

# **Announcement on Moodle**

# Announcement on Moodle

1122\_703038001/75384 ...

Home

儀表板

事件

我的課程

這個課程



我的課程 > 1122 > 資訊學院-College of Informatics > 資訊科學系-Co



公告 Announcements



程式作業討論區

# Announcement on Moodle (Cont.)

Home 儀表板 事件 我的課程 這個課程

## 公告 Announcements

一般消息與公告

新增一個主題

### 議題

作業回饋

手寫作業一成績公布與解答

課程助教

程式作業一：成績公布

手寫作業二公布

程式作業一：線上測試 Python 使用版本

程式作業一：關於 random-restart 最佳 cost 的廁所位置

台灣 AI 博覽會 - AI EXPO 2024 (自由參加)

程式作業一：random-restart 時間限制

程式作業一：距離計算簡化

程式作業一：random-restart 次數問題

### 開始於



李逸盛



李逸盛



Wei LY



李逸盛



Wei LY



Wei LY



Wei LY



Wei LY



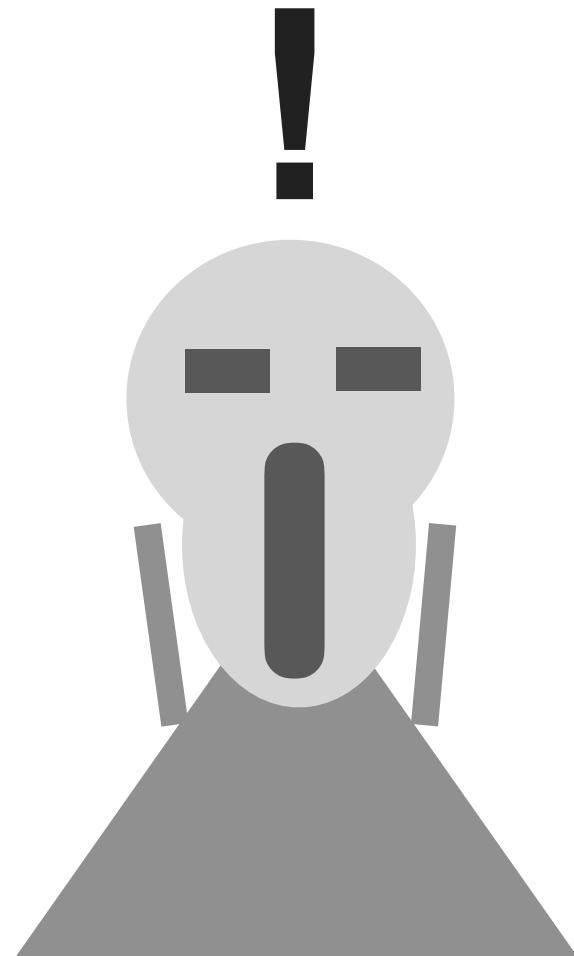
李逸盛



Wei LY



Wei LY



# Get Announcement Information by Email

- Moodle: default email setting: Mail2000 (@.[nccu.edu.tw](mailto:nccu.edu.tw))
- Method 1
  - Modify your email address on Moodle
- Method 2
  - Use auto-forwarding in Mail2000
    - ref. <https://sites.google.com/g.nccu.edu.tw/gsuite/auto-forward>

# Method 1



偏好 > 用戶帳號 > 編修個人資料

Wei LY

▼ 一般

姓氏 \*

Wei

名字 \*

LY

電子郵件信箱 \*

lywei@g.nccu.edu.tw

## Method 2

# 政大郵件信箱的信自動轉到Google Workspace

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1. 登入mail2000系統 <http://nccu.edu.tw/>
2. 點選左側的個人設定->信件處理->自動轉寄



寫信

信件匣

通訊錄

云端硬碟

信箱服務

個人設定

▶ 信箱安全

▶ 個人化設定

▼ 信件處理

- 自動回覆

- 自動轉寄

- 信件過濾

▶ 簡易廣告信過濾

## 信件自動轉寄

我要啟用信件自動轉寄。

系統自動將來信轉至下列位址，空白代表不使用該轉寄位址。

電子郵件位址1：

電子郵件位址2：

電子郵件位址3：

保留副本

限期轉寄

4. 如欲保留副本於mail2000系統上，請勾選「保留副本」。

5. 最後請按下「確定」。

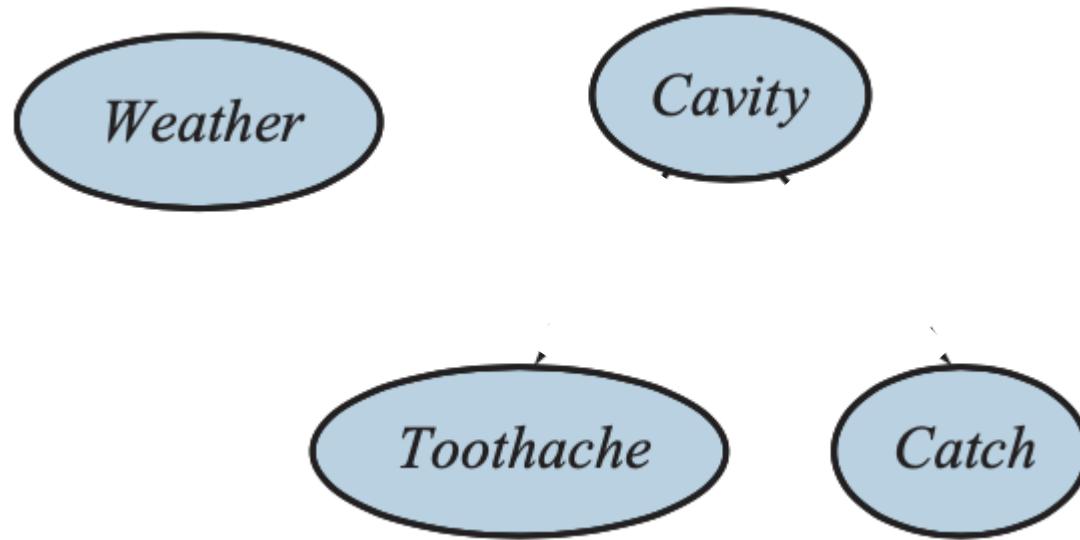
# Issue for Full Joint Probability Distribution

- Examples
  - For **3** boolean variables,  
a full joint probability distribution requires  $2 \times 2 \times 2 = 2^3 = 8$  numbers
  - For **30** boolean variables,  
a full joint probability distribution requires  **$2^{30}$**  numbers

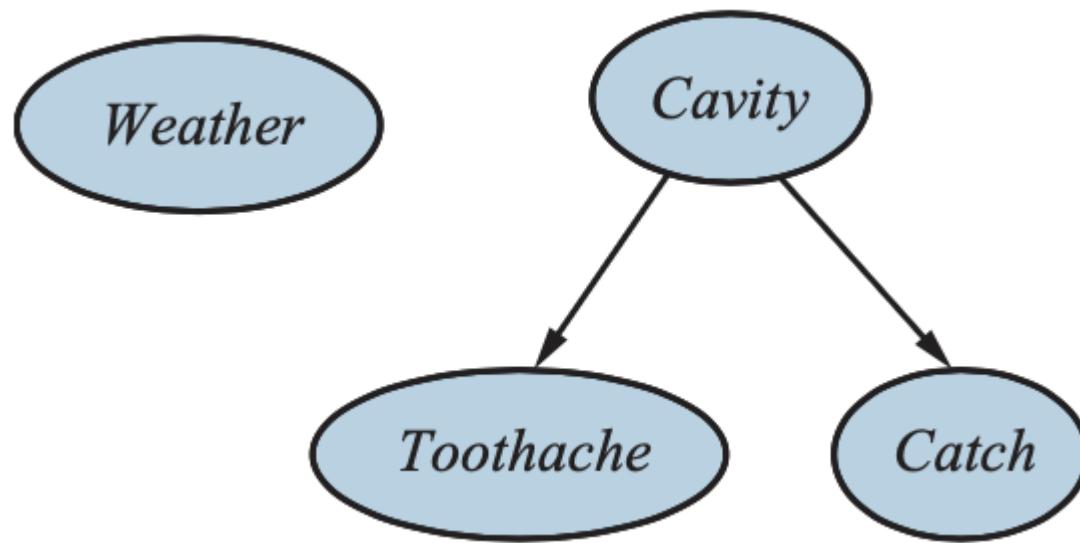
Some variables are

**independent or conditional independent**

# Example

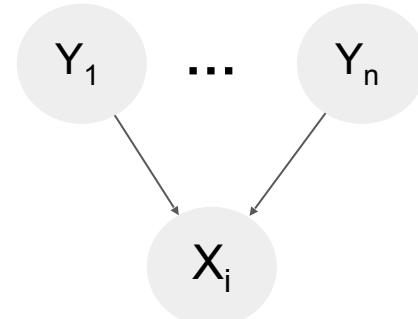


# Example



# Bayes Net Semantics

- Bayes net = Topology (directed graph) + Local Conditional Probabilities
  - Graph
    - Nodes: random variables
    - Edges: dependency between variables
      - If Y has a direct influence on X, there is an arrow from node Y to node X (Y is a parent of X)
  - A conditional distribution for each node
    - Each node  $X_i$  has associated probability information
$$P(X_i | \text{Parents}(X_i))$$
    - **Conditional probability table (CPT)**

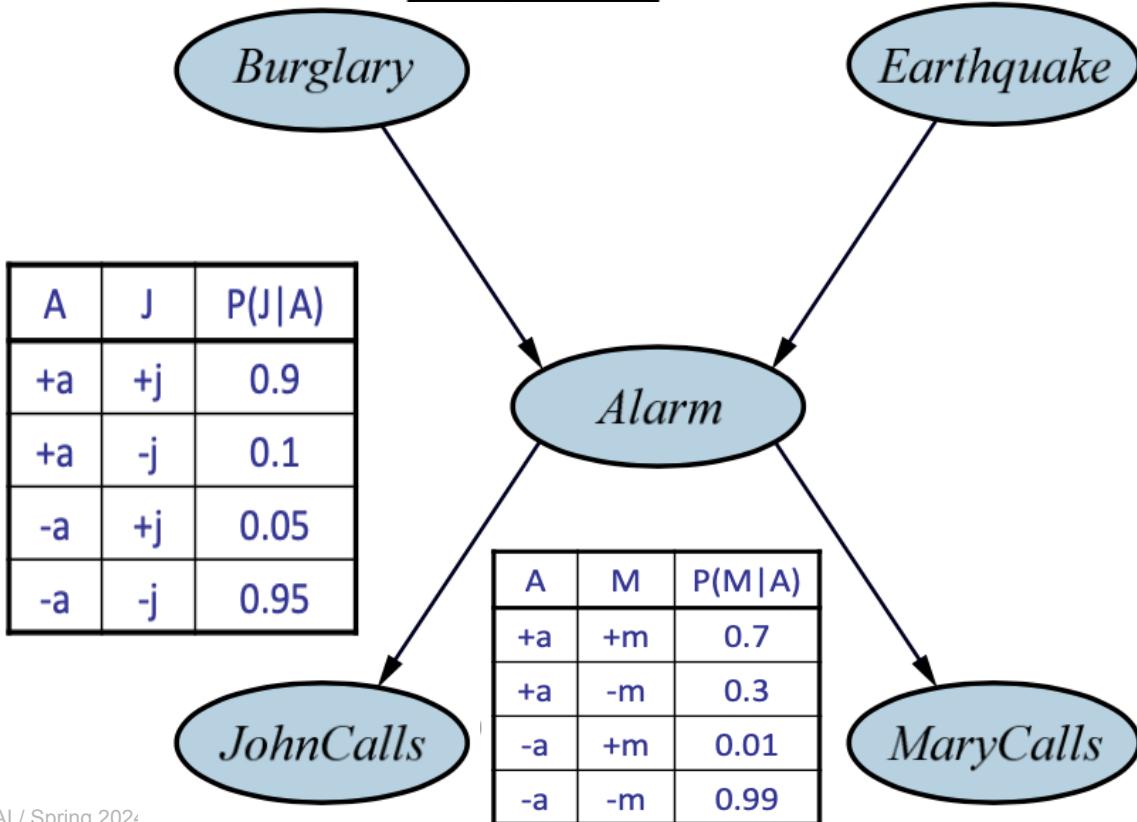


# Example

B	P(B)
+b	0.001
-b	0.999

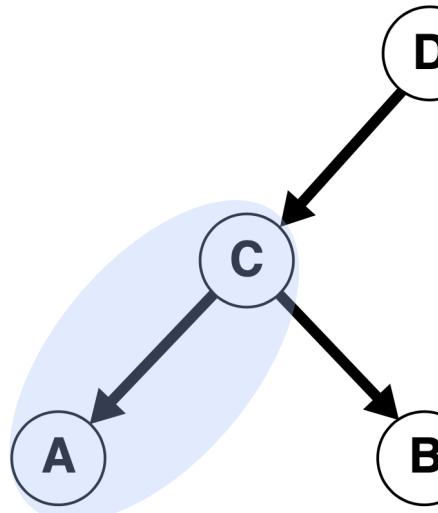
E	P(E)
+e	0.002
-e	0.998



B	E	A	P(A B,E)
+b	+e	+a	0.95
+b	+e	-a	0.05
+b	-e	+a	0.94
+b	-e	-a	0.06
-b	+e	+a	0.29
-b	+e	-a	0.71
-b	-e	+a	0.001
-b	-e	-a	0.999

# Local Markov Property

- A node in a Bayes net is **conditionally independent** of all of its non-descendants (including its ancestors), if its parents are given
  - e.g., A is conditionally independent of both B and D given C



