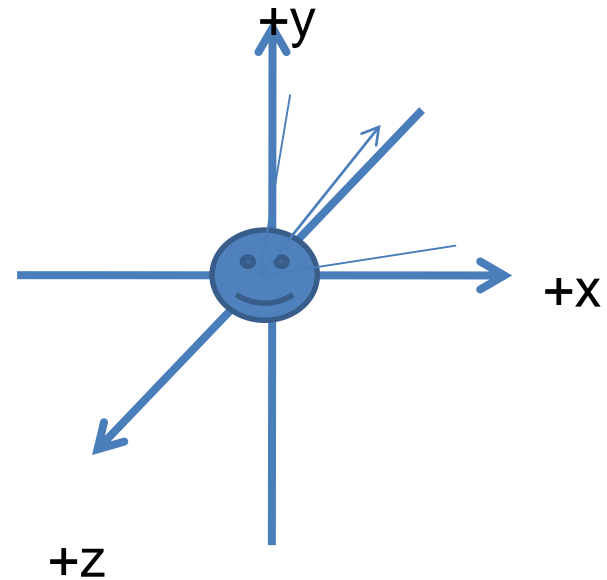
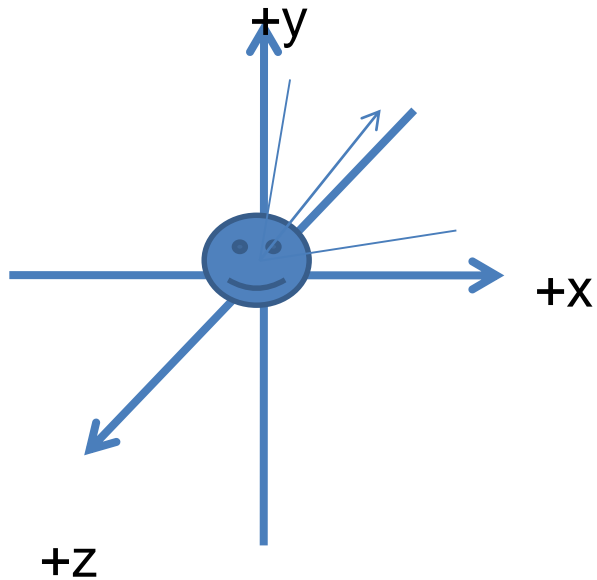


Rotation

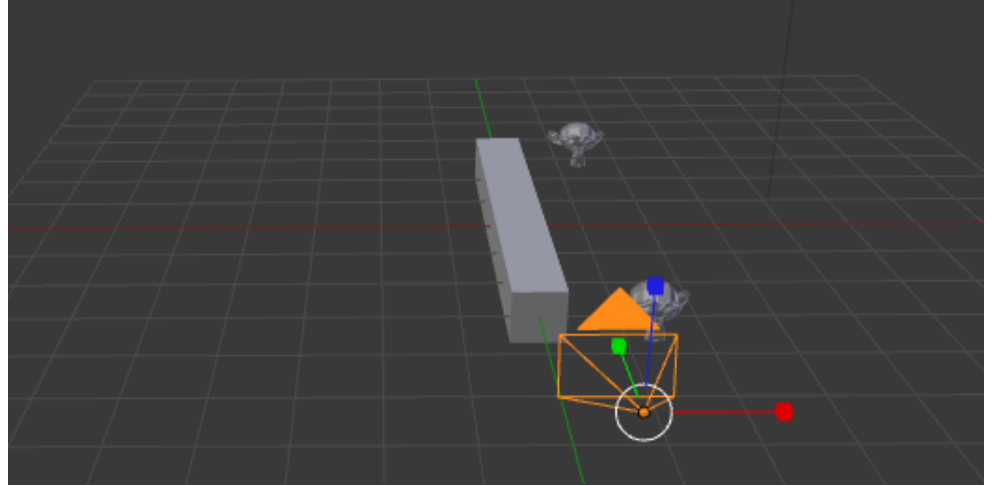


Scaling

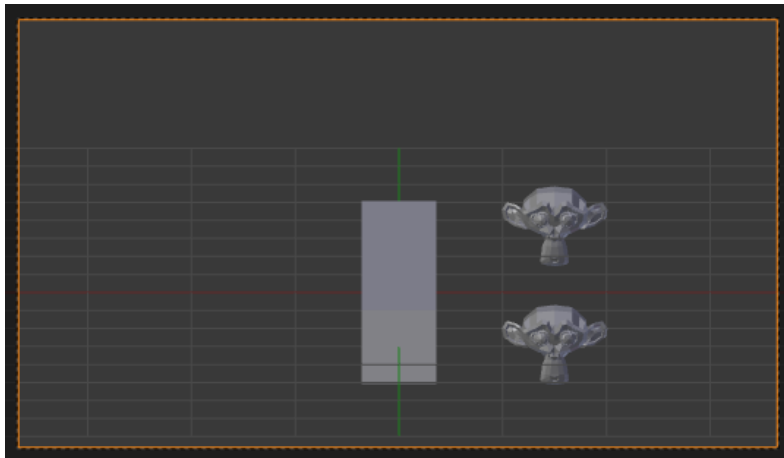
The Modelview Duality



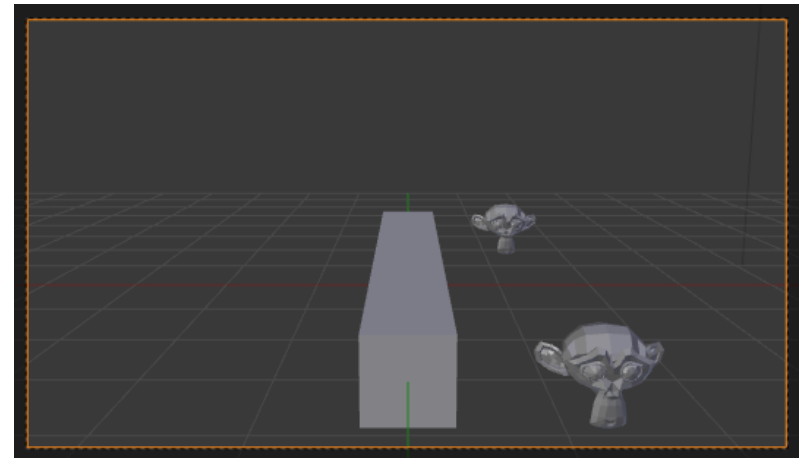
Projection



World space



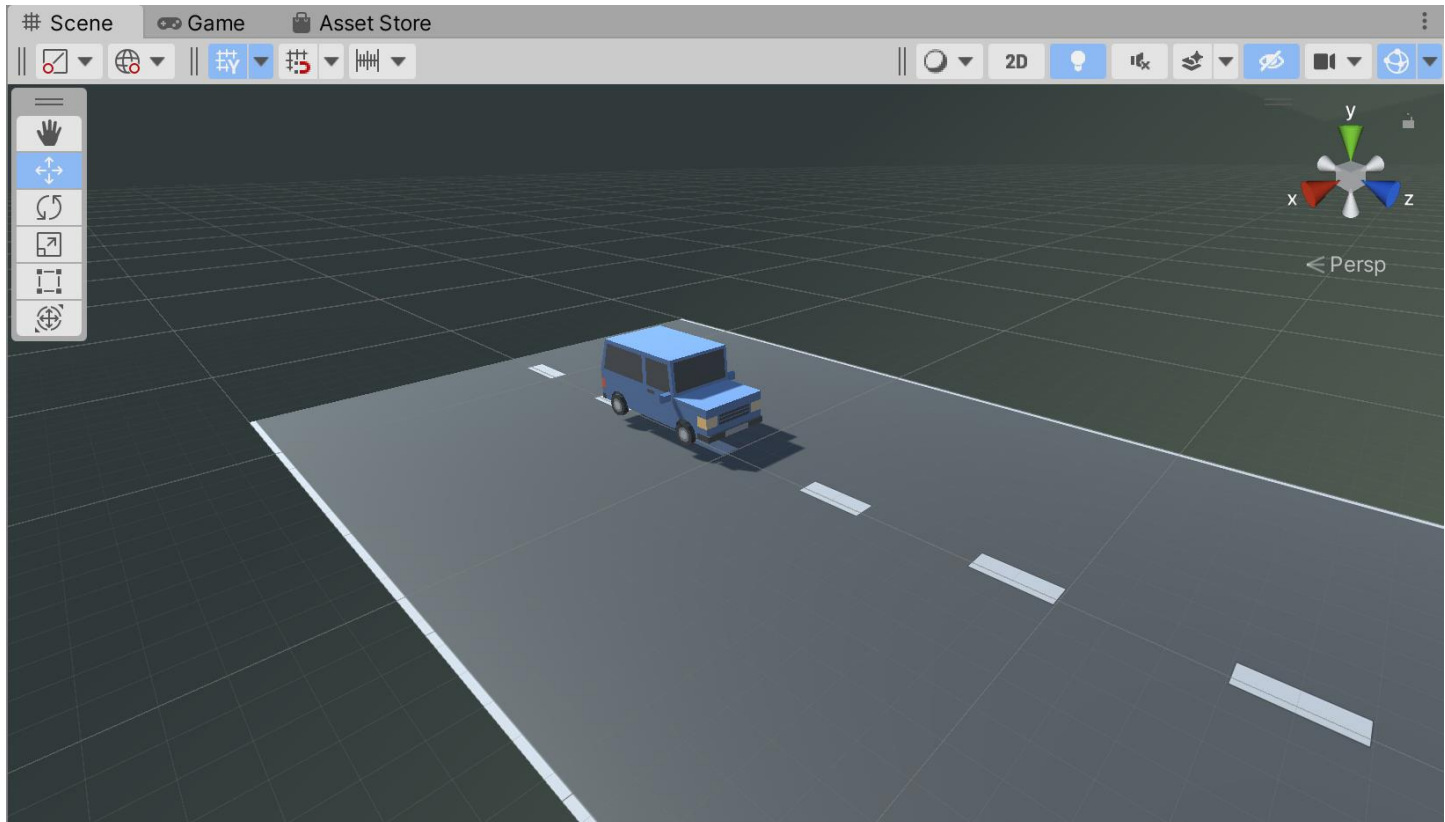
Orthographic



Perspective

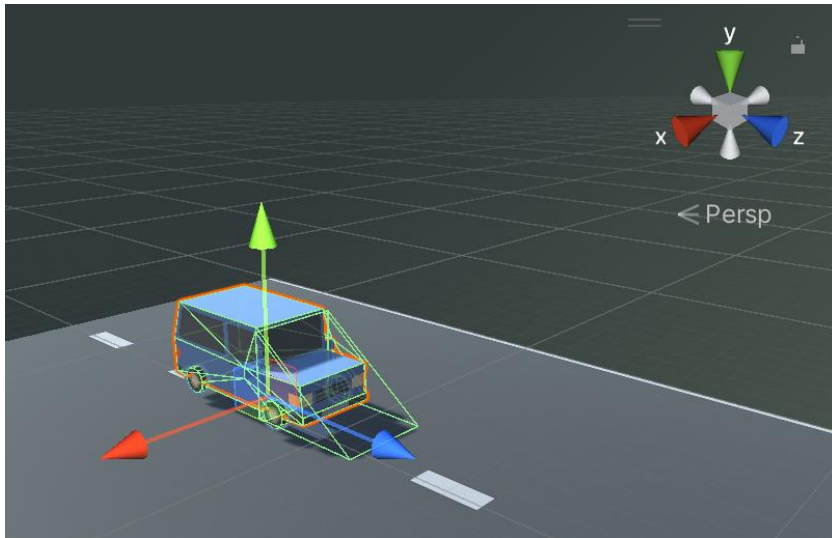
Transform

- ✍ Transform used to store and manipulate the position, rotation and scale of the object.