**D is parent of C**

**A is child of C**

**B is descendant of D**

**D is ancestor of A**

# Probabilities in Bayes Nets

- Bayes nets implicitly encode joint distributions
- Given a Bayes net containing  $n$  variables,  $X_1, \dots, X_n$ , and the Bayes net defines the probability to a full assignment as

$$P(x_1, \dots, x_n) = \prod_{i=1}^n P(x_i | parents(X_i))$$

where  $parents(X_i)$  denotes the values of  $Parents(X_i)$  that appear in  $x_1, \dots, x_n$

Probabilities in Bayes Nets:  $P(x_1, \dots, x_n) = \prod_{i=1}^n P(x_i | parents(X_i))$

$\Downarrow$   $P(x_n, x_{n-1}, \dots, x_1)$  (topological ordering)

$$P(x_1, \dots, x_n) = P(x_n | x_{n-1}, \dots, x_1) P(x_{n-1}, \dots, x_1) \text{ (product rule)}$$

(chain rule)

$$= P(x_n | x_{n-1}, \dots, x_1) P(x_{n-1} | x_{n-2}, \dots, x_1) \cdots P(x_2 | x_1) P(x_1)$$

$$= \prod_{i=1}^n P(x_i | x_{i-1}, \dots, x_1)$$

(if  $Parents(X_i) \subseteq \{X_{i-1}, \dots, X_1\}$  and

$$= \prod_{i=1}^n P(x_i | parents(X_i))$$

$\{X_1, \dots, X_i\}$  is topological order of the Bayes Net )

# Conditional Independence

- **Conditional independence** of two variables A and B, given a third variable C, i.e.,  $A \perp\!\!\!\perp B | C$ , is defined as

$$P(A, B | C) = P(A | C)P(B | C) \quad P(A, B) = P(A)P(B)$$

Equivalent forms:  $P(A | B, C) = P(A | C)$  and  $P(B | A, C) = P(B | C)$

$$P(A | B) = P(A) \quad P(B | A) = P(B)$$

\* analogy

Claim:  $P(A, B | C) = P(A | C) P(B | C)$   
 $\equiv P(A | B, C) = P(A | C)$  and  $P(B | A, C) = P(B | C)$

$$P(A, B | C) = P(A | C) P(B | C)$$

$$\rightarrow \frac{P(A, B, C)}{P(C)} = P(A | C) \frac{P(B, C)}{P(C)}$$

by the def. of conditional probability:

$$P(A, B | C) = \frac{P(A, B, C)}{P(C)}$$

$$\rightarrow \frac{P(A | B, C) P(B, C)}{P(C)} = P(A | C) \frac{P(B, C)}{P(C)}$$

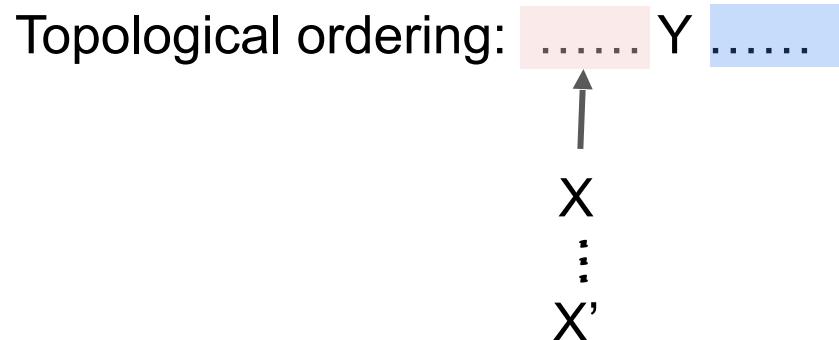
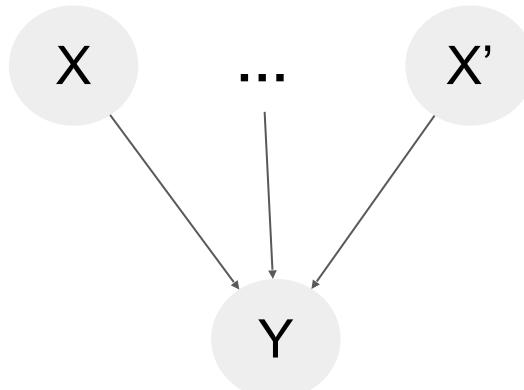
$$P(B | C) = \frac{P(B, C)}{P(C)}$$

$$\rightarrow P(A | B, C) = P(A | C)$$

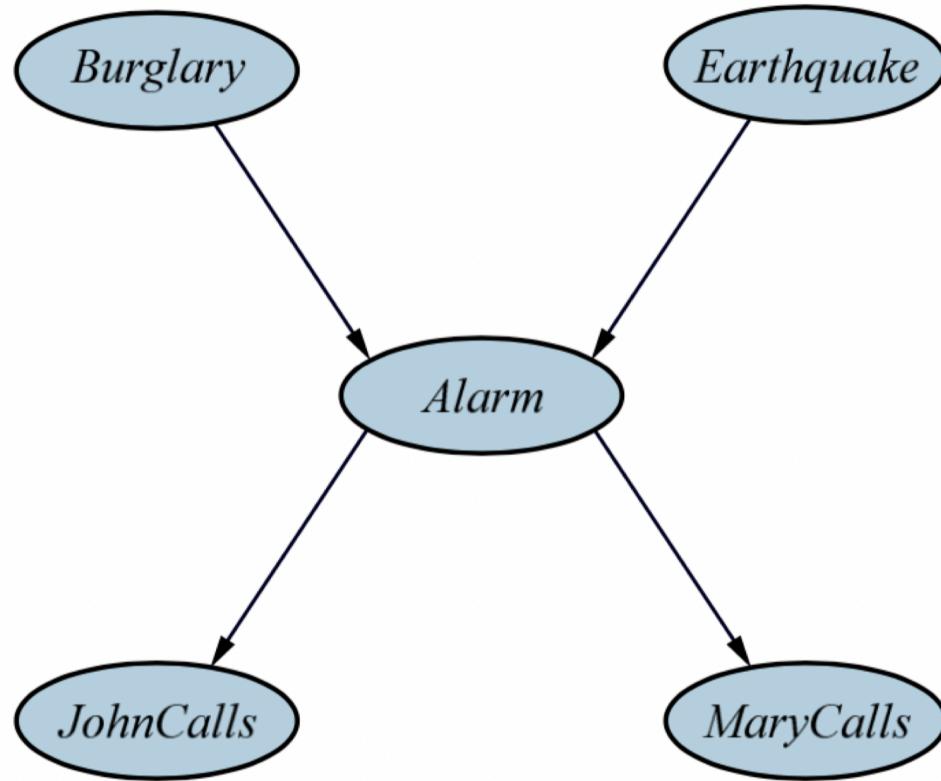
$$P(A, B, C) = P(A | B, C) P(B, C)$$

# Topological Ordering (Topological Sort)

- Given a directed acyclic graph (DAG), a topological ordering is a linear ordering of nodes such that for every directed edge  $\langle X, Y \rangle$  from node  $X$  to node  $Y$ ,  $X$  comes before  $Y$  in the ordering



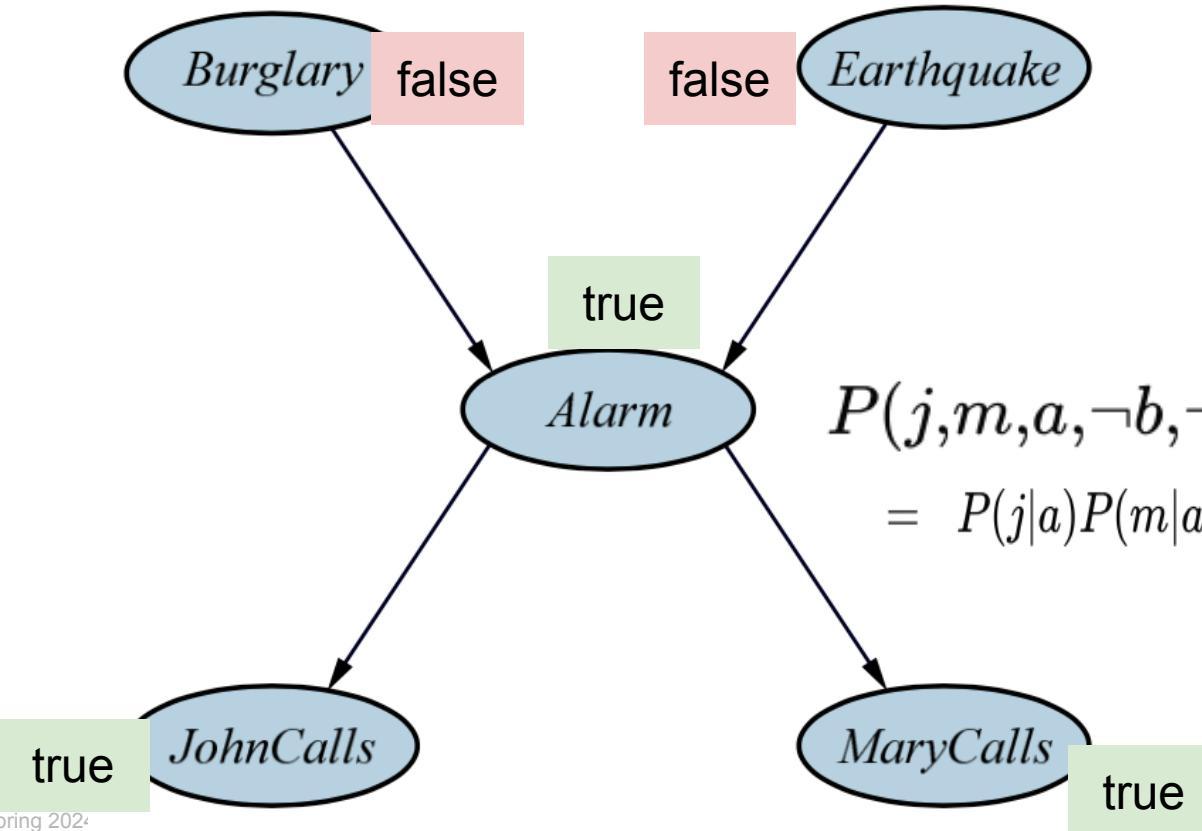
# Example: Topological Ordering



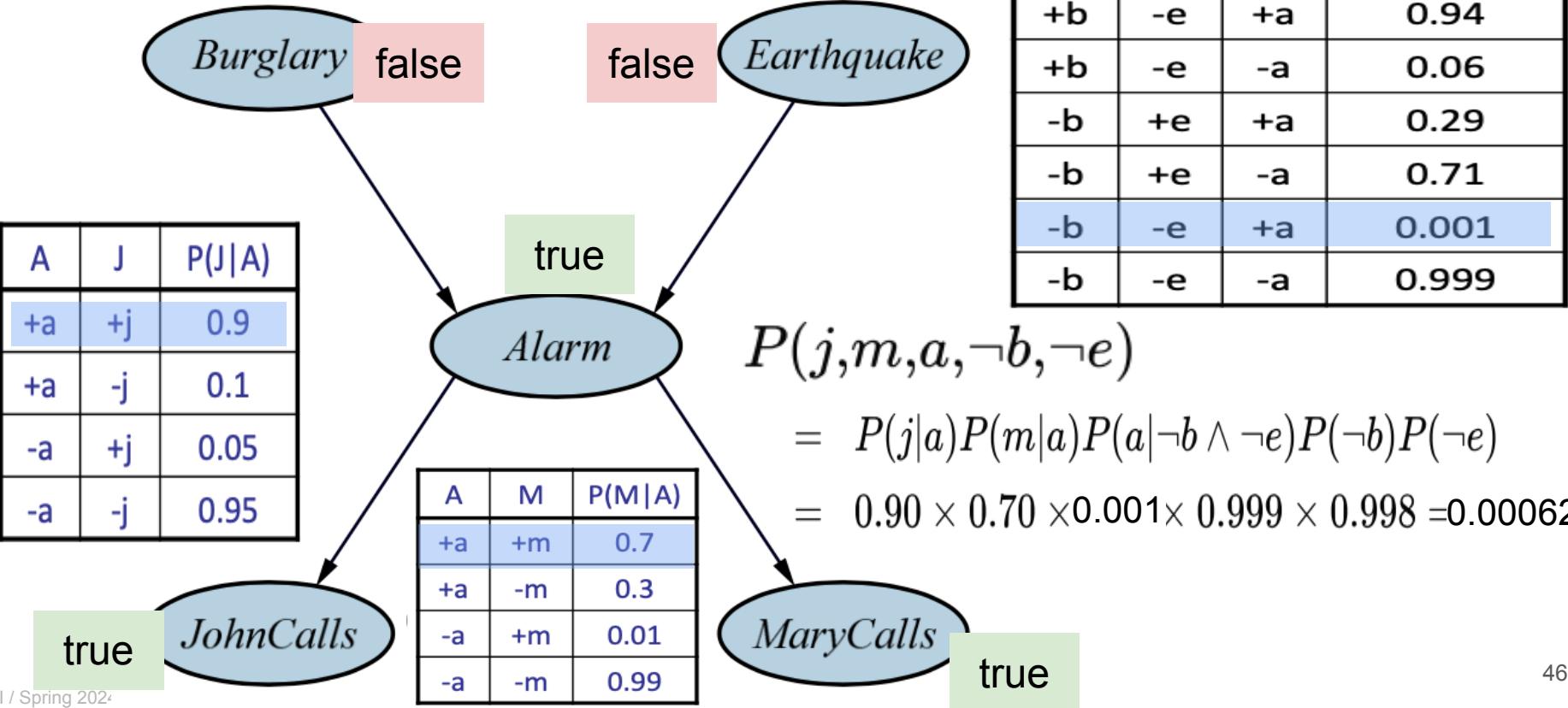
- B, E, A, J, M
- E, B, A, M, J
- ...

$$P(x_1, \dots, x_n) = \prod_{i=1}^n P(x_i | \text{parents}(X_i))$$

## Example



# Example



# Construction of Bayes Nets

- Nodes
  - First determine the set of variables that are required to model the domain
  - Now order them,  $\{X_1, \dots, X_n\}$ 
    - Any order will work
      - The resulting network will be more compact if the variables are ordered such that causes precede effects
- Links: For  $i = 1$  to  $n$  do:
  - Choose a **minimal** set  $S$  of parents for  $X_i$  from  $\{X_1, \dots, X_{i-1}\}$ , such that
$$P(X_i | X_{i-1}, \dots, X_1) = P(X_i | \text{Parents}(X_i))$$
  - For each parent insert a link from the parent to  $X_i$
  - CPTs: Write down the conditional probability table,  $P(X_i | \text{Parents}(X_i))$

# Example 1

- Node order: B, E, A, J, M
- Links:

# Example 1



- Node order: B, E, A, J, M
- Links:
  - $X_1=B$



# Example 1



- Node order: B, E, A, J, M
- Links:
  - $X_1=B$
  - $X_2=E$

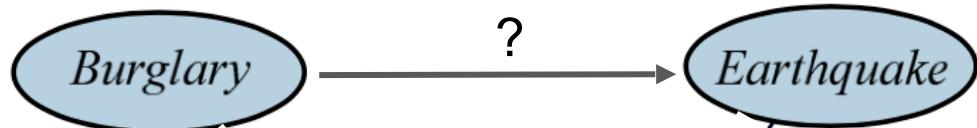
Burglary

Earthquake

# Example 1



- Node order: B, E, A, J, M
- Links:
  - $X_1=B$
  - $X_2=E$ 
    - Minimal Parents(E) = {?} \subseteq \{B\}



# Example 1



- Node order: **B**, E, A, J, M
- Links:
  - $X_1=B$
  - $X_2=E$ 
    - Minimal Parents(E) = {?} ⊆ \{B\}
    - Check  $B \perp\!\!\!\perp E$ ?  
by  $P(B,E) = P(B)P(E)$



# Example 1



- Node order: **B**, E, A, J, M
- Links:
  - $X_1=B$
  - $X_2=E$ 
    - Minimal Parents(E) = {?} ⊆ \{B\}
    - Check  $B \perp\!\!\!\perp E$ ?  
by  $P(B,E) = P(B)P(E)$

*Burglary*

*Earthquake*

# Example 1



- Node order: B, E, A, J, M
- Links:
  - $X_1=B$
  - $X_2=E$ 
    - Minimal Parents(E) = {?}  $\subseteq \{B\}$
    - Check  $B \perp\!\!\!\perp E$  ?  
by  $P(B,E) = P(B)P(E)$
  - $X_3=A$

*Burglary*

*Earthquake*

*Alarm*

# Example 1



- Node order: B, E, A, J, M
- Links:
  - $X_1 = B$
  - $X_2 = E$ 
    - Minimal Parents(E) = {?}  $\subseteq \{B\}$
    - Check  $B \perp\!\!\!\perp E$  ?  
by  $P(B,E) = P(B)P(E)$
  - $X_3 = A$ 
    - Minimal Parents(A) = {?}  $\subseteq \{E, B\}$

Burglary

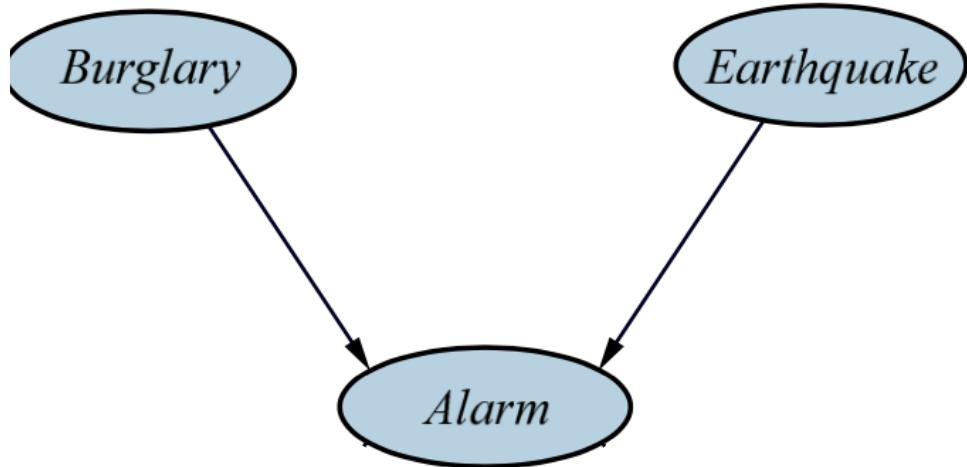
Earthquake

Alarm

# Example 1



- Node order: **B, E**, A, J, M
- Links:
  - $X_1=B$
  - $X_2=E$ 
    - Minimal Parents(E) = {?}  $\subseteq \{B\}$
    - Check  $B \perp\!\!\!\perp E$  ?  
by  $P(B,E) = P(B)P(E)$
  - $X_3=A$ 
    - Minimal Parents(A)= {?}  $\subseteq \{E,B\}$



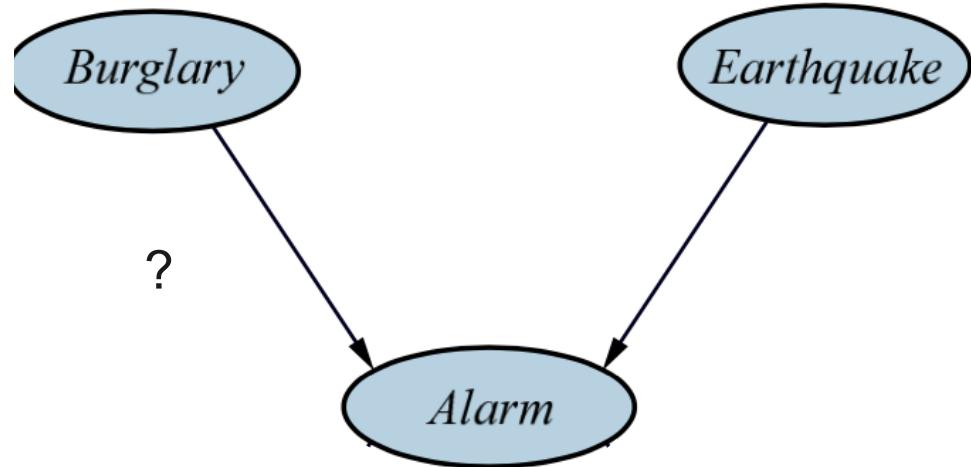
# Example 1



- Node order: B, E, A, J, M

- Links:

- $X_1 = B$ 
    - Minimal Parents(E) = {?} \subseteq \{B\}
    - Check  $B \perp\!\!\!\perp E$  ?  
by  $P(B, E) = P(B)P(E)$
  - $X_2 = E$ 
    - Minimal Parents(A) = {?} \subseteq \{E, B\}
    - Check  $A \perp\!\!\!\perp B | E$  ? by  $P(A, B | E) = P(A|E)P(B|E)$
  - $X_3 = A$



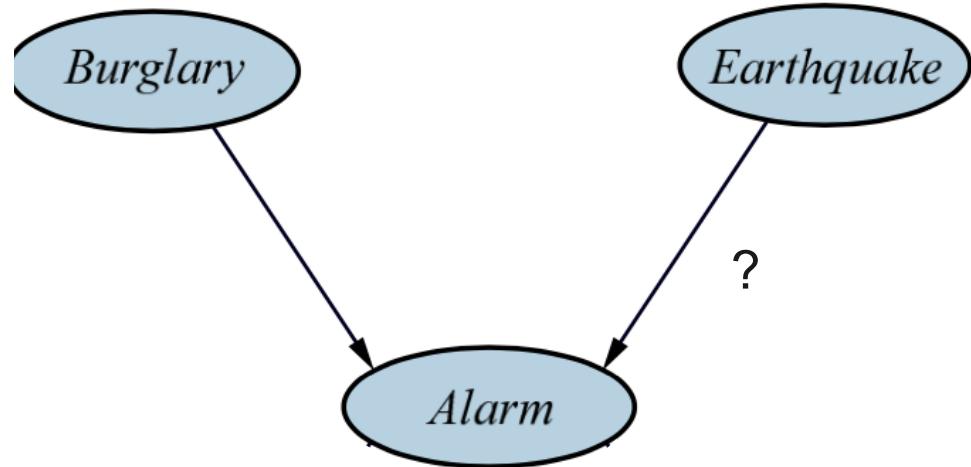
# Example 1



- Node order: **B, E, A, J, M**

- Links:

- $X_1=B$ 
    - Minimal Parents(E) = {?}  $\subseteq \{B\}$
    - Check  $B \perp\!\!\!\perp E$  ?  
by  $P(B,E) = P(B)P(E)$
  - $X_2=E$ 
    - Minimal Parents(A)= {?}  $\subseteq \{E,B\}$
    - Check  $A \perp\!\!\!\perp B | E$  ? by  $P(A,B | E) = P(A|E)P(B|E)$
    - Check  $A \perp\!\!\!\perp E | B$  ? by  $P(A,E | B) = P(A|B)P(E|B)$
  - $X_3=A$



# Example 1



- Node order: B, E, A, J, M

- Links:

- $X_1 = B$
  - $X_2 = E$

- Minimal Parents(E) = {?}  $\subseteq \{B\}$

- Check  $B \perp\!\!\!\perp E$  ?

- by  $P(B, E) = P(B)P(E)$

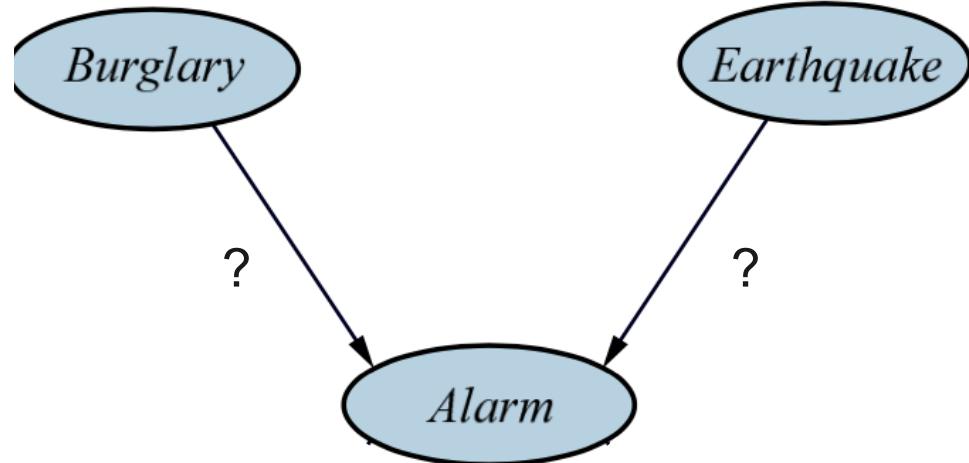
- $X_3 = A$

- Minimal Parents(A) = {?}  $\subseteq \{E, B\}$

- Check  $A \perp\!\!\!\perp B | E$  ? by  $P(A, B | E) = P(A|E)P(B|E)$

- Check  $A \perp\!\!\!\perp E | B$  ? by  $P(A, E | B) = P(A|B)P(E|B)$

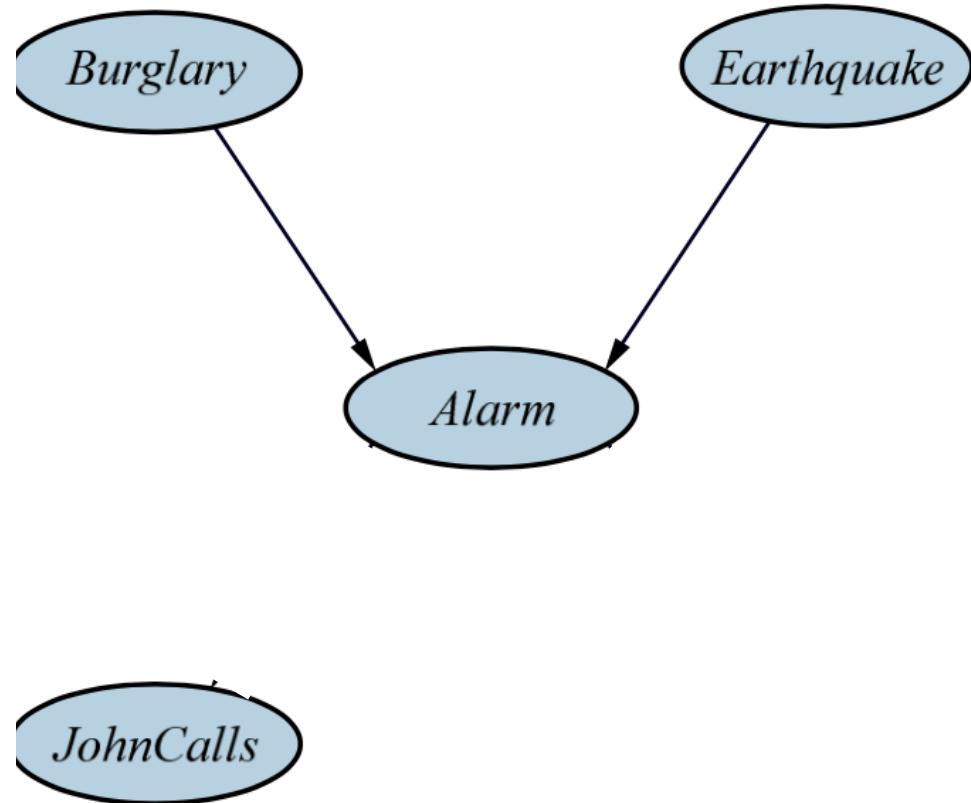
- Check  $A \perp\!\!\!\perp (E, B)$  ? by  $P(A, E, B) = P(A)P(E, B)$