Coordinate System

 Unity is a **Left-Handed** Coordinate System



<u>right</u>	The red axis of the transform in world space.	X
<u>up</u>	The green axis of the transform in world space	Y
<u>forward</u>	the blue axis of the transform in world space.	Z

[Vector3: Static Properties](#)

Translate in Unity

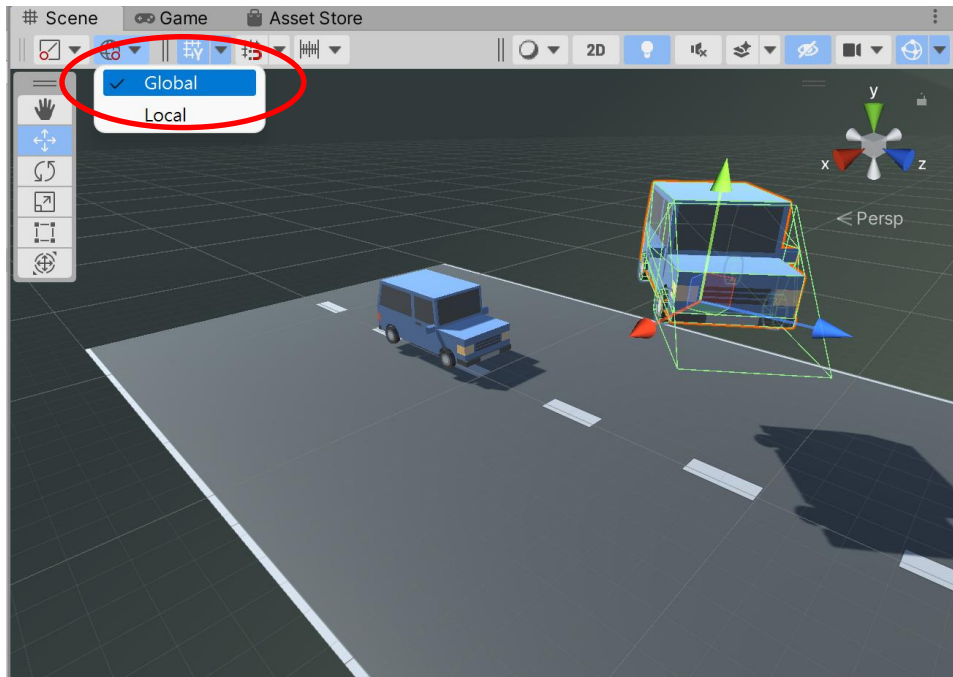
$$\begin{bmatrix} 1 & 0 & 0 & tx \\ 0 & 1 & 0 & ty \\ 0 & 0 & 1 & tz \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

 public
void Translate(Vector3 translation, Space relativeTo =
Space.Self);

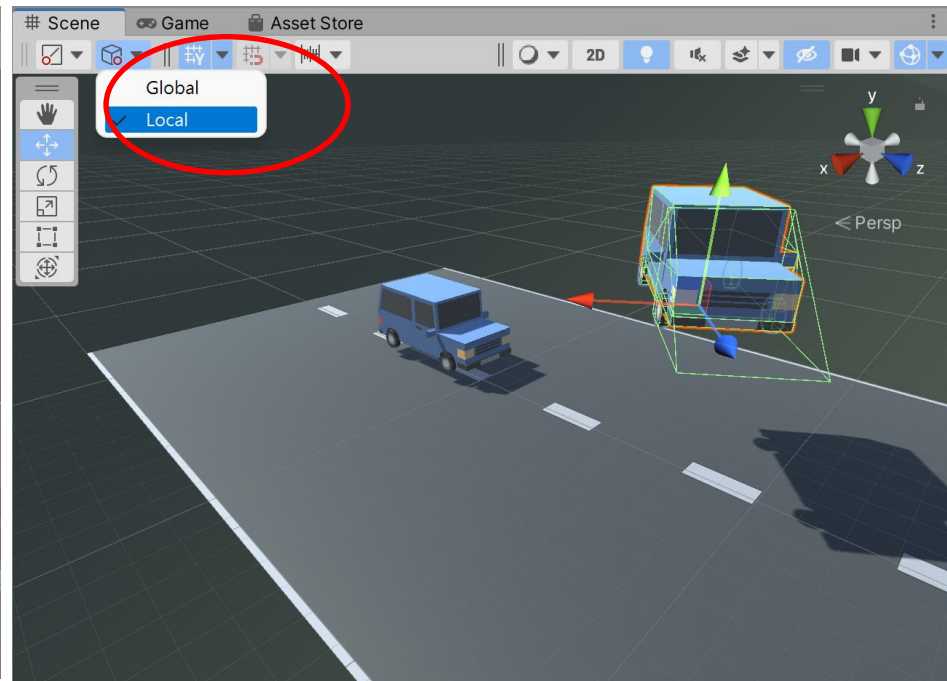
```
// Move the object forward along its z axis 1 unit/second.  
transform.Translate(Vector3.forward * Time.deltaTime);  
  
// Move the object upward in world space 1 unit/second.  
transform.Translate(Vector3.up * Time.deltaTime, Space.World);
```

 public void Translate(float x, float y, float z);

Space



Space.World



Space.Self

Matrix/vector

$$\begin{bmatrix} 1 & 5 & 9 & 13 \\ 2 & 6 & 10 & 14 \\ 3 & 7 & 11 & 15 \\ 4 & 8 & 12 & 16 \end{bmatrix}$$

$$\begin{bmatrix} 1 \\ 2 \\ 3 \\ 4 \end{bmatrix}$$

Scale



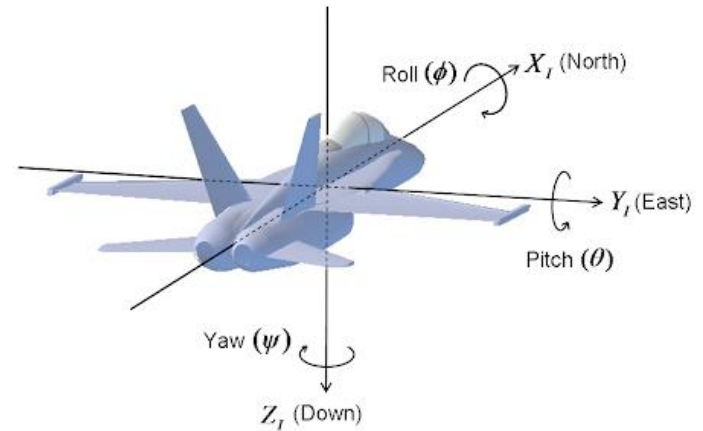
public Vector3 **localScale**;

- The scale of the transform relative to the GameObjects parent.

```
public float x = 0.1f;
public float y = 0.1f;
public float z = 0.1f;
void Update() {
    // Widen the object by x, y, and z values
    transform.localScale += new Vector3(x, y, z);
}
```

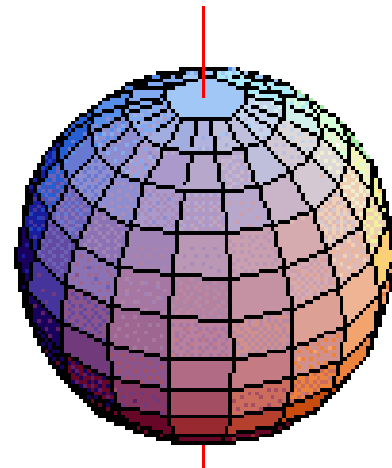
Rotate - Euler Angles

```
public  
void Rotate(Vector3 eulerAngles, Space relative  
To = Space.Self);
```



Rotate – Axis

```
public void Rotate(Vector3 axis,  
float angle, Space relativeTo = Space.Self);  
public  
void RotateAround(Vector3 point, Vector3 axis,  
float angle);
```

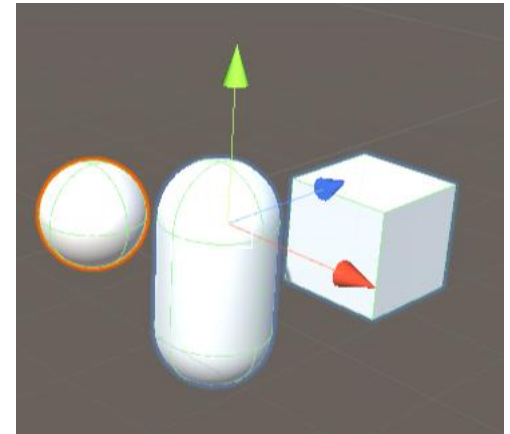
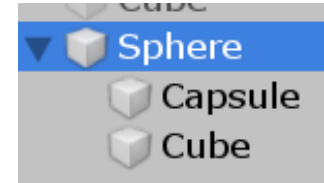


【傅老師】用一顆石頭架場景！！】



Parent/Child

```
// Moves all transform children 10 units upwards!  
void Start()  
{  
    foreach (Transform child in transform)  
    {  
        child.position += Vector3.up * 10.0f;  
    }  
}
```



Reset to parent transform

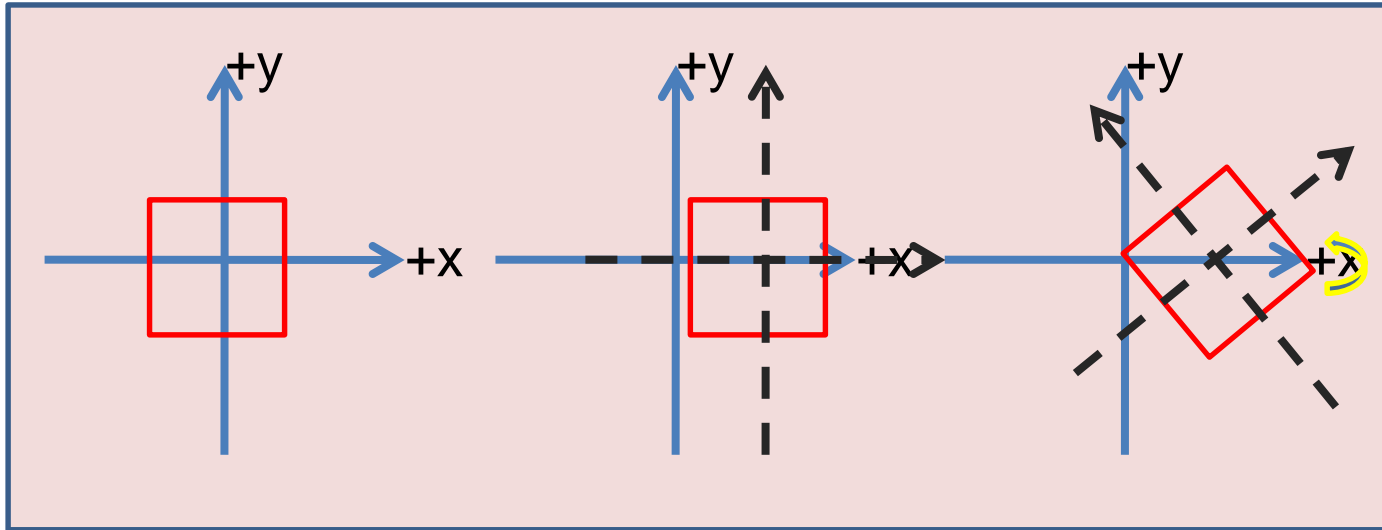
```
transform.rotation = transform.parent.transform.rotation;  
transform.localPosition = Vector3.zero;  
transform.localScale = Vector3.one;
```

SetParent

```
public void Example(Transform newParent)
{
    //Sets "newParent" as the new parent of the player GameObject.
    player.transform.SetParent(newParent);

    //Same as above, except this makes the player keep its local orientation
    //rather than its global orientation.
    player.transform.SetParent(newParent, false);
}
```

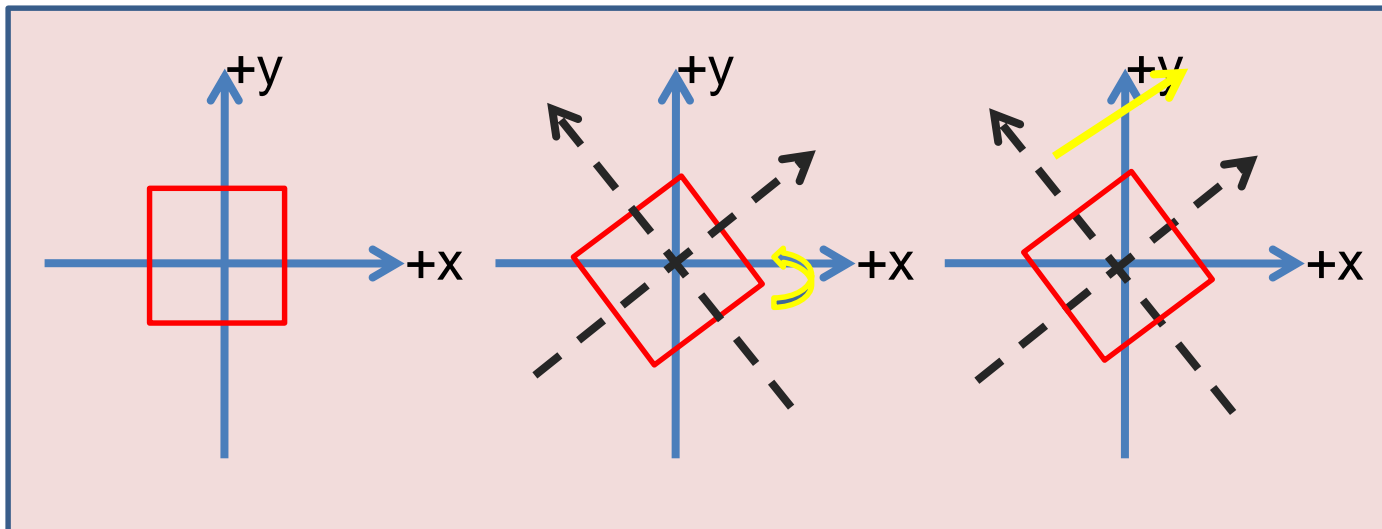
Rotation/Translation from world to object



Translate()

Rotate()

Rect()

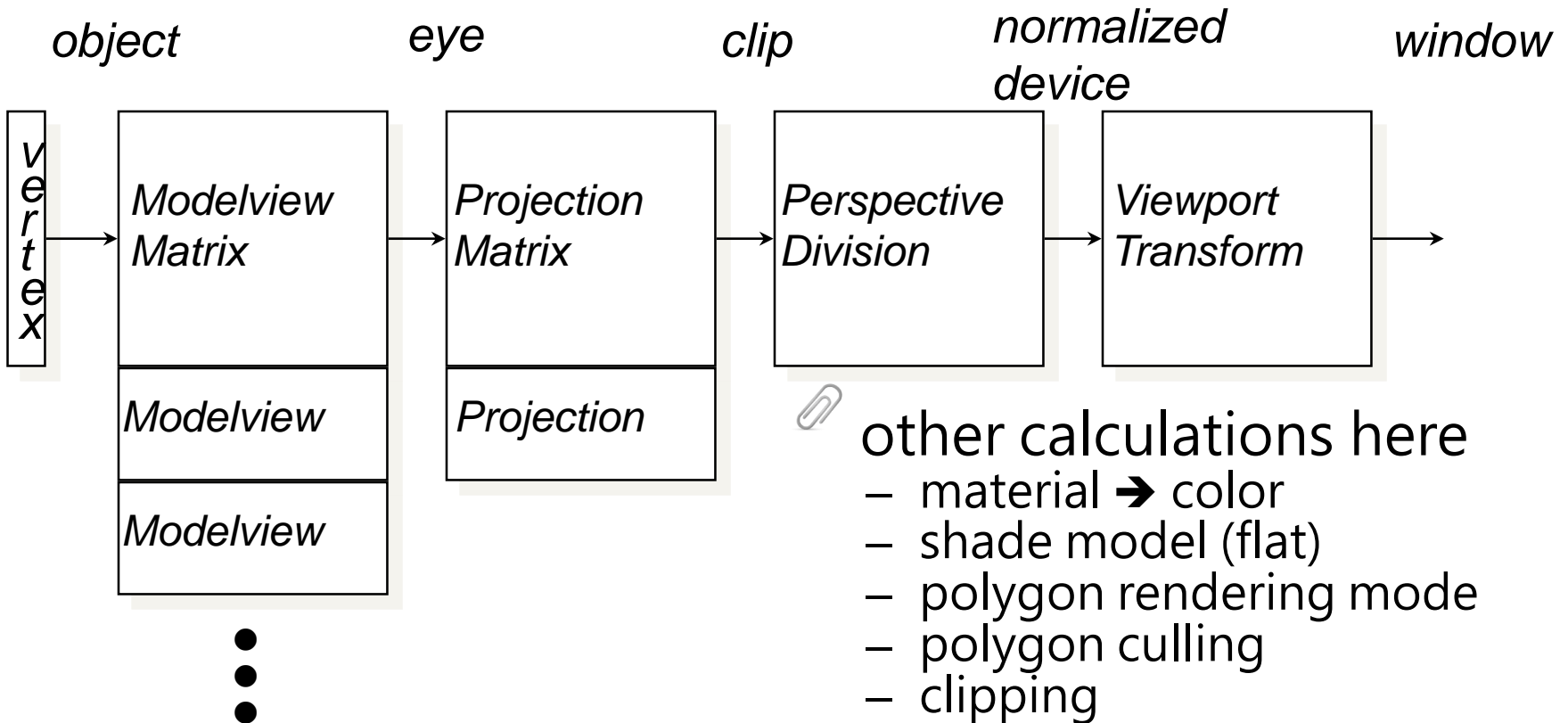
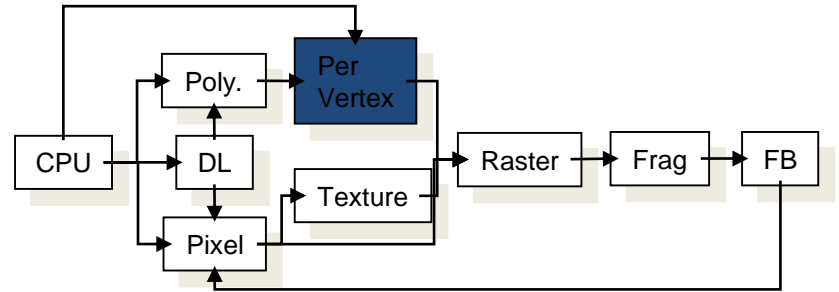


Rotate()

Translate()

Rect()

Transformation Pipeline



The Life of a vertex

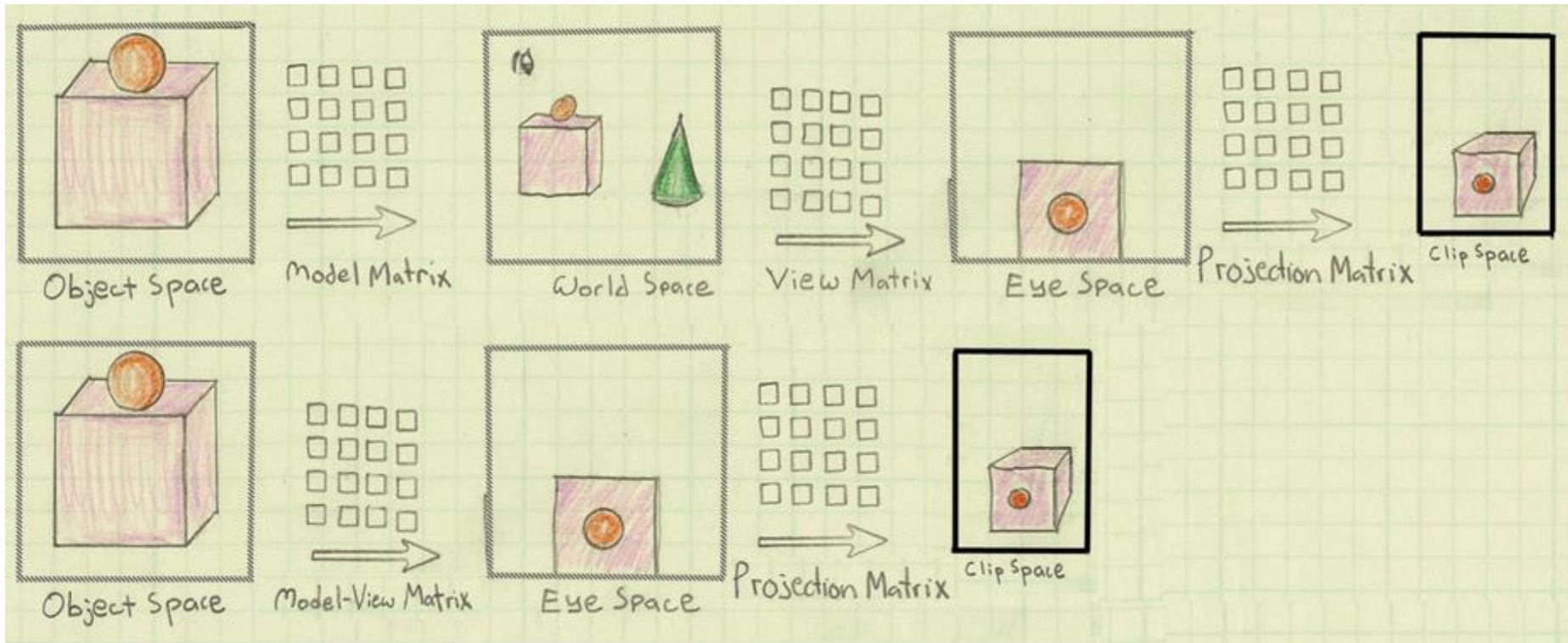
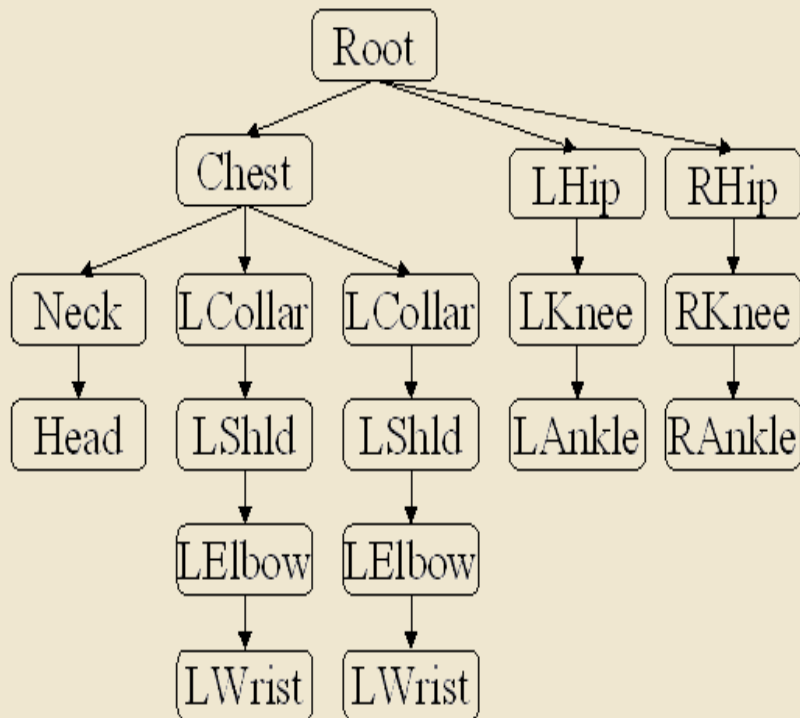