# Example 1

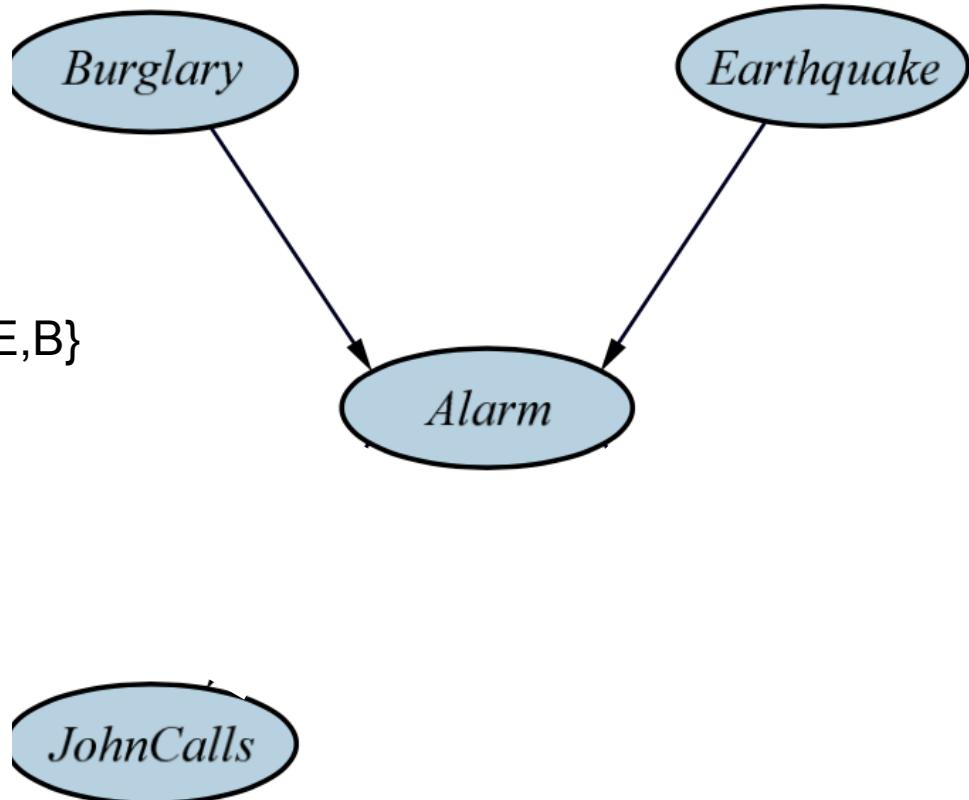


- Node order: B, E, A, J, M
- Links:
  - $X_4=J$



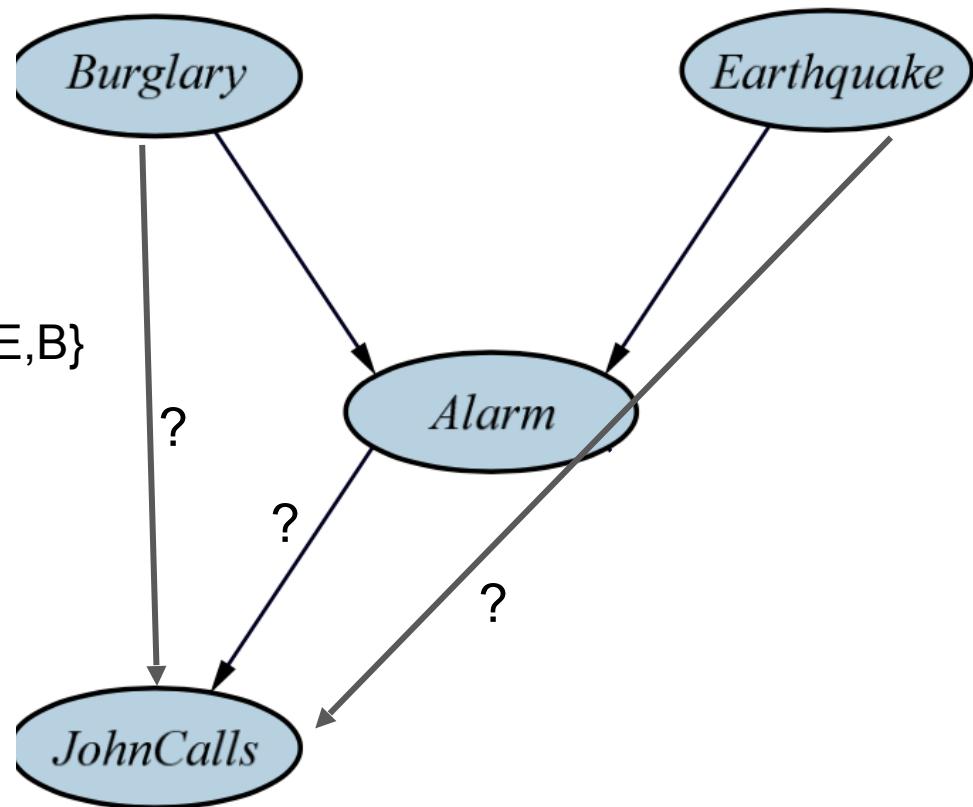
# Example 1

- Node order: B, E, A, J, M
- Links:
  - $X_4 = J$ 
    - Minimal Parents(J) = {?} \subseteq \{A, E, B\}



# Example 1

- Node order: B, E, A, J, M
- Links:
  - $X_4 = J$ 
    - Minimal Parents(J) = {?} \subseteq \{A, E, B\}

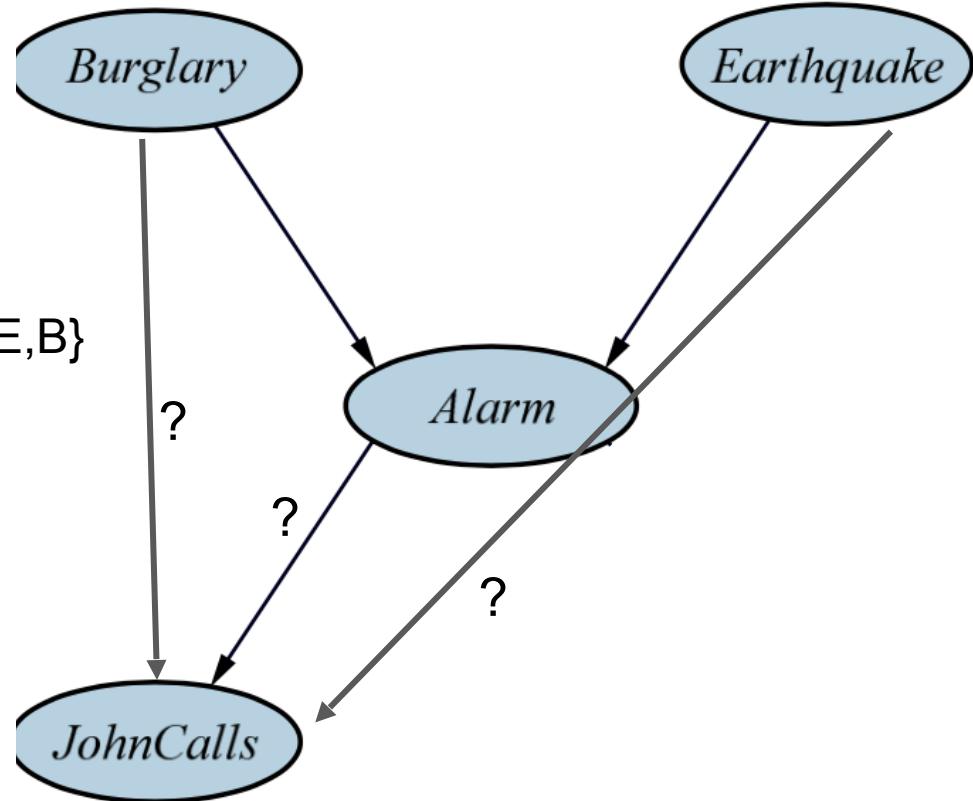


# Example 1

- Node order: B, E, A, J, M
- Links:

○  $X_4 = J$

- Minimal Parents(J) = {?}  $\subseteq \{A, E, B\}$
- Check  $J \perp\!\!\!\perp A | (B, E)$  ?
- Check  $J \perp\!\!\!\perp B | (A, E)$  ?
- Check  $J \perp\!\!\!\perp E | (A, B)$  ?
- Check  $J \perp\!\!\!\perp (B, E) | A$  ?
- Check  $J \perp\!\!\!\perp (A, E) | B$  ?
- Check  $J \perp\!\!\!\perp (A, B) | E$  ?
- Check  $J \perp\!\!\!\perp (A, E, B)$  ?



# Example 1

- Node order: B, E, A, J, M
- Links:

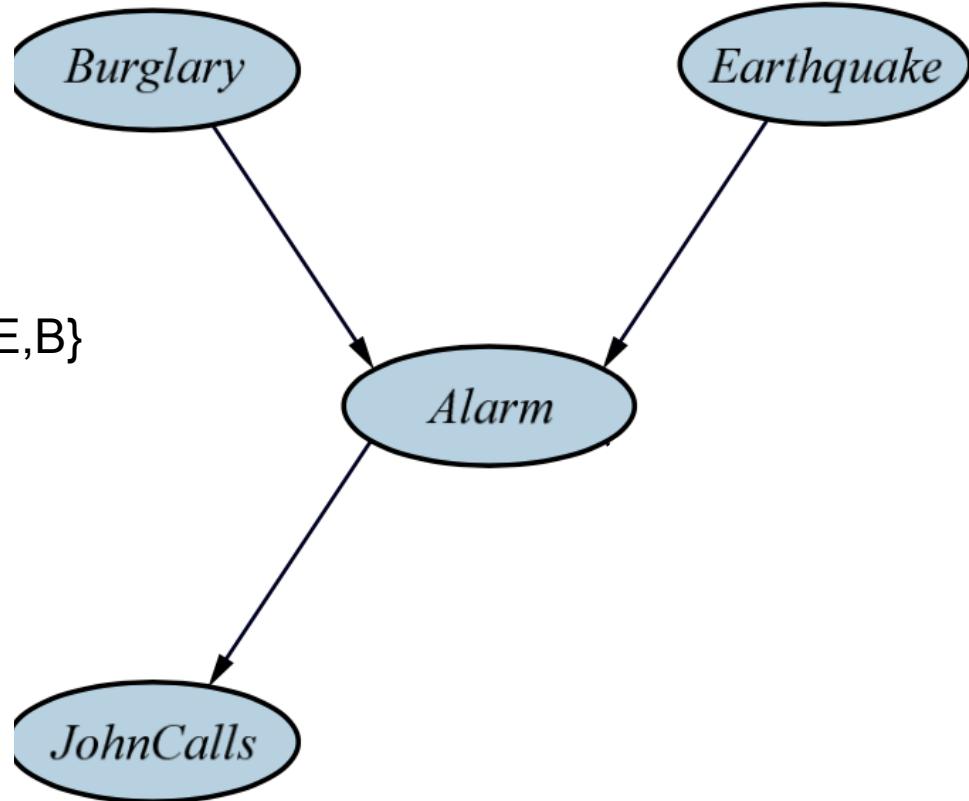
$$X_4 = J$$

- Minimal Parents(J) = {?}  $\subseteq \{A, E, B\}$
- Check  $J \perp\!\!\!\perp A | (B, E)$  ?
- Check  $J \perp\!\!\!\perp B | (A, E)$  ?
- Check  $J \perp\!\!\!\perp E | (A, B)$  ?
- Check  $J \perp\!\!\!\perp (B, E) | A$  ?
- Check  $J \perp\!\!\!\perp (A, E) | B$  ?
- Check  $J \perp\!\!\!\perp (A, B) | E$  ?
- Check  $J \perp\!\!\!\perp (A, E, B)$  ?