Image by Philp Rideout

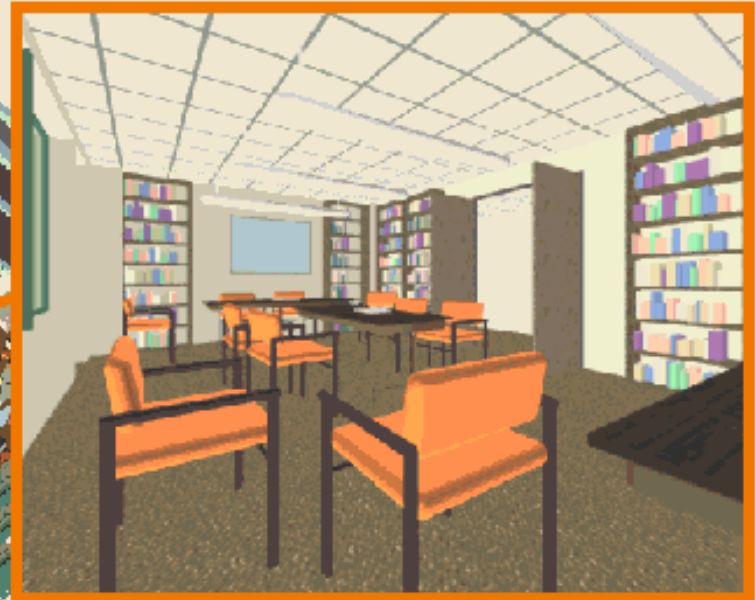
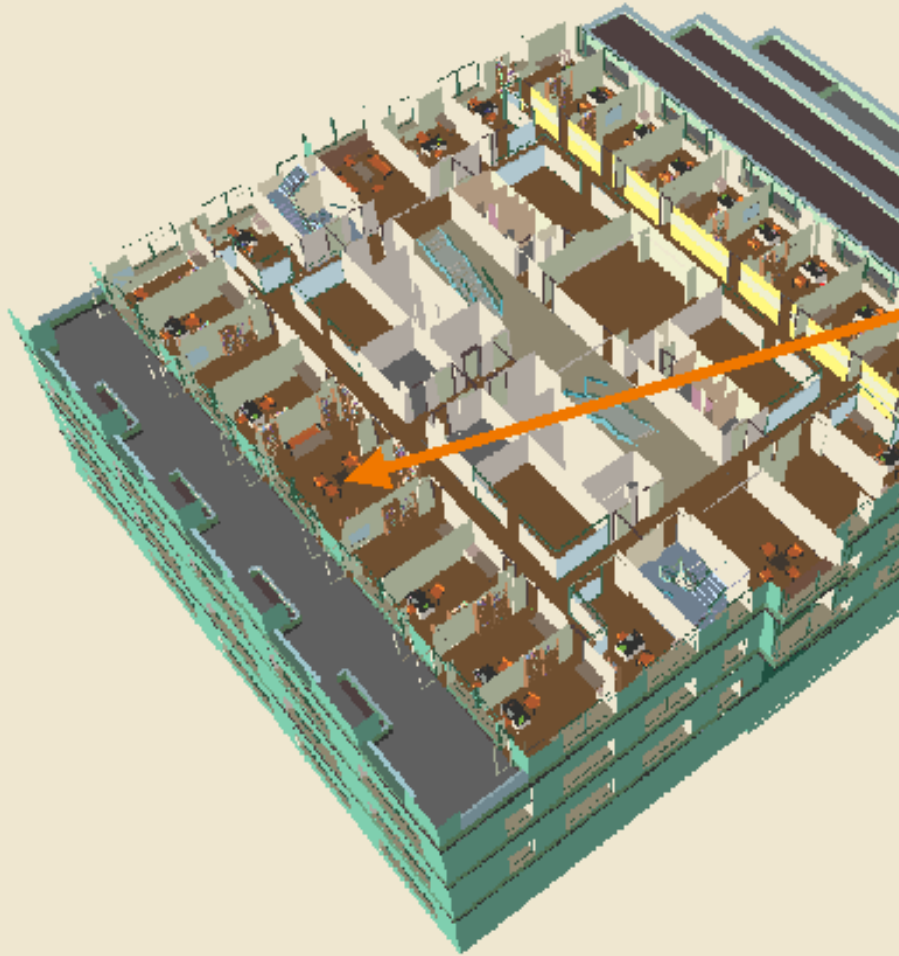
Transformation Example 1

- Well-suited for humanoid characters



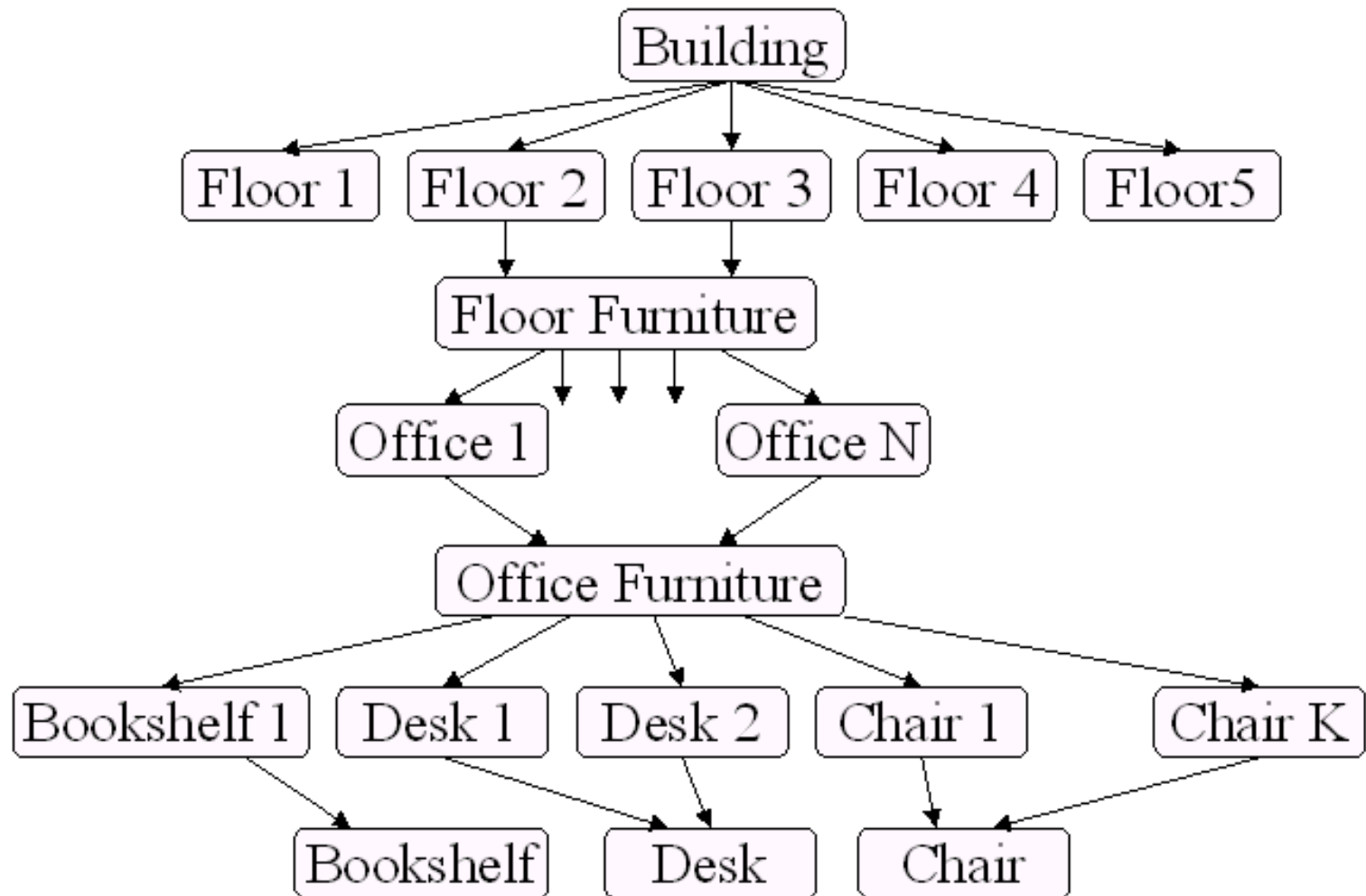
Transformation Example 2

- An object may appear in a scene multiple times



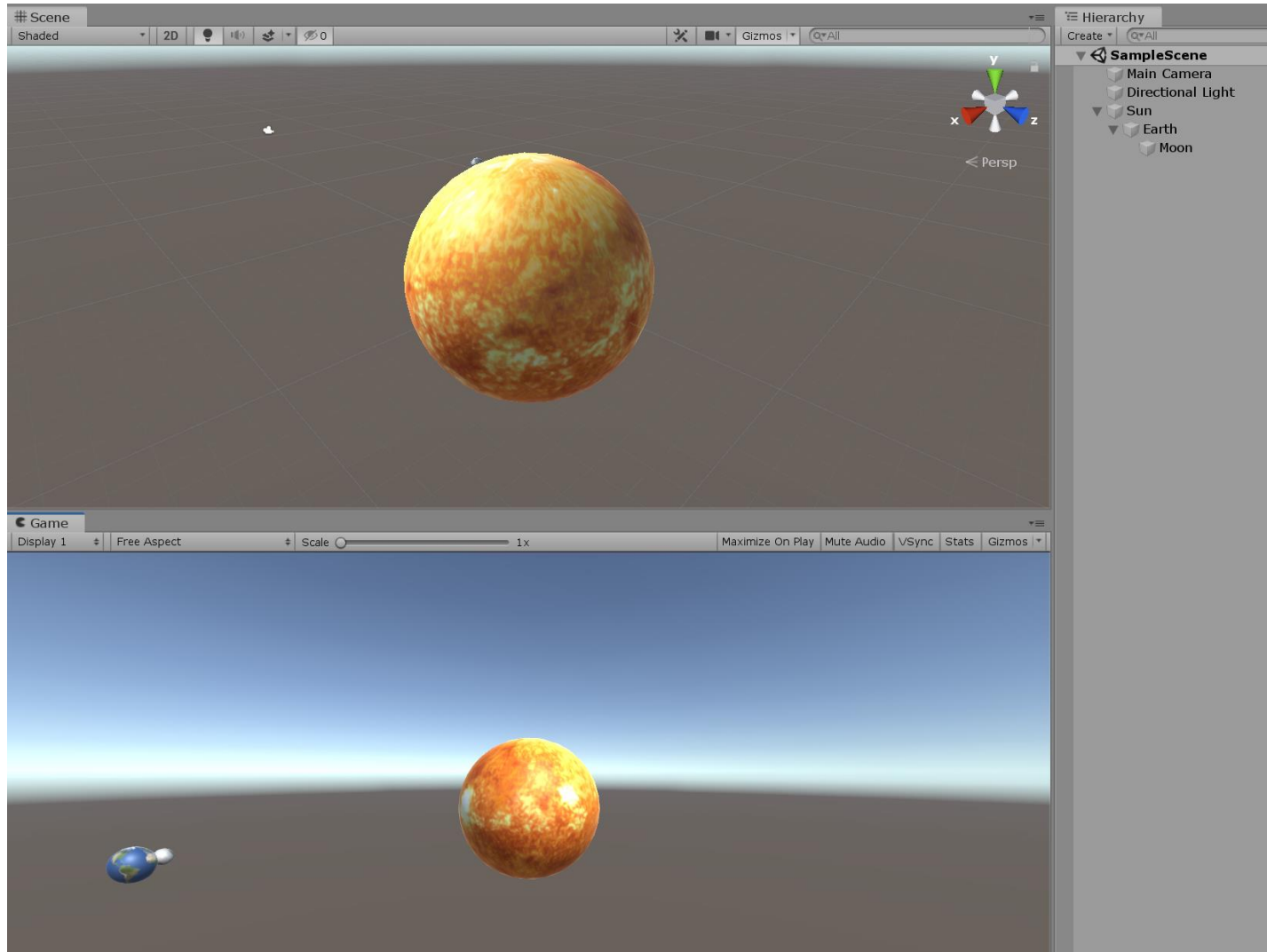
Draw same 3D data with different transformations

Transformation Example 2

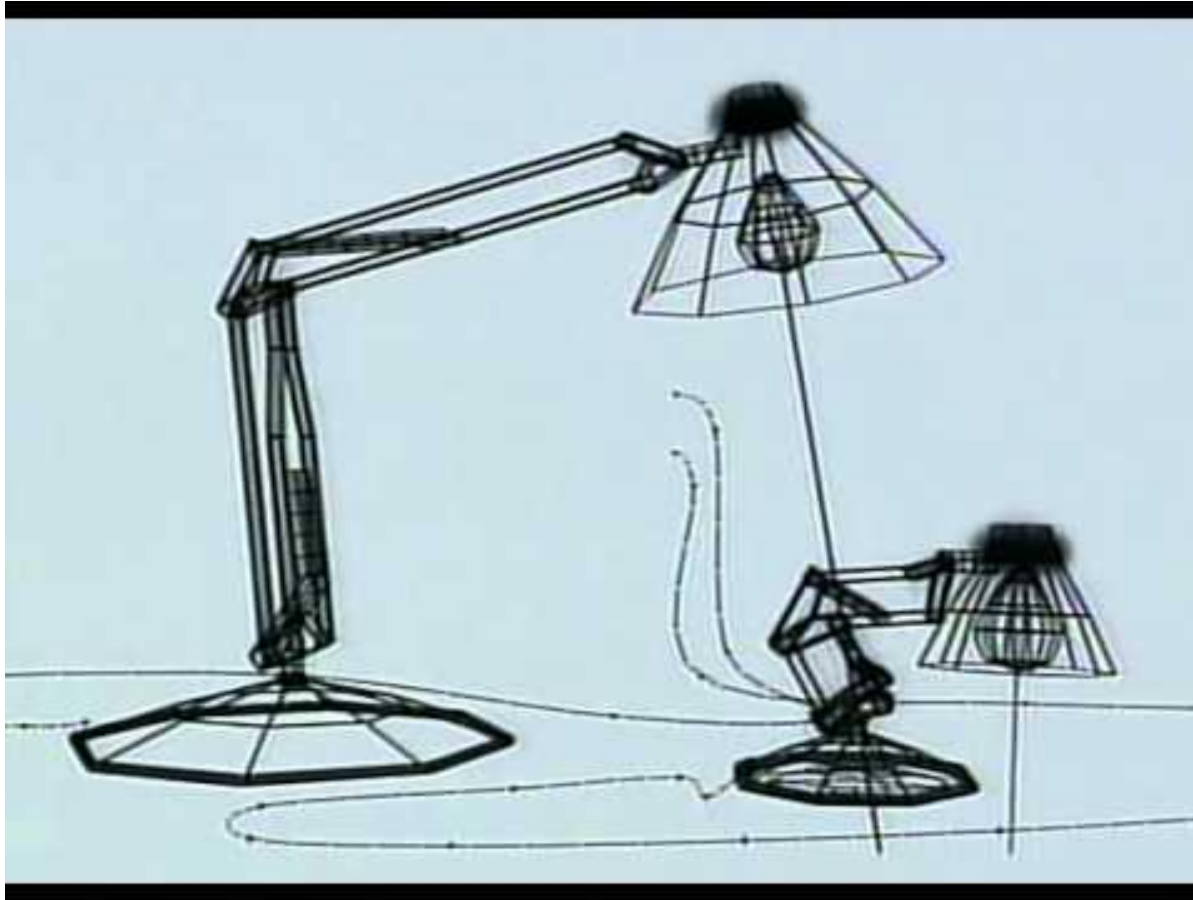


Sun Earth Moon

[Assets download](#)



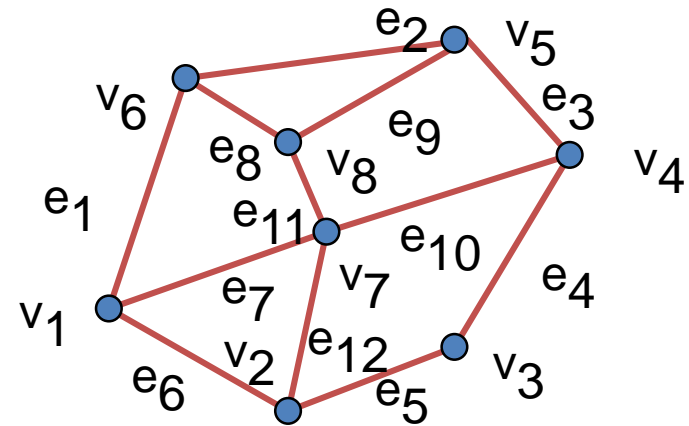
Luxo Jr [Pencil Test] [1986]



MESH FORMAT

Representing a Mesh

📎 Consider a mesh



📎 There are 8 nodes and 12 edges

- 5 interior polygons
- 6 interior (shared) edges

📎 Each vertex has a location $v_i = (x_i \ y_i \ z_i)$

3D model format

SIMPLE



Triangle

vertex1_X vertex1_Y vertex1_Z normal1_X normal1_Y normal1_Z
vertex2_X vertex2_Y vertex2_Z normal2_X normal2_Y normal2_Z
vertex3_X vertex3_Y vertex3_Z normal3_X normal3_Y normal3_Z



COLOR



Triangle

frontcolor_R frontcolor_G frontcolor_B backcolor_R backcolor_G backcolor_B
vertex1_X vertex1_Y vertex1_Z normal1_X normal1_Y normal1_Z
vertex2_X vertex2_Y vertex2_Z normal2_X normal2_Y normal2_Z
vertex3_X vertex3_Y vertex3_Z normal3_X normal3_Y normal3_Z

Simple Representation

- Define each polygon by the geometric locations of its vertices
- Leads to OpenGL code such as

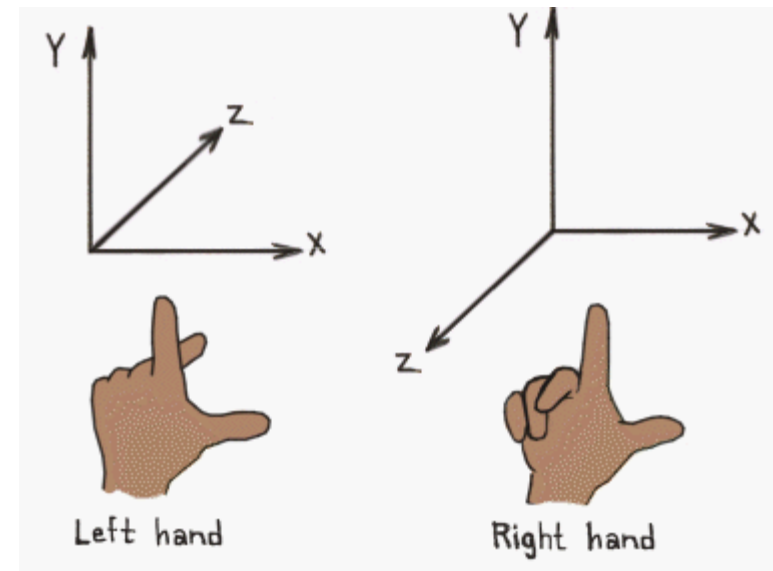
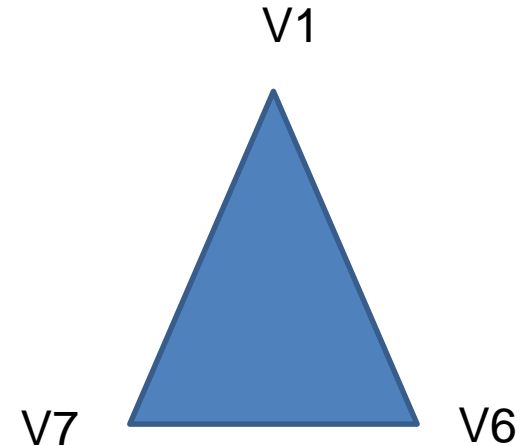
```
glBegin(GL_POLYGON) ;  
    glVertex3f(x1, x1, x1) ;  
    glVertex3f(x6, x6, x6) ;  
    glVertex3f(x7, x7, x7) ;  
glEnd() ;
```

- Inefficient and unstructured
 - Consider moving a vertex to a new location
 - Must search for all occurrences

Inward and Outward Facing Polygons

📎 The order $\{v_1, v_6, v_7\}$ and $\{v_6, v_7, v_1\}$ are equivalent in that the same polygon will be rendered **but the order $\{v_1, v_7, v_6\}$ is different.**

📎 Use the ***left-hand rule*** = clockwise encirclement of outward-pointing normal



Left-handed

Right-handed

Y
is
up



DirectX



Z
is
up



UNREAL
ENGINE



Wavefront obj format



#example obj file

v -1.63326156 -3.04798102 -8.81131839

....

vn 0.00379090 0.40057179 0.01256634

...

vt 0.22390614 0.97395277 (texture)

...

f 4/2/4 3/1/3 2/2/2 (index to v/t/n)

Reference



obj format

<http://www.martinreddy.net/gfx/3d/OBJ.spec>



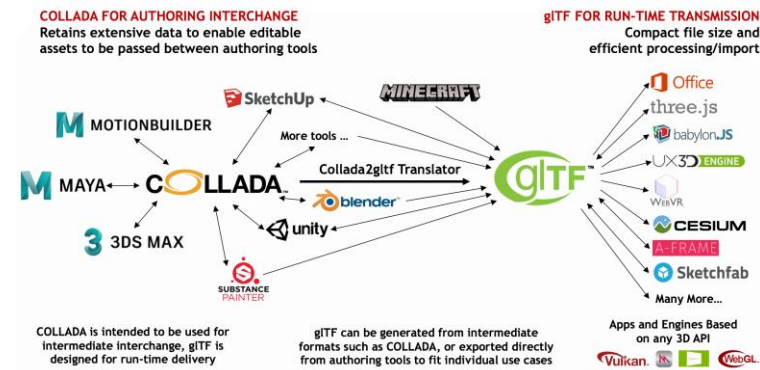
ply format



STL format -

[http://en.wikipedia.org/wiki/STL_\(file_format\)](http://en.wikipedia.org/wiki/STL_(file_format))

Scene Graph



FBX (Filmbox) by Autodesk



COLLADA (*COLLABorative Design Activity*)



Alembic by sony



USD (Universal Scene Description) by pixar

– Five Things to Know About USD



Universal Scene Description, USD

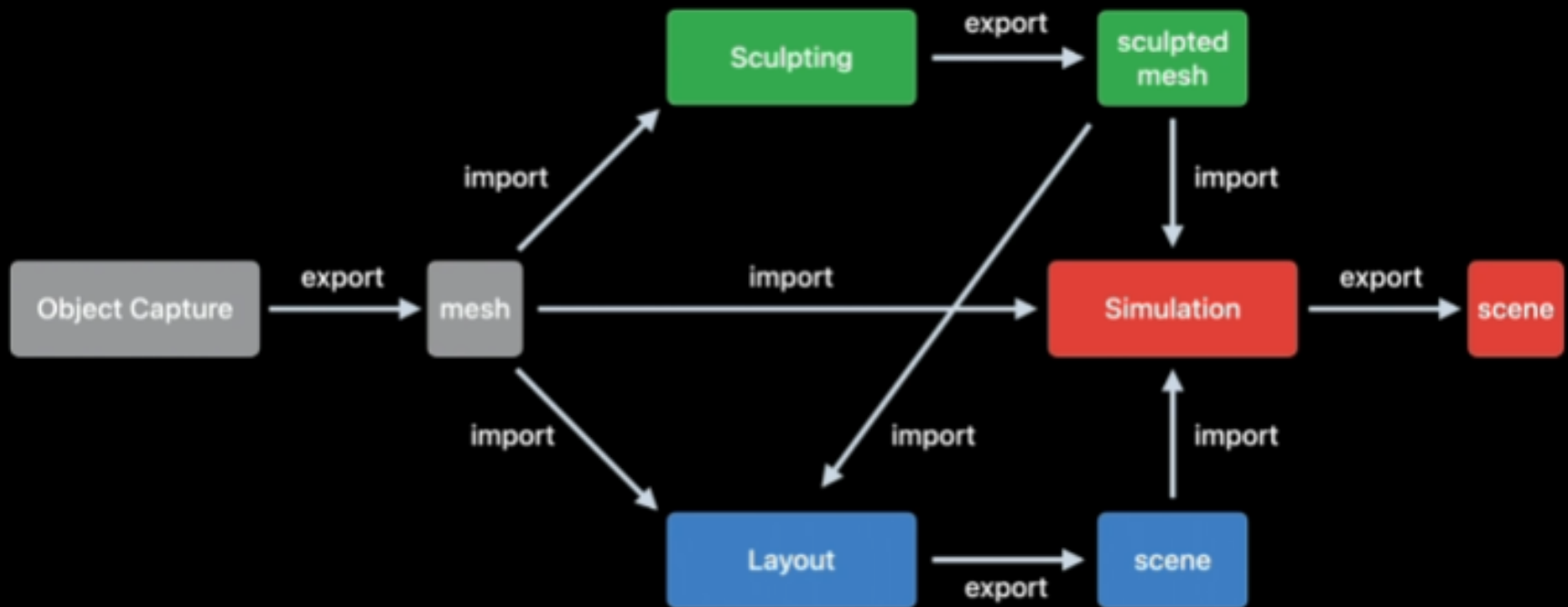
([WWDC 2021](#))

3D file formats

		Live composition, collaboration	Bundles textures, audio, ...
		Scalable to complex scenes	Scalable to complex scenes
	Scene graph	Scene graph	Scene graph
3D model	3D models	3D models	3D models
.obj	.gltf, .fbx, .abc	.usd	.usdz