$$C_1^3 = 3$$

$$C_2^3 = 3$$

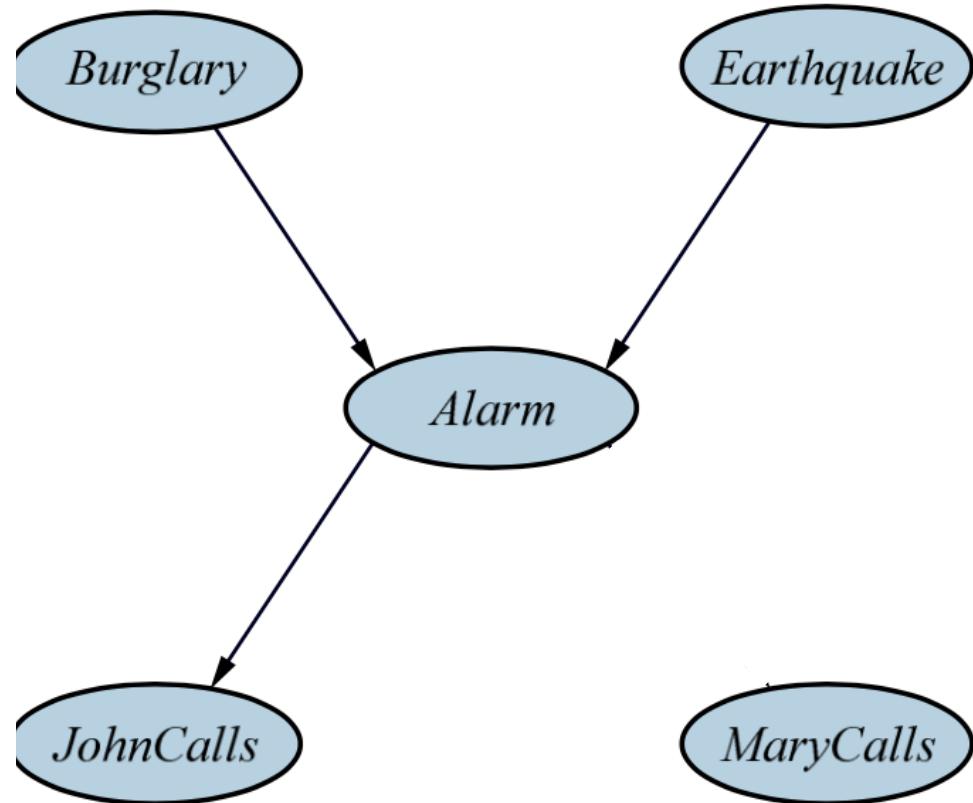
$$C_3^3 = 1$$



# Example 1

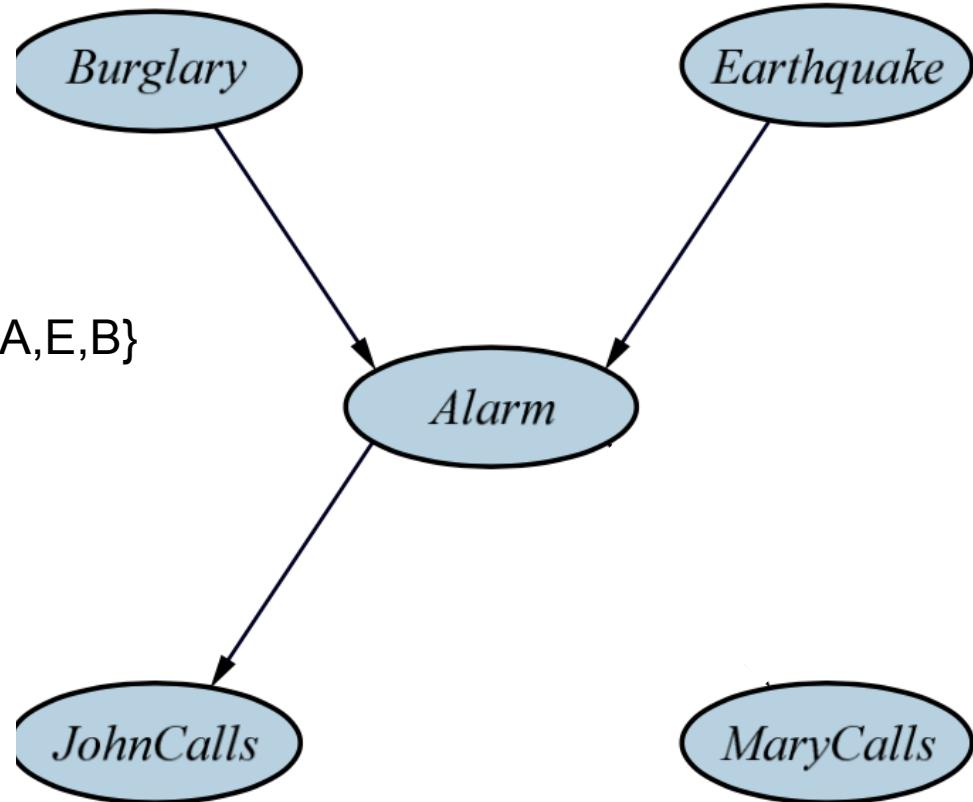


- Node order: B, E, A, J, M
- Links:
  - $X_5 = M$



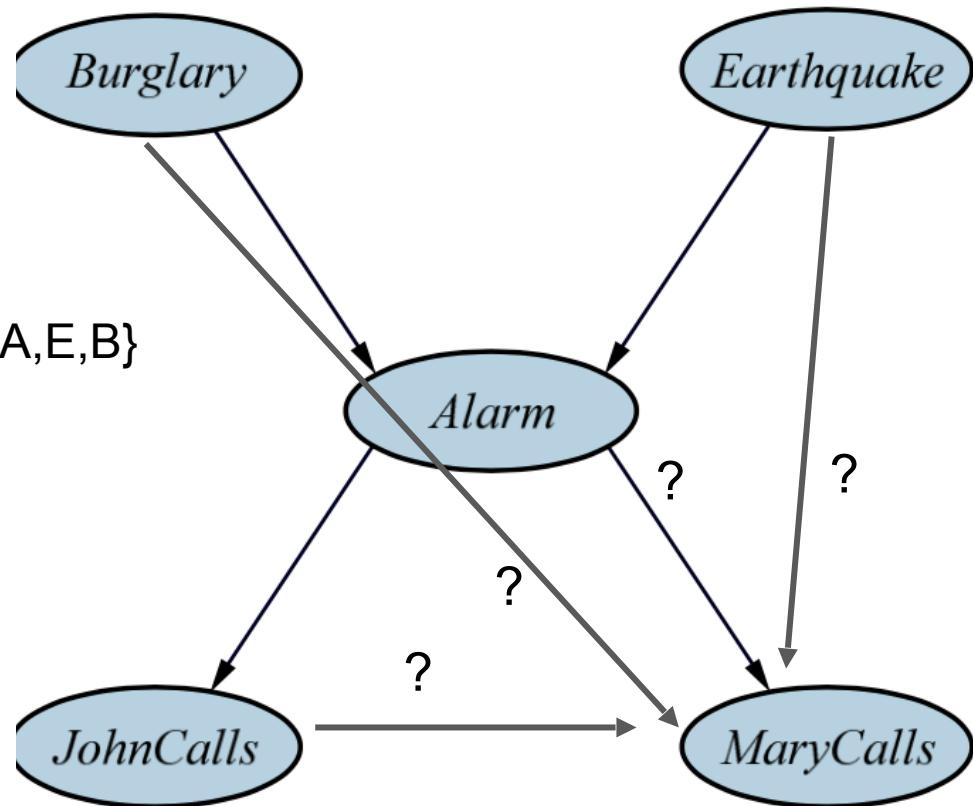
# Example 1

- Node order: B, E, A, J, M
- Links:
  - $X_5 = M$ 
    - Minimal Parents(M) = {?}  $\subseteq \{J, A, E, B\}$



# Example 1

- Node order: B, E, A, J, M
- Links:
  - $X_5 = M$ 
    - Minimal Parents(M) = {?} \subseteq \{J, A, E, B\}



# Example 1

- Node order: B, E, A, J, M
- Links:

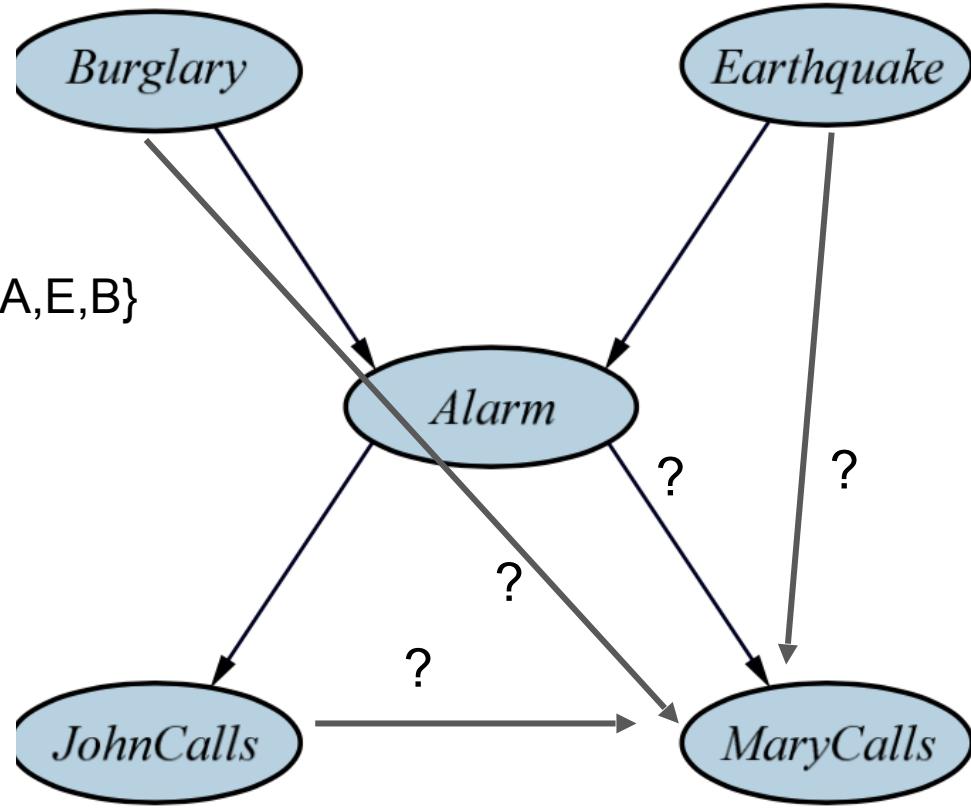
$$X_5 = M$$

■ Minimal Parents(M) = {?}  $\subseteq \{J, A, E, B\}$

- Check  $M \perp\!\!\!\perp A | (B, E, J)$  ?
- Check  $M \perp\!\!\!\perp B | (A, E, J)$  ?
- Check  $M \perp\!\!\!\perp E | (A, B, J)$  ?
- Check  $M \perp\!\!\!\perp J | (A, B, E)$  ?
- Check  $M \perp\!\!\!\perp (B, E) | (A, J)$  ?
- Check  $M \perp\!\!\!\perp (B, A) | (E, J)$  ?
- Check  $M \perp\!\!\!\perp (B, J) | (E, A)$  ?
- Check  $M \perp\!\!\!\perp (E, A) | (B, J)$  ?
- Check  $M \perp\!\!\!\perp (E, J) | (B, A)$  ?
- Check  $M \perp\!\!\!\perp (A, J) | (B, E)$  ?

$$C_1^4 = 4$$

$$C_2^4 = 6$$



# Example 1



- Node order: B, E, A, J, M
- Links:

$$X_5 = M$$

- Minimal Parents(M) = {?}  $\subseteq \{J, A, E, B\}$

- ...

- Check  $M \perp\!\!\!\perp (B, E, J) | A$  ?

- Check  $M \perp\!\!\!\perp (A, E, J) | B$  ?

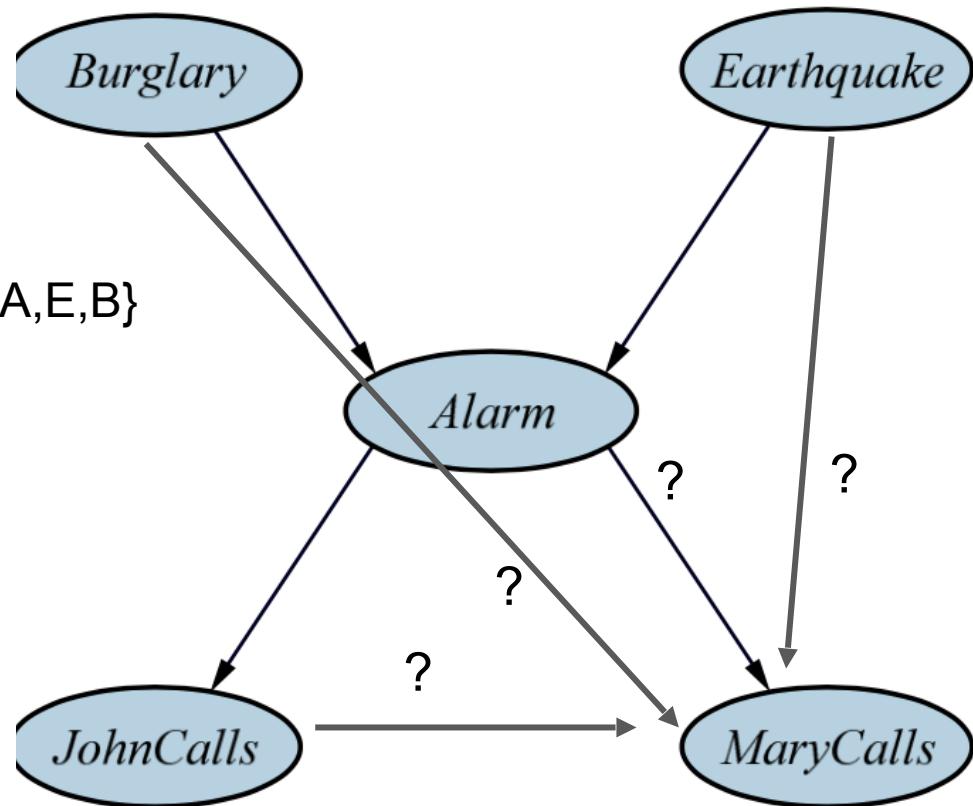
- Check  $M \perp\!\!\!\perp (A, B, J) | E$  ?

- Check  $M \perp\!\!\!\perp (A, B, E) | J$  ?

- Check  $M \perp\!\!\!\perp (J, A, E, B)$  ?