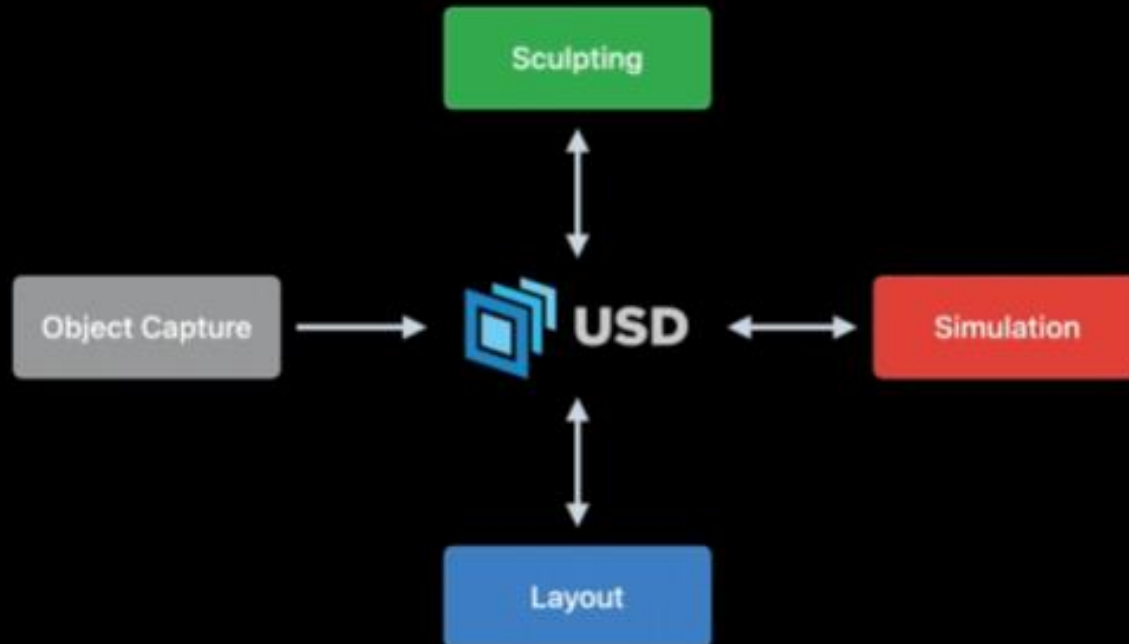
Create 3D workflows with USD ([WWDC 2021](#))

Traditional workflow



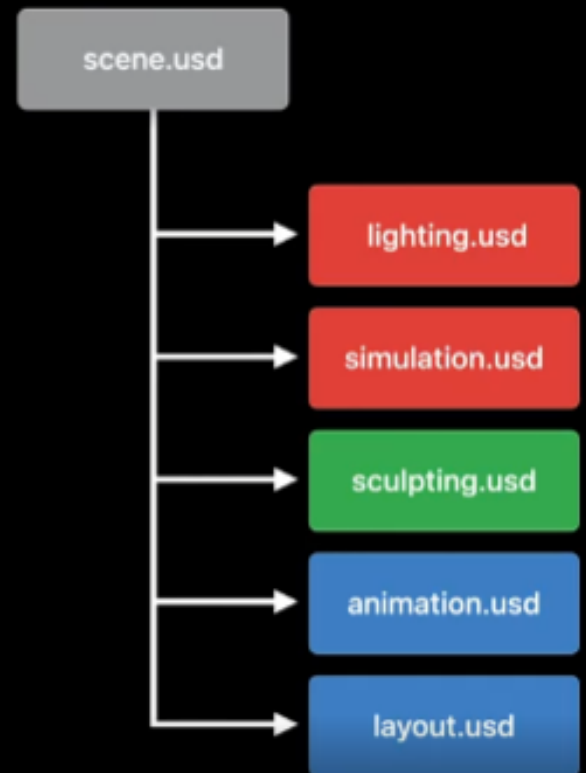
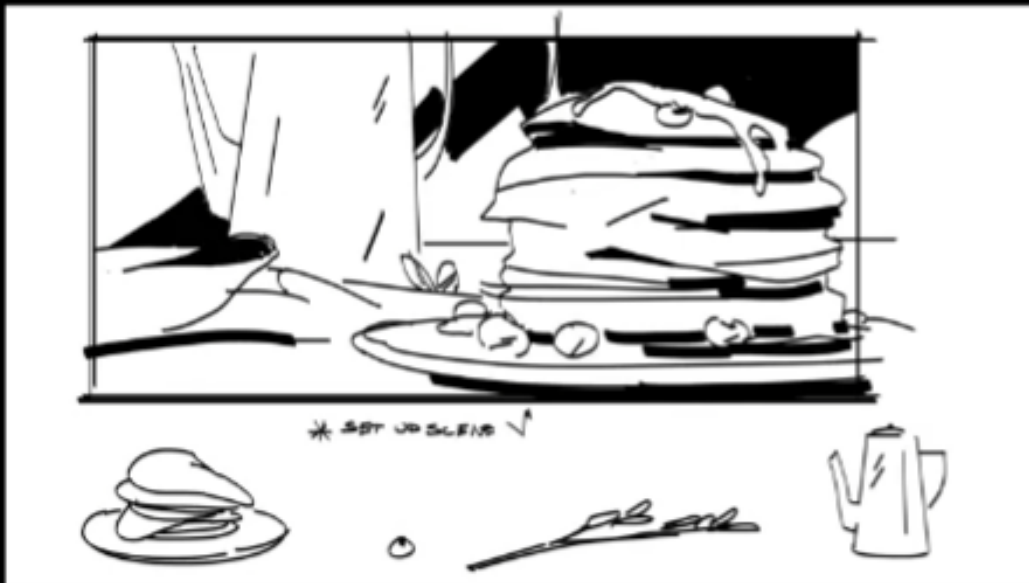
Create 3D workflows with USD ([WWDC 2021](#))

USD workflow



Create 3D workflows with USD ([WWDC 2021](#))

Structure



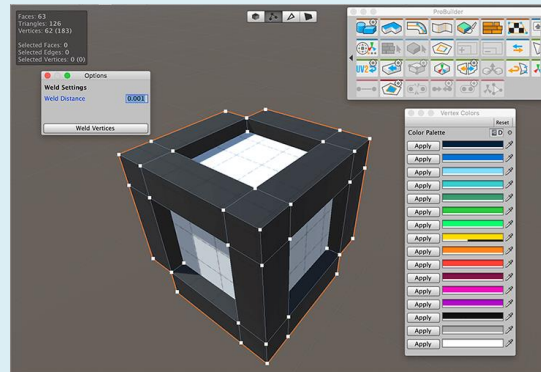
PROBUILDER

Building and editing complex Meshes inside Unity

Modeling



Assemble
with Primitive



ProBuilder
inside Unity

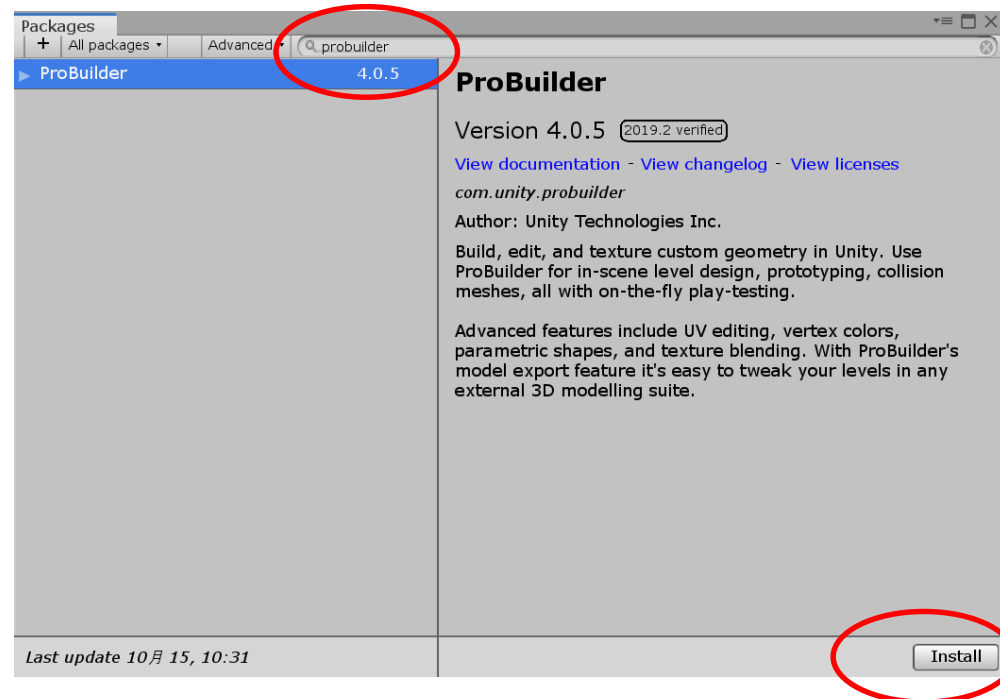


Import
from modeling
tools



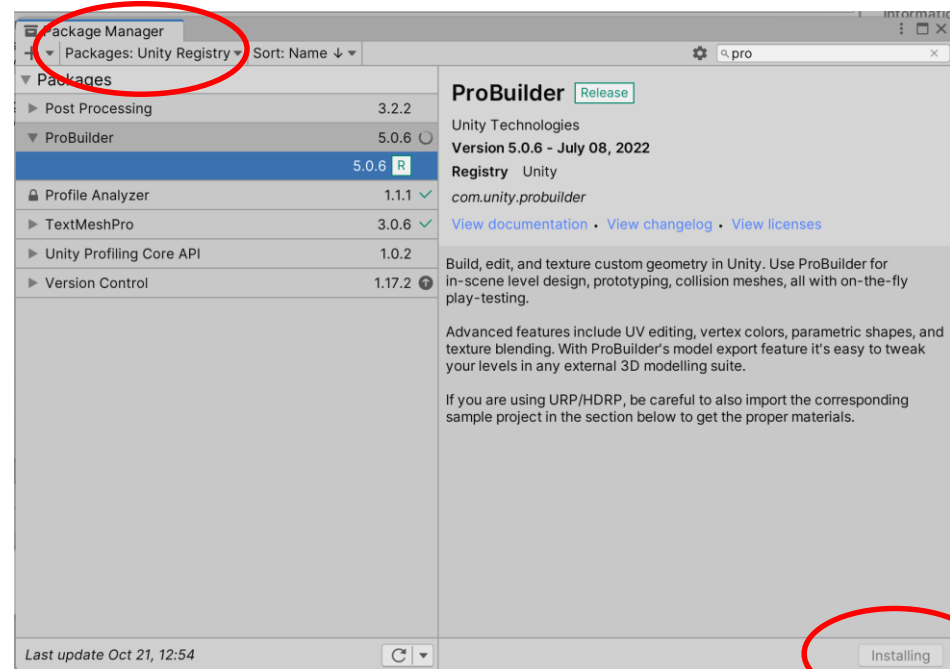
Installing ProBuilder

- Open the Package Manager (in Unity's top menu: **Window > Package Manager**).
- Enter **ProBuilder** in the search box.
- Click **ProBuilder** in the package list (left side), then click the **Install** button in the package details (right side).



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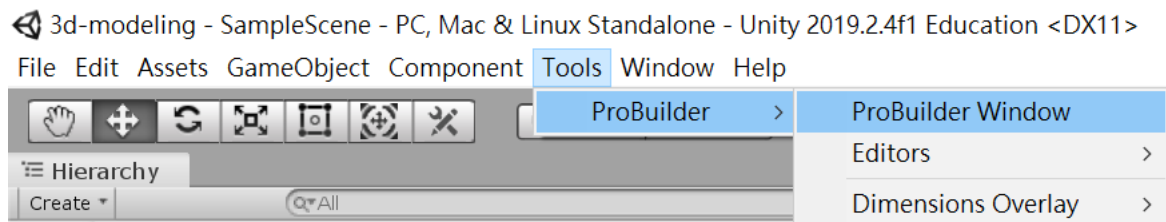


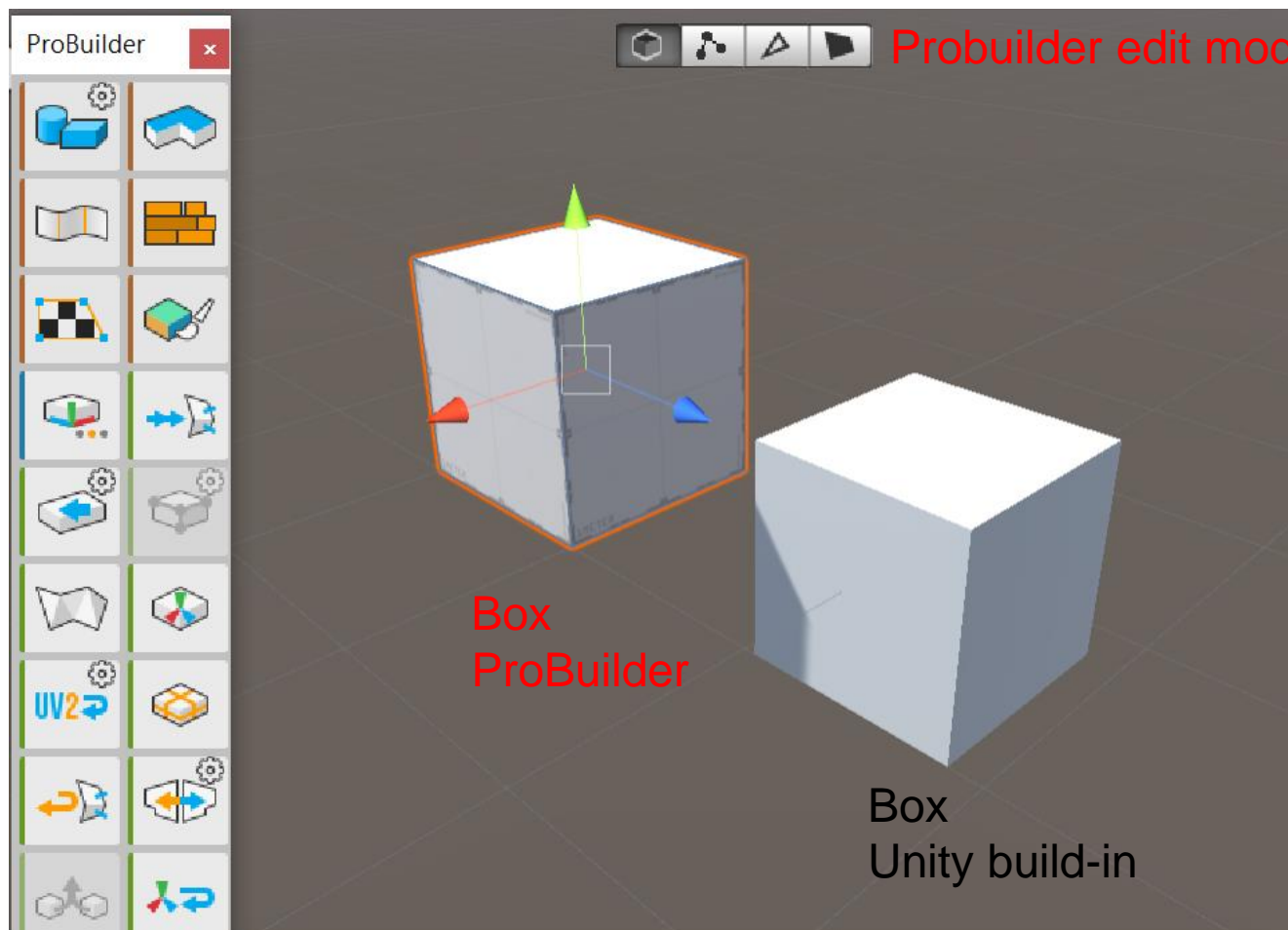


To verify that ProBuilder is correctly installed, open the ProBuilder toolbar (from Unity's top menu: **Tools > ProBuilder > ProBuilder Window**).



If you don't see the ProBuilder Window menu item, then ProBuilder did not install correctly.





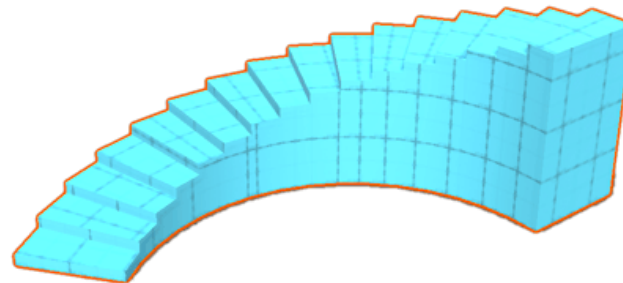
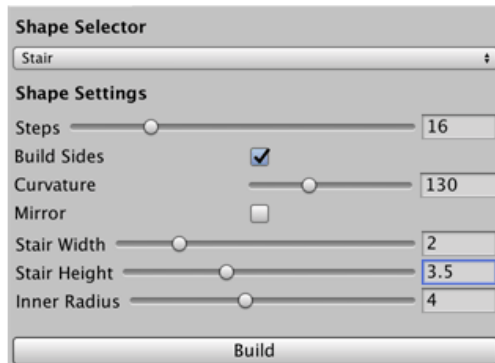
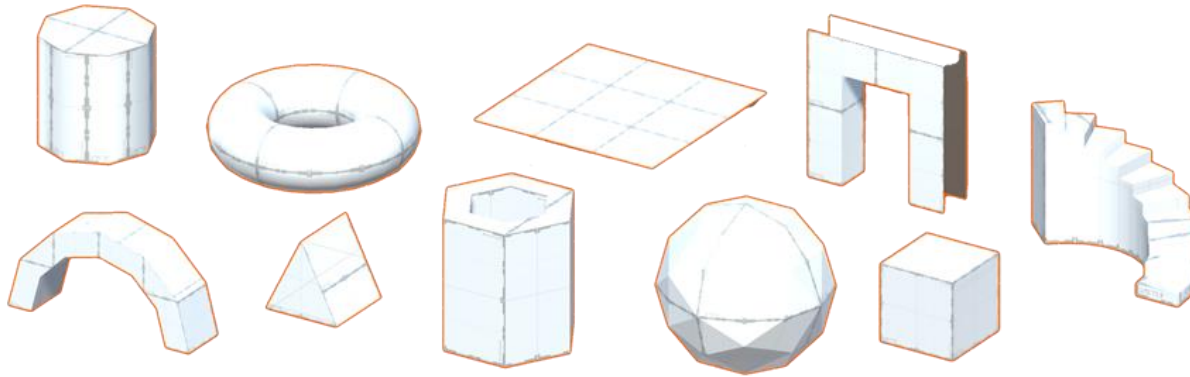
Probuilder edit mode toolbar

Box
ProBuilder

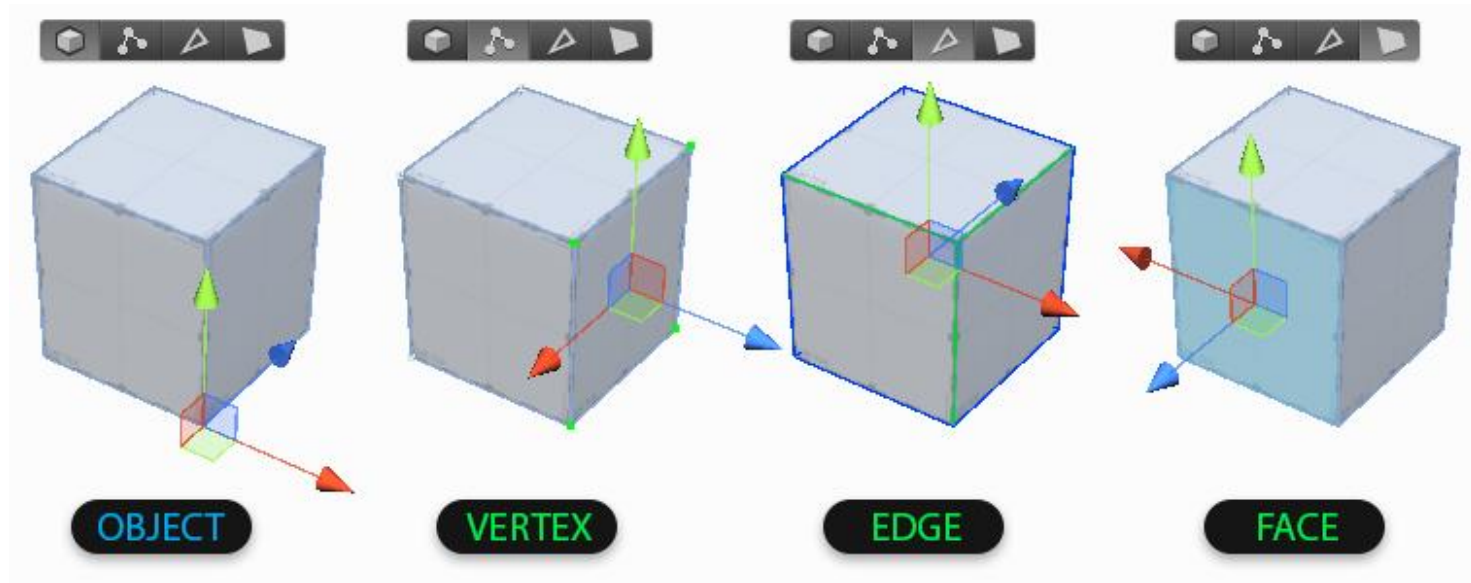
Box
Unity build-in

Probuilder toolbar

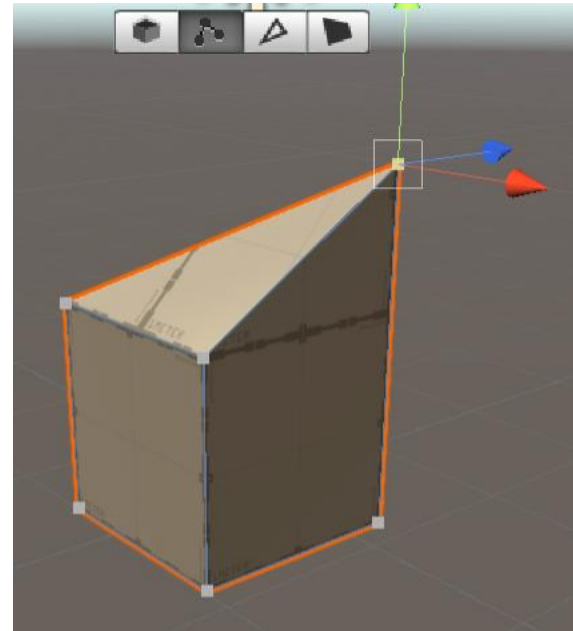
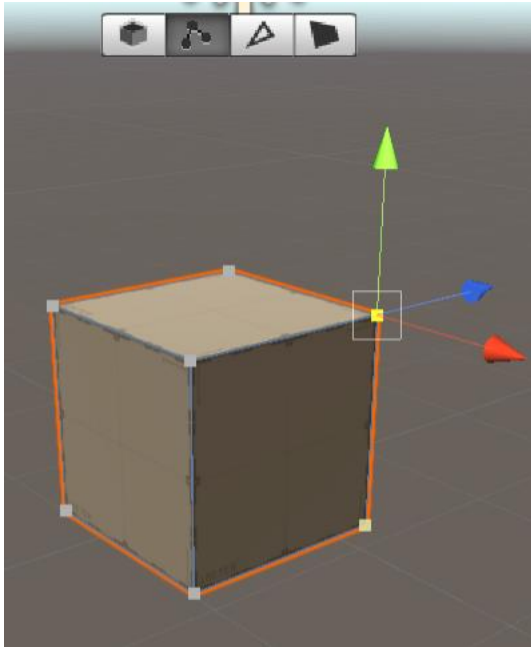
Creating Meshes



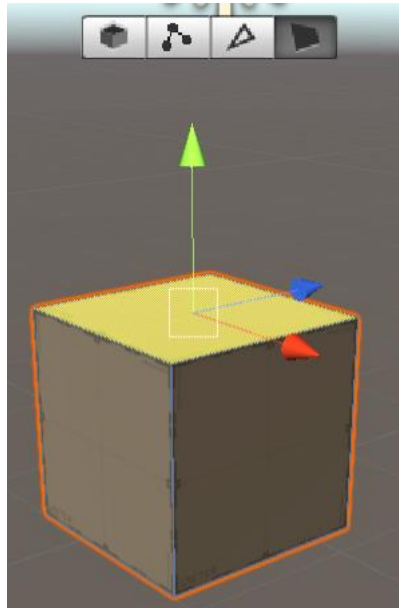
Edit modes (Object vs Element)