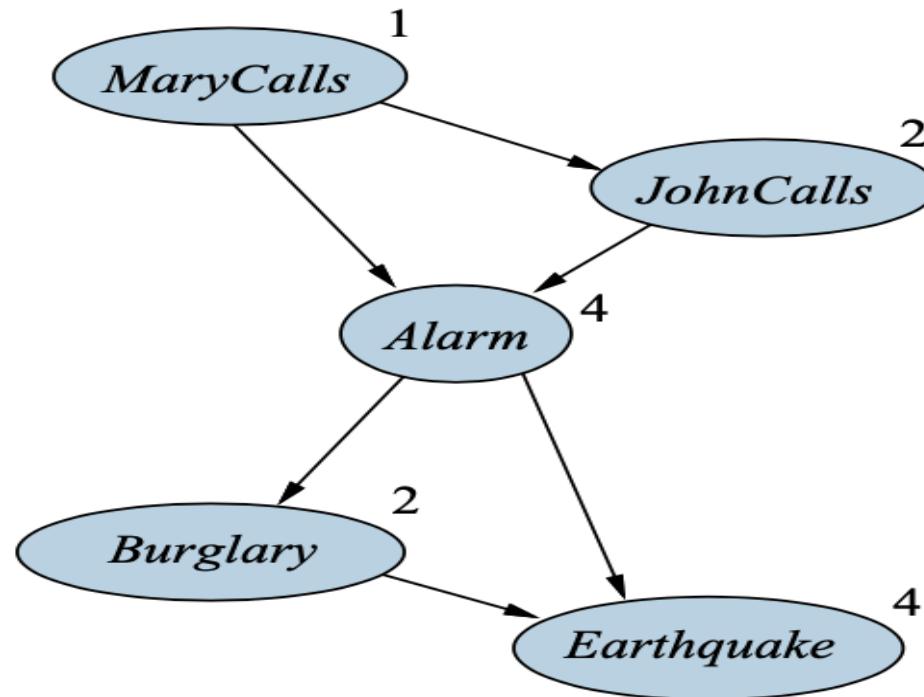
$$C_5^4 = 4$$

$$C_4^4 = 1$$



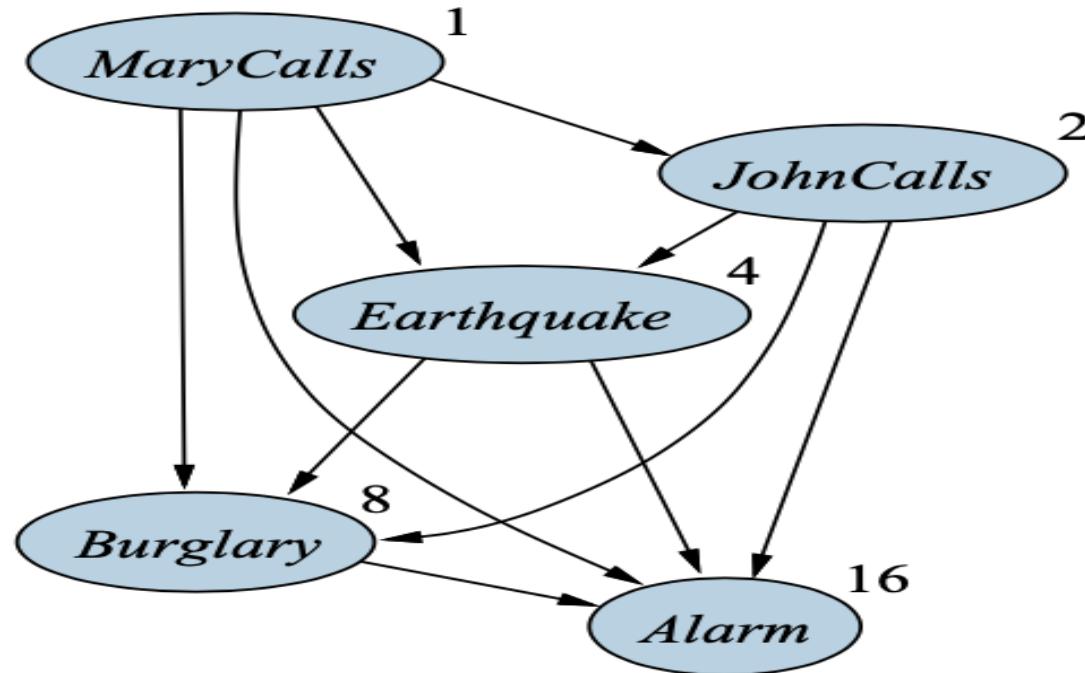
## Example 2

- Node order: M, J, A, B, E



## Example 3

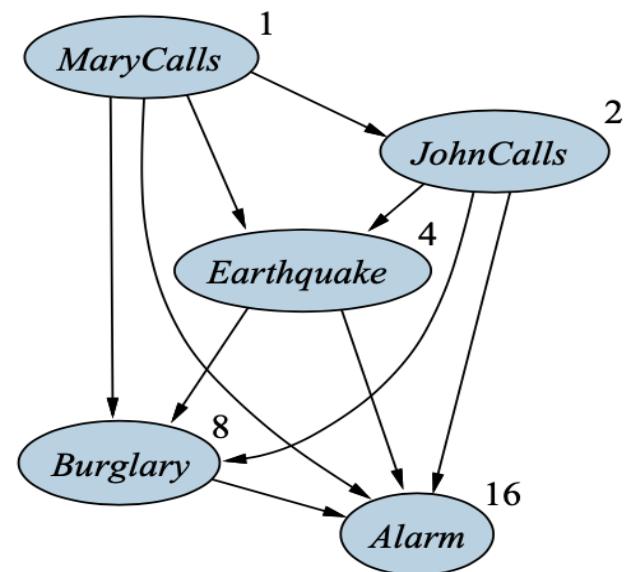
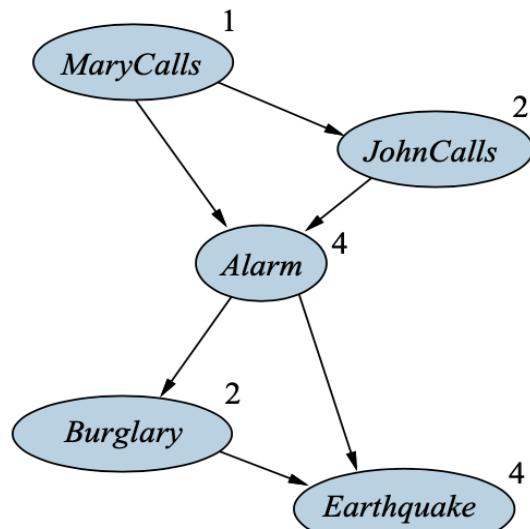
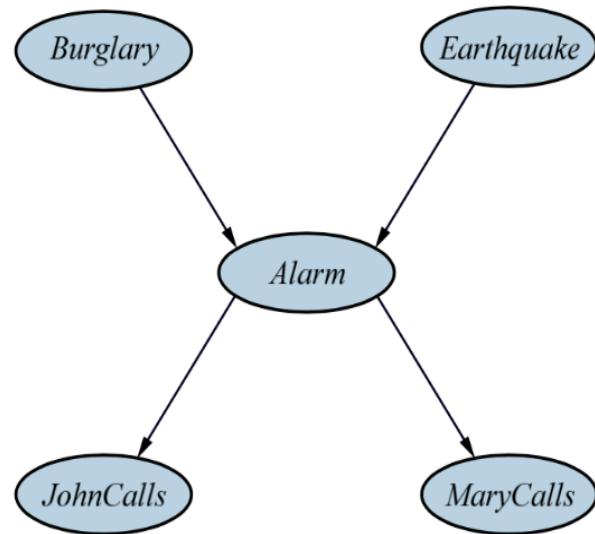
- Node order: M, J, E, B, A



# Construction of Bayes Nets

- Nodes
  - First determine the set of variables that are required to model the domain.
  - Now order them,  $\{X_1, \dots, X_n\}$ 
    - Any order will work, but the resulting network will be more compact if the variables are ordered such that causes precede effects
- Links: For  $i = 1$  to  $n$  do:
  - Choose a minimal set  $S$  of parents for  $X_i$  from  $\{X_1, \dots, X_{i-1}\}$ , such that
$$P(X_i | X_{i-1}, \dots, X_1) = P(X_i | \text{Parents}(X_i))$$
  - For each parent insert a link from the parent to  $X_i$
  - CPTs: Write down the conditional probability table,  $P(X_i | \text{Parents}(X_i))$

# Compactness and Node Ordering



compact  $\rightarrow$  ideal

# Compactness and Node Ordering

- Compactness
  - More compact than the full joint distribution
  - Example
    - 30 nodes (boolean)
    - Each node has five parents
    - Bayes net requires  $30 \times 2^5 = 960$  numbers

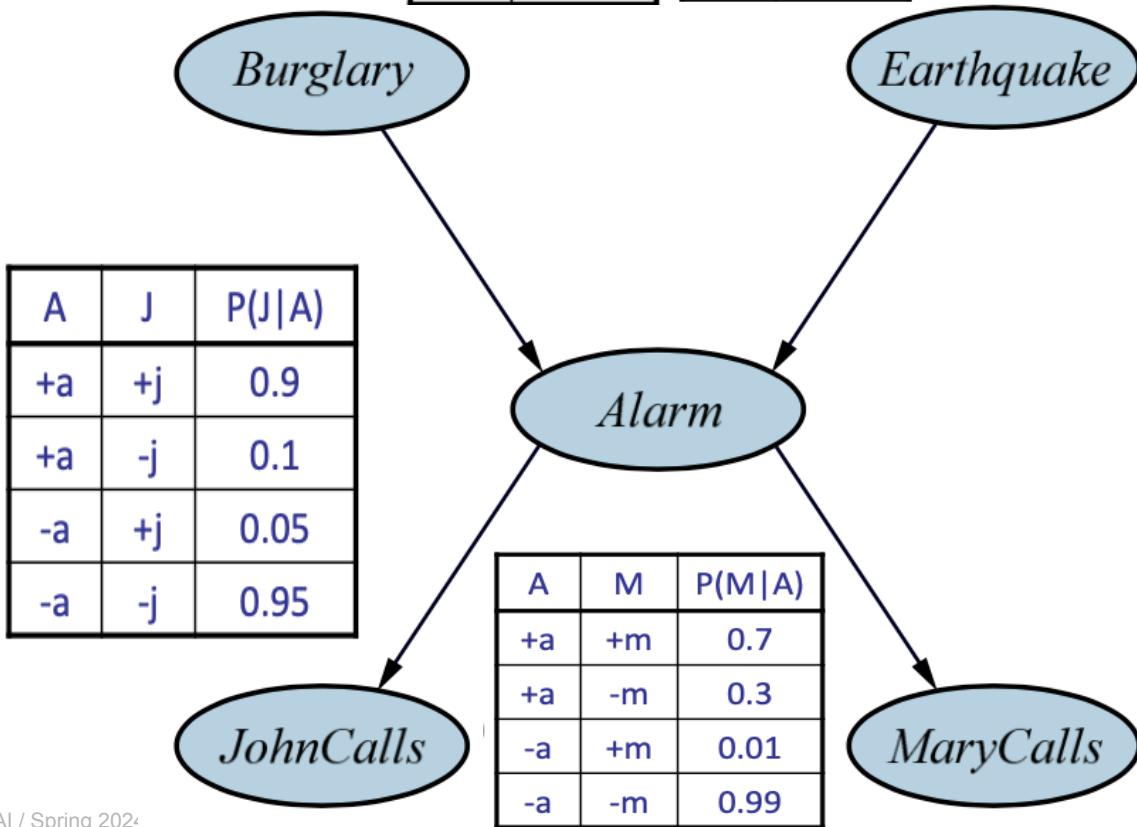
# Example

B	P(B)
+b	0.001
-b	0.999

E	P(E)
+e	0.002
-e	0.998

B	E	A	P(A B,E)
+b	+e	+a	0.95
+b	+e	-a	0.05
+b	-e	+a	0.94
+b	-e	-a	0.06
-b	+e	+a	0.29
-b	+e	-a	0.71
-b	-e	+a	0.001
-b	-e	-a	0.999

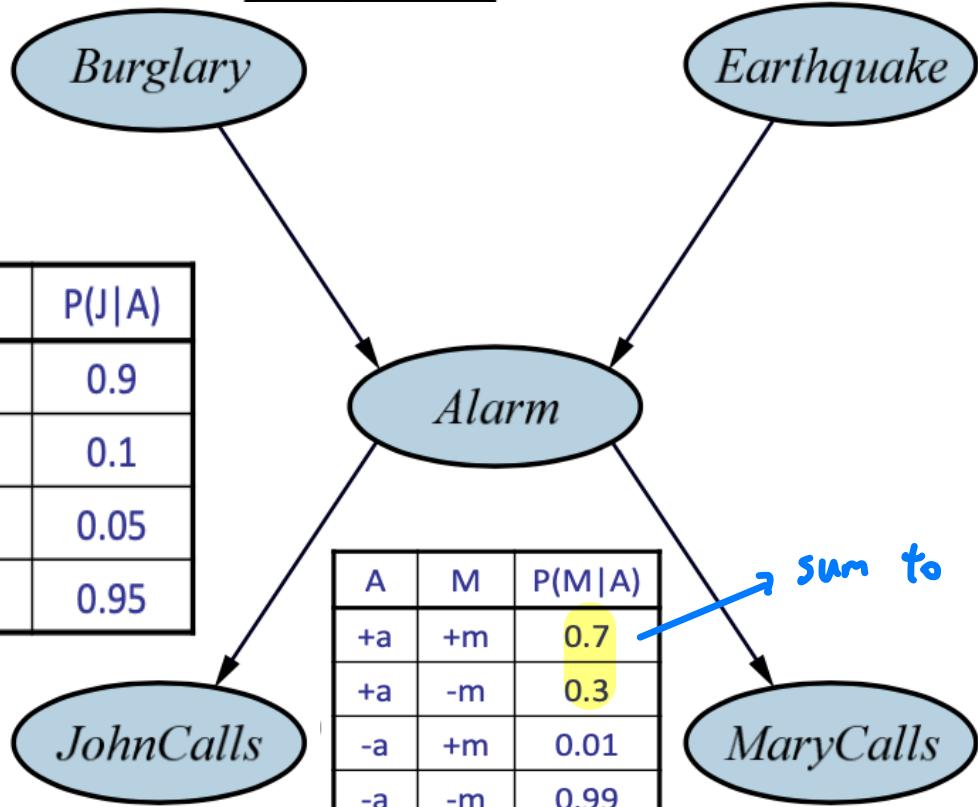


# Example

B	P(B)
+b	0.001
-b	0.999

E	P(E)
+e	0.002
-e	0.998

B	E	A	P(A B,E)
+b	+e	+a	0.95
+b	+e	-a	0.05
+b	-e	+a	0.94
+b	-e	-a	0.06
-b	+e	+a	0.29
-b	+e	-a	0.71
-b	-e	+a	0.001
-b	-e	-a	0.999