Select -> Transforming

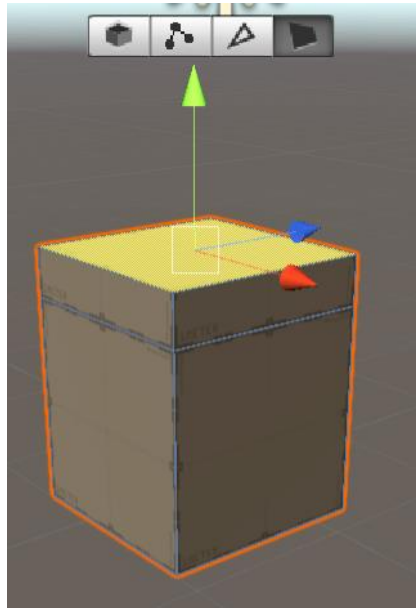


Select face -> Extruding



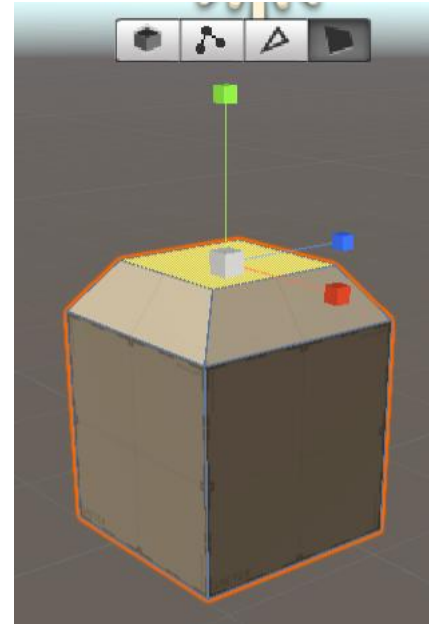
Select a face

Extruding



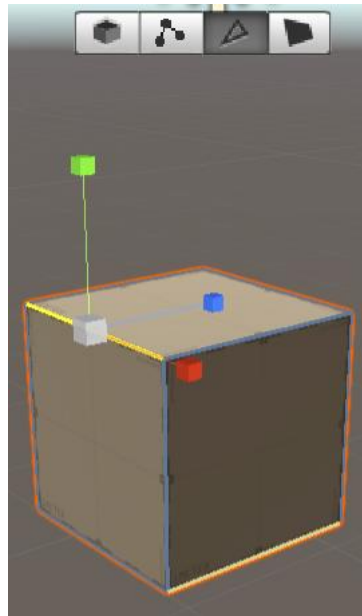
Shift key +
Translate

Insetting

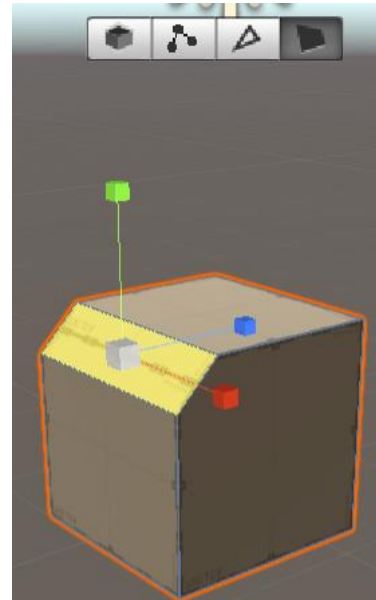


Shift key +
Scale

Select edge -> Bevel

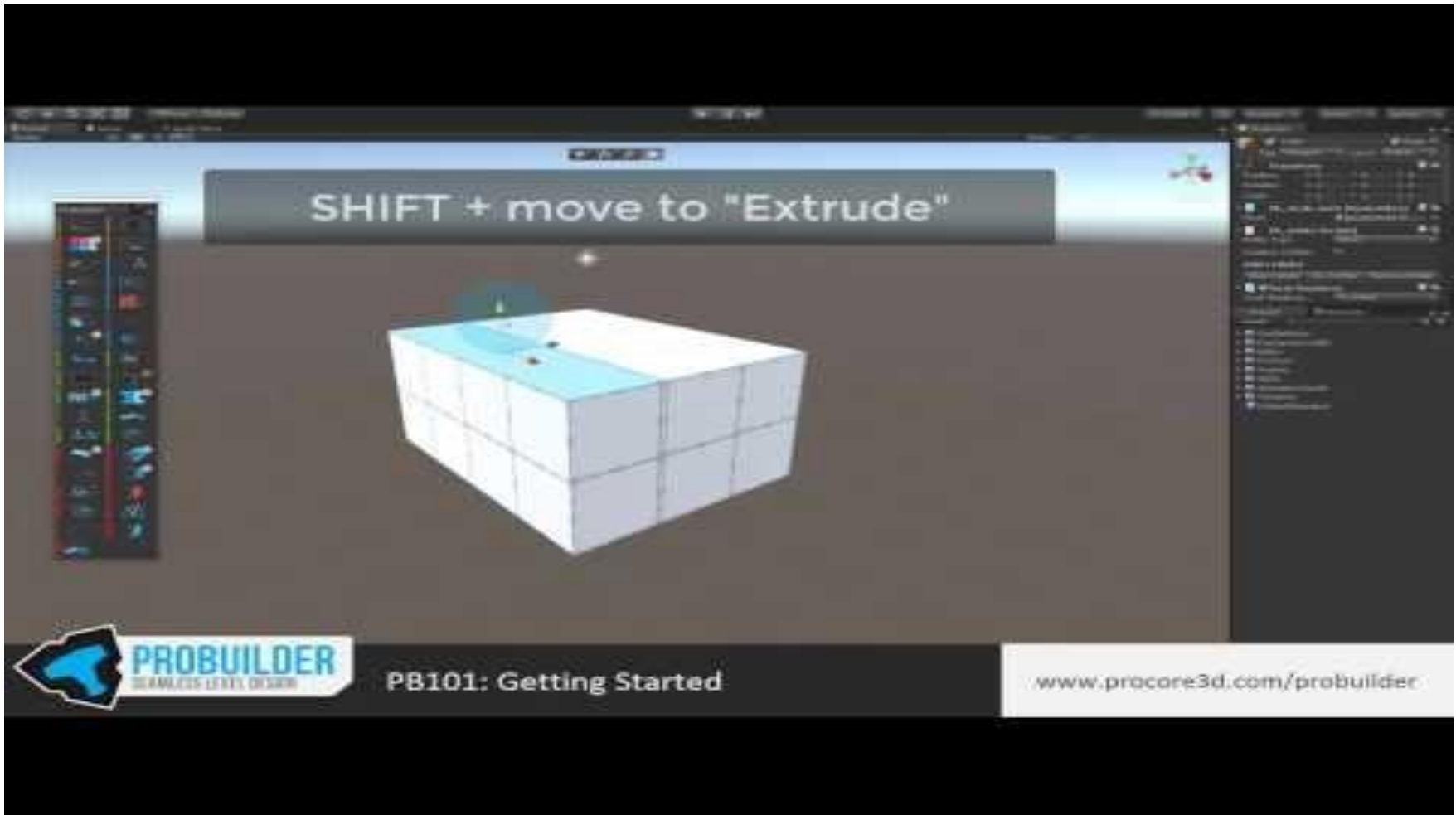


Select a edge

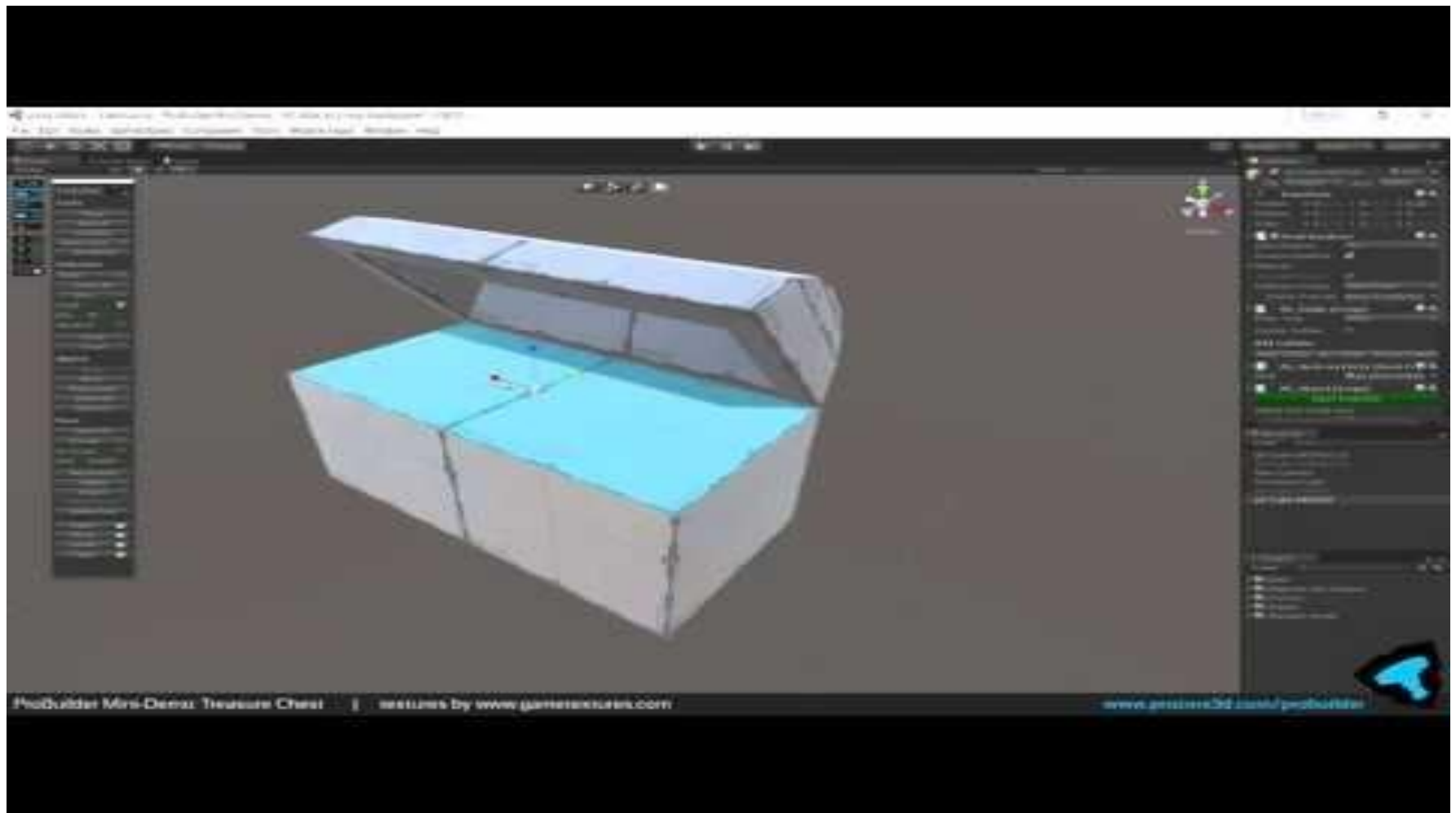


Bevel edge

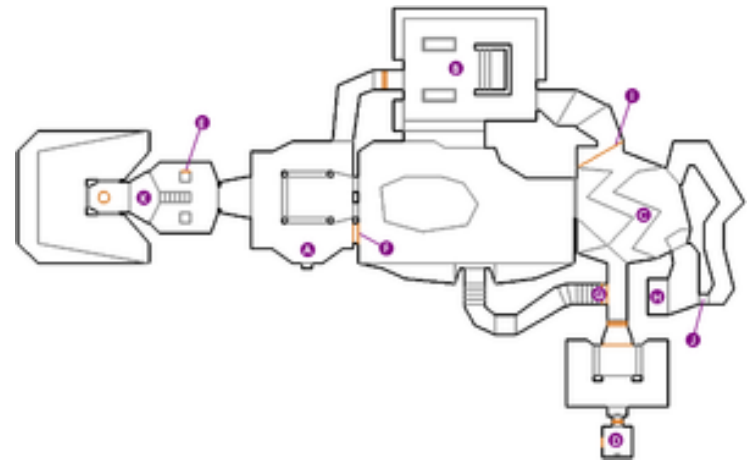
Getting Started with ProBuilder for Unity



Treasure Chest



Level Editor



PROBUILDER "HOW TO MAKE..." TUTORIAL SERIES:
RE-CREATING THE "E1M1" LEVEL FROM DOOM, IN UNITY 3D

PART 1: FLOORS



PART 2: WALLS



PART 3: CEILINGS



PART 4: COLORIZING



PART 5: TEXTURING



PART 6: DOORS



PART 7: CUSTOM COLLISION



PART 8: OCCLUSION



PART 9: TRIGGERS



PART 10: LIGHTING



PROBUILDER BRINGS CORE LEVEL DESIGN AND GEOMETRY CREATION FUNCTIONALITY TO UNITY 3D - WWW.PROCORE3D.COM

ULTIMATE FPS CAMERA - THE SMOOTHEST CONTROLS AND MOST POWERFUL FPS CAMERA AVAILABLE FOR UNITY - WWW.VISIONWORKS.COM



UFPS