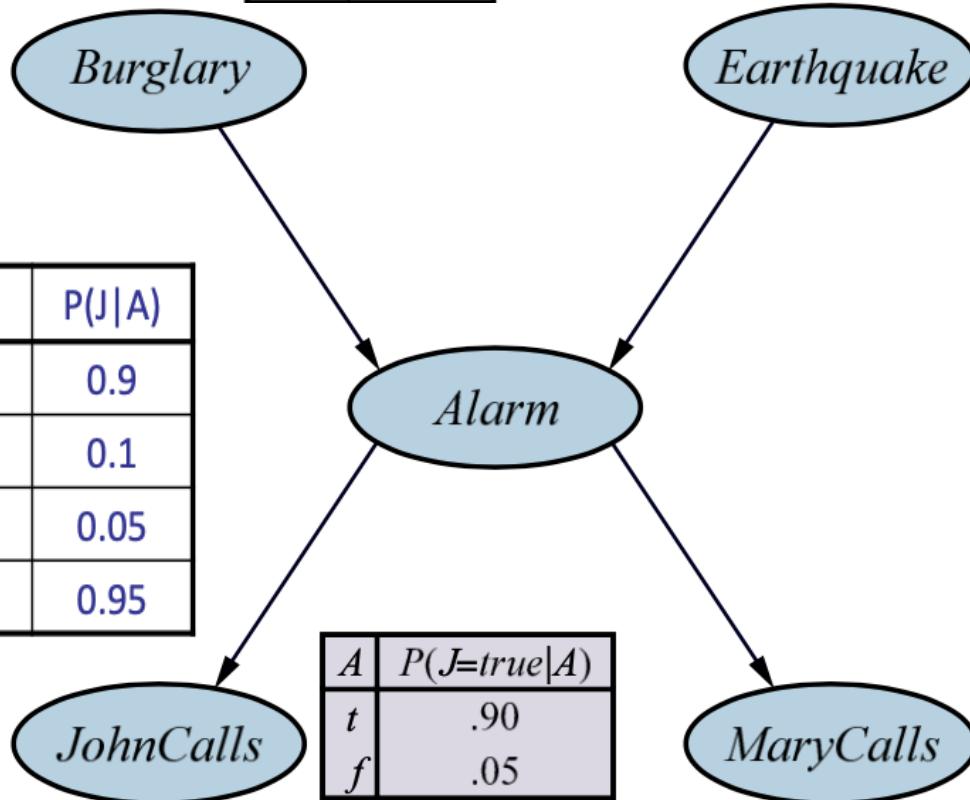
A	$P(M=\text{true} A)$
t	.70
f	.01

# Example

B	P(B)
+b	0.001
-b	0.999

E	P(E)
+e	0.002
-e	0.998

B	E	A	P(A B,E)
+b	+e	+a	0.95
+b	+e	-a	0.05
+b	-e	+a	0.94
+b	-e	-a	0.06
-b	+e	+a	0.29
-b	+e	-a	0.71
-b	-e	+a	0.001
-b	-e	-a	0.999

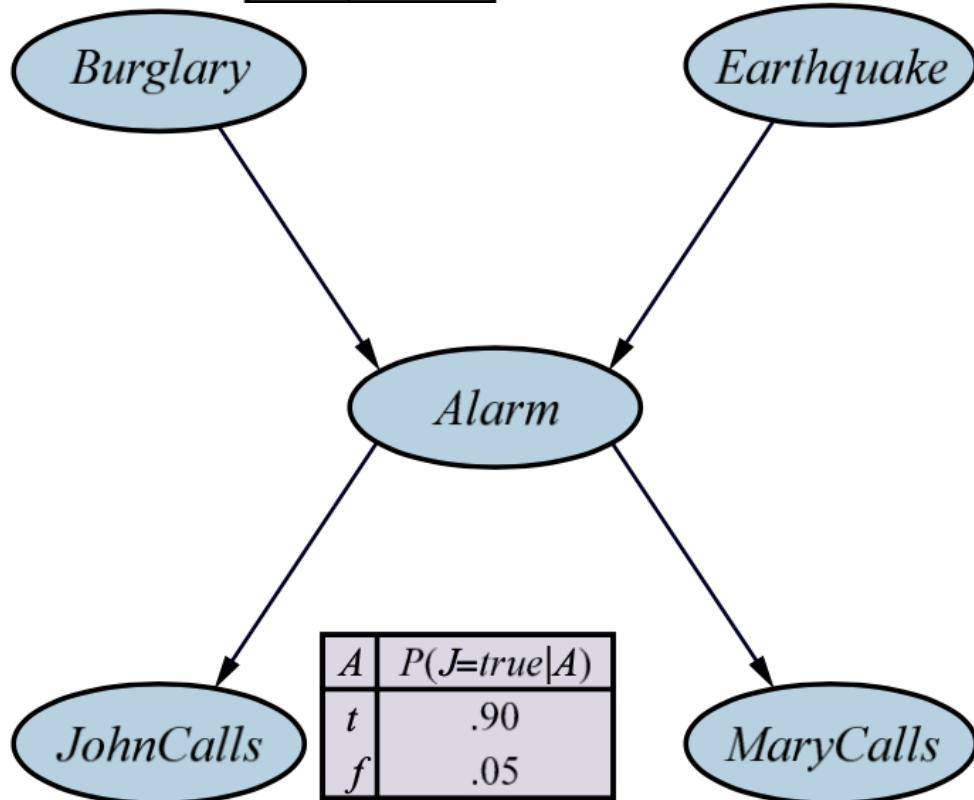


# Example

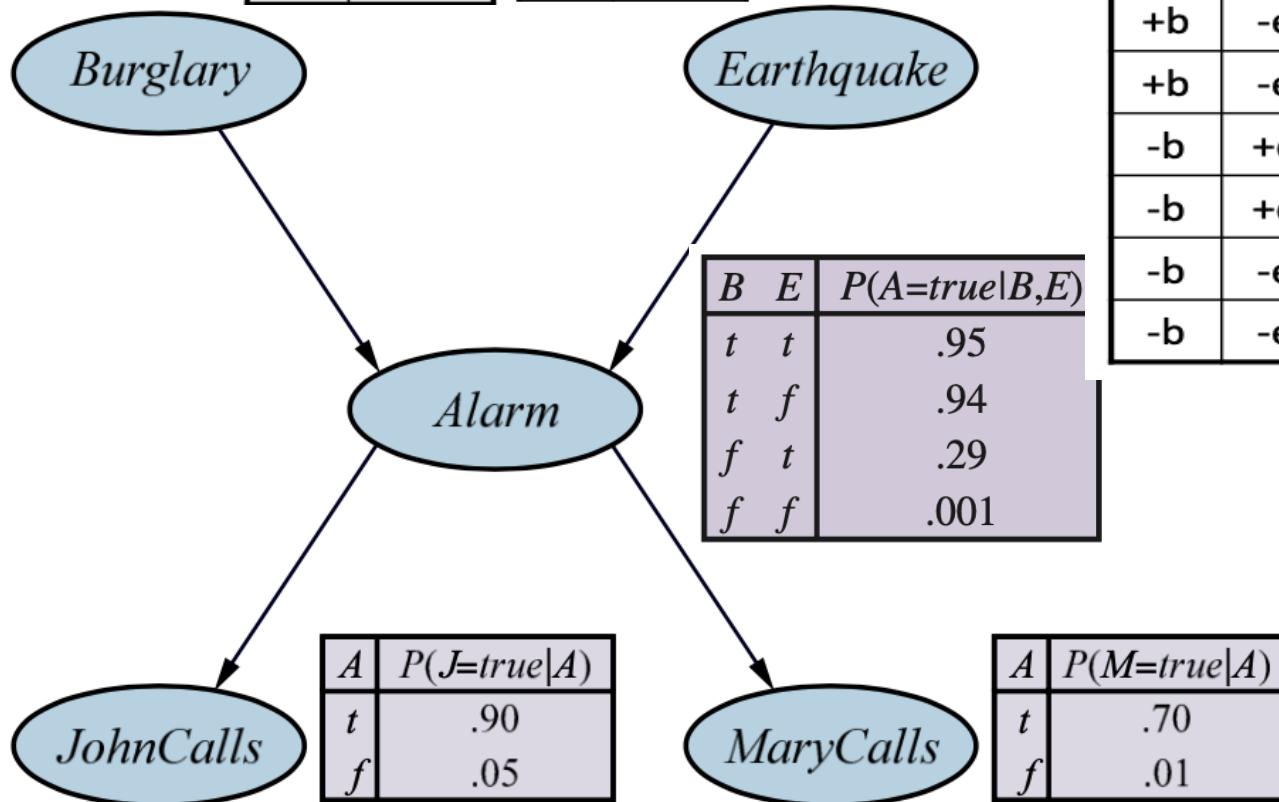
B	P(B)
+b	0.001
-b	0.999

E	P(E)
+e	0.002
-e	0.998

B	E	A	P(A B,E)
+b	+e	+a	0.95
+b	+e	-a	0.05
+b	-e	+a	0.94
+b	-e	-a	0.06
-b	+e	+a	0.29
-b	+e	-a	0.71
-b	-e	+a	0.001
-b	-e	-a	0.999



# Example

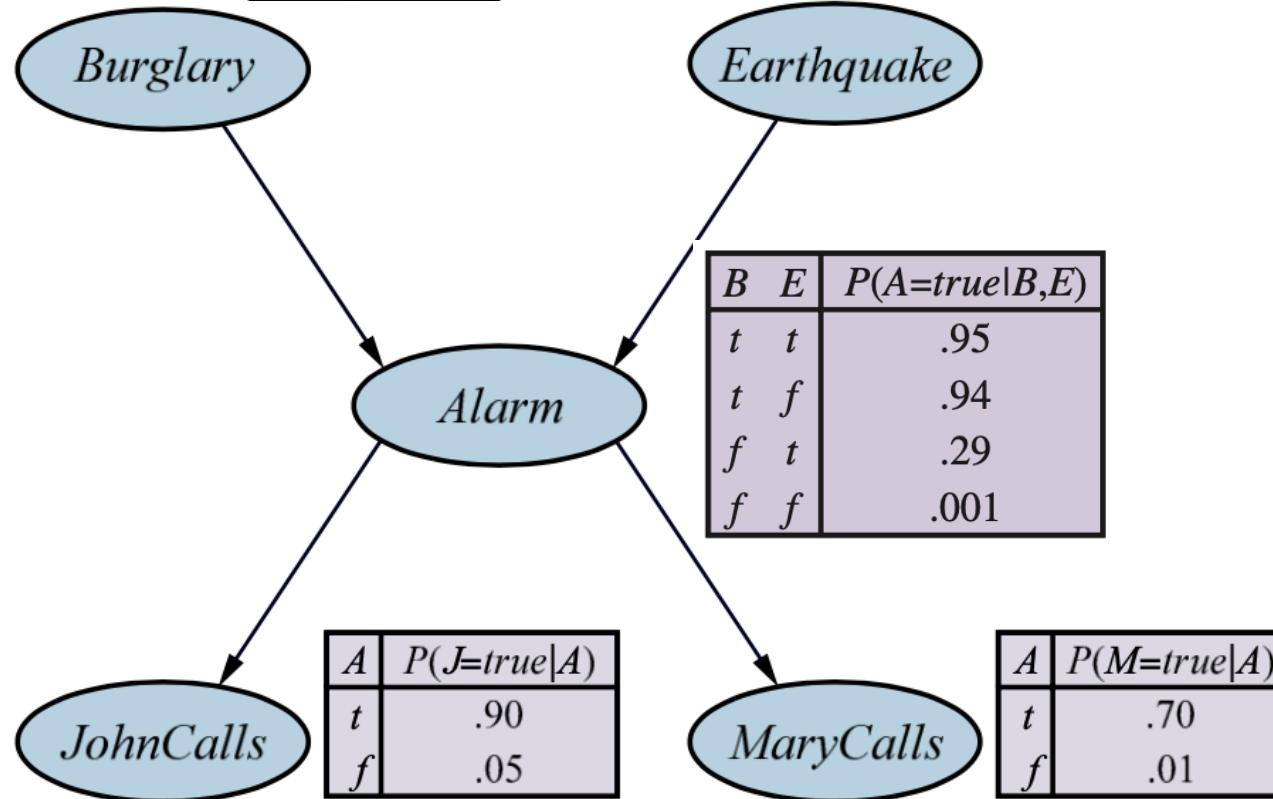


B	E	A	P(A B,E)
+b	+e	+a	0.95
+b	+e	-a	0.05
+b	-e	+a	0.94
+b	-e	-a	0.06
-b	+e	+a	0.29
-b	+e	-a	0.71
-b	-e	+a	0.001
-b	-e	-a	0.999

# Example

B	P(B)
+b	0.001
-b	0.999

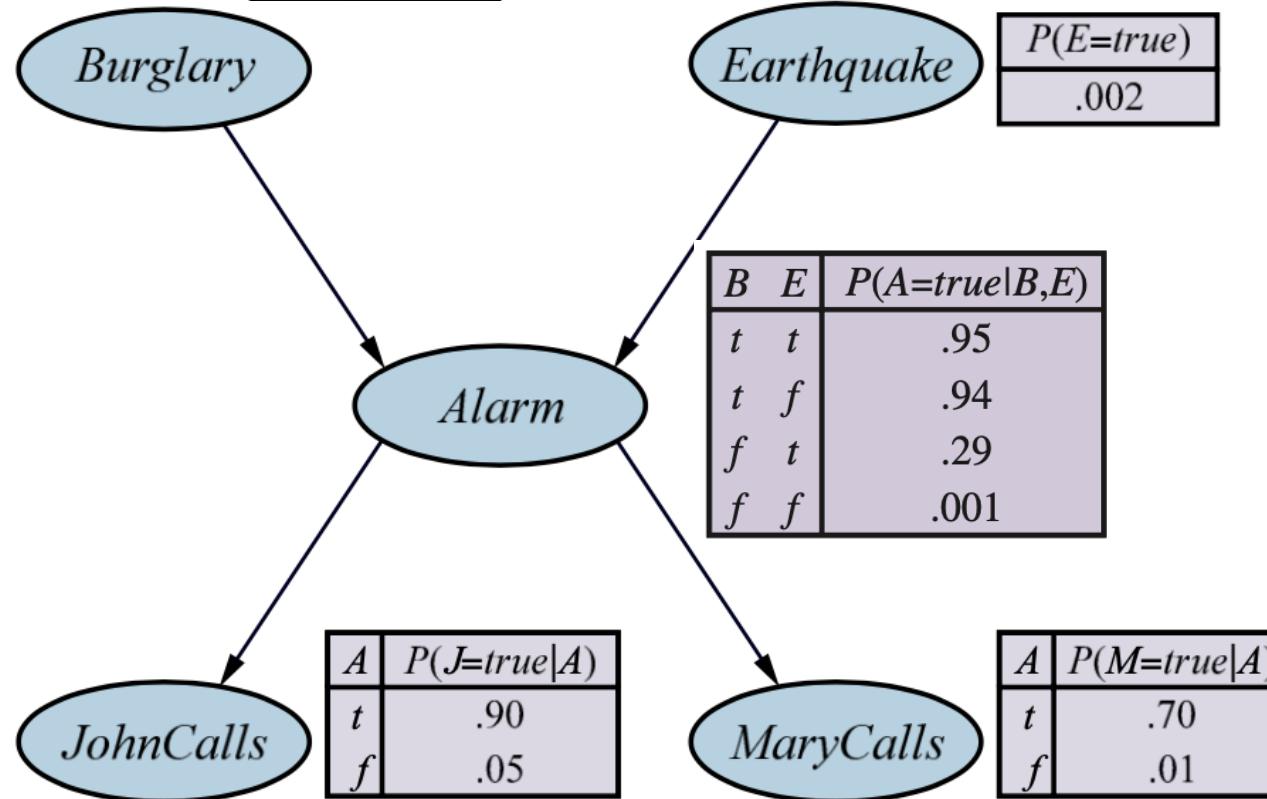
E	P(E)
+e	0.002
-e	0.998



# Example

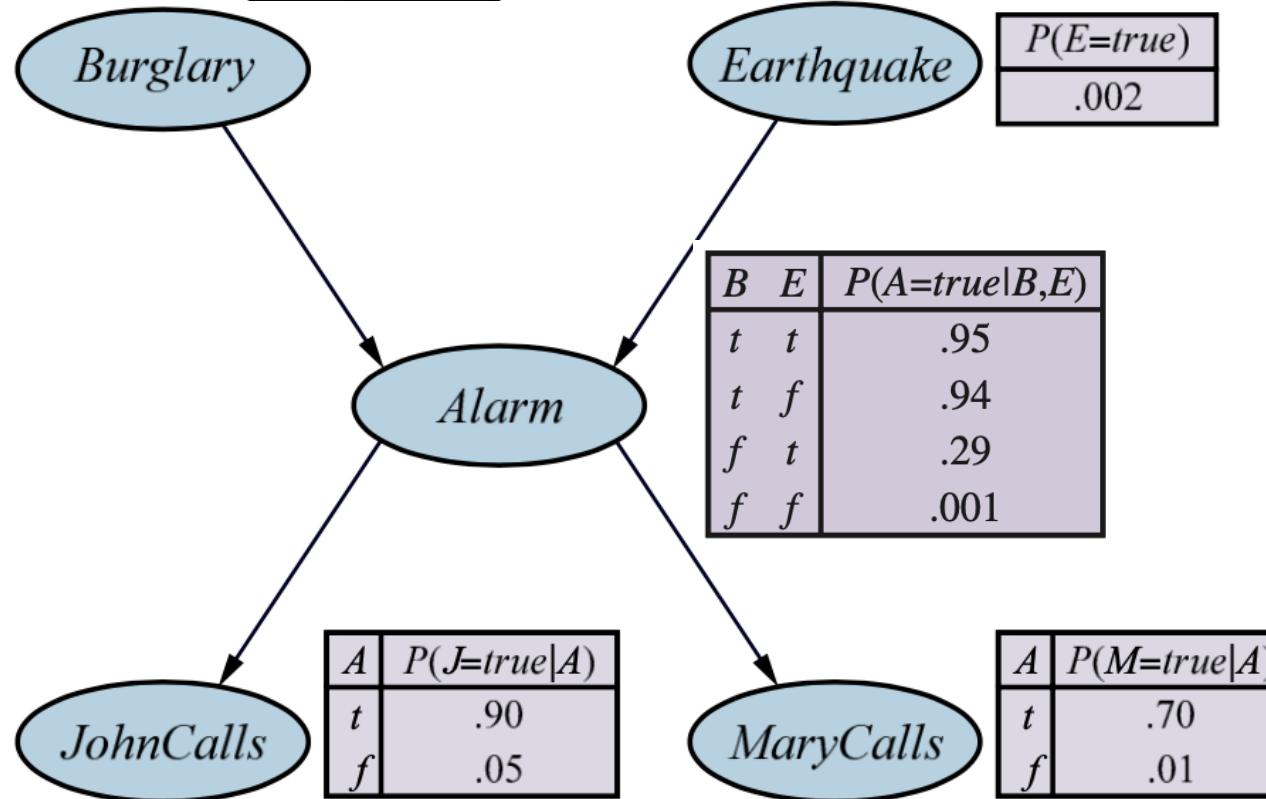
B	P(B)
+b	0.001
-b	0.999

E	P(E)
+e	0.002
-e	0.998



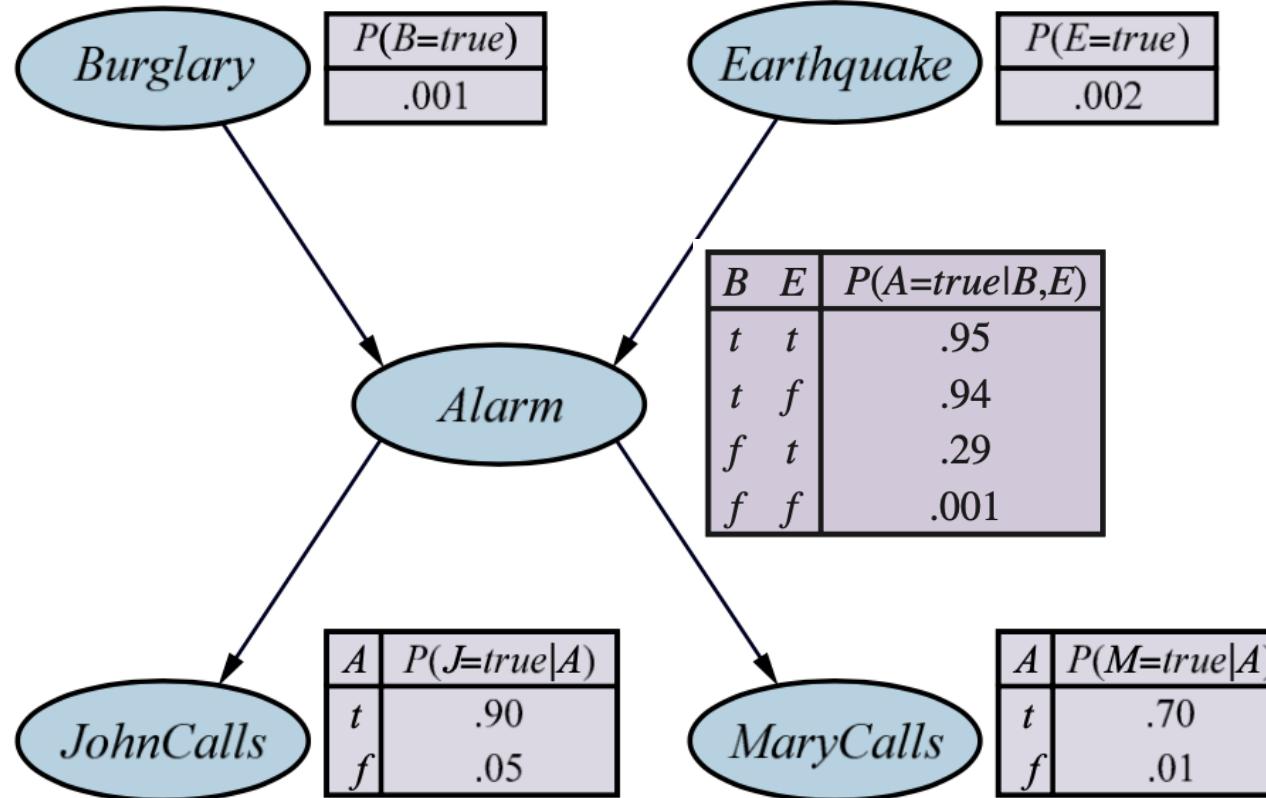
# Example

B	P(B)
+b	0.001
-b	0.999

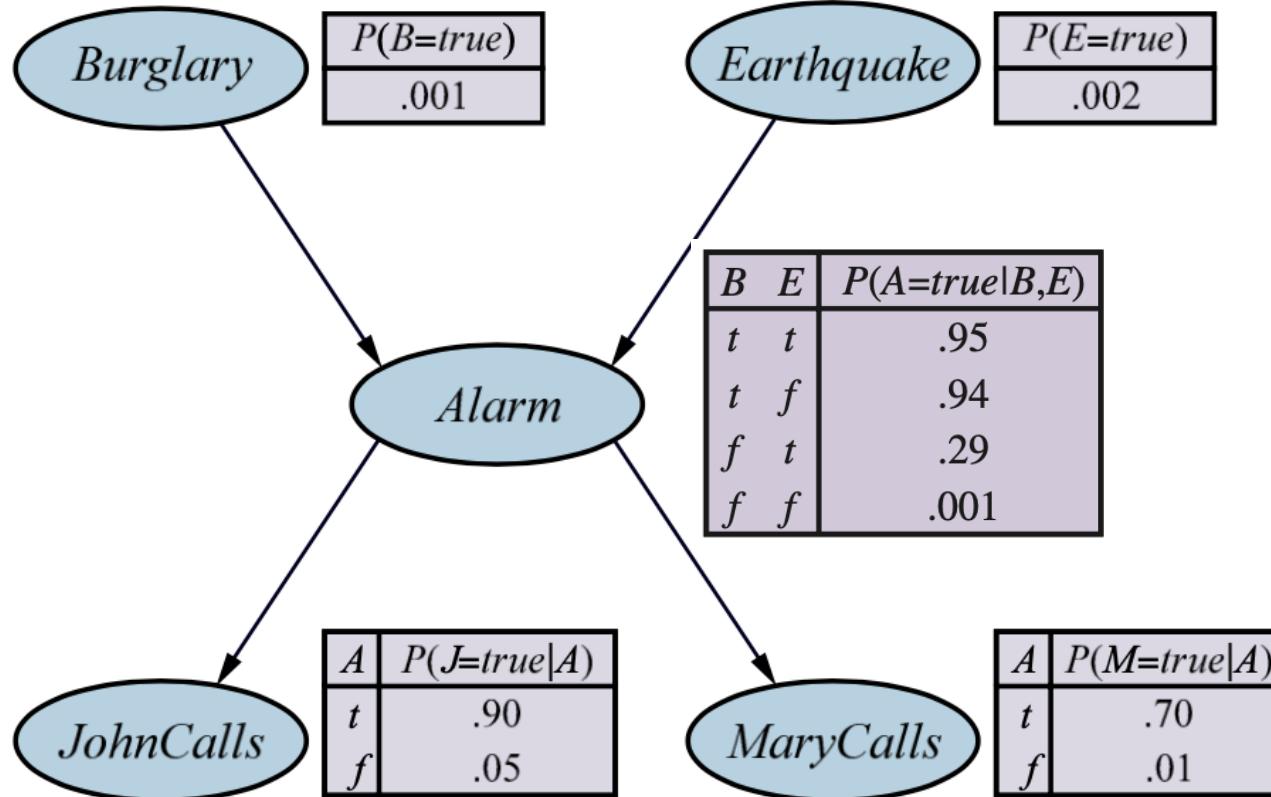


# Example

B	P(B)
+b	0.001
-b	0.999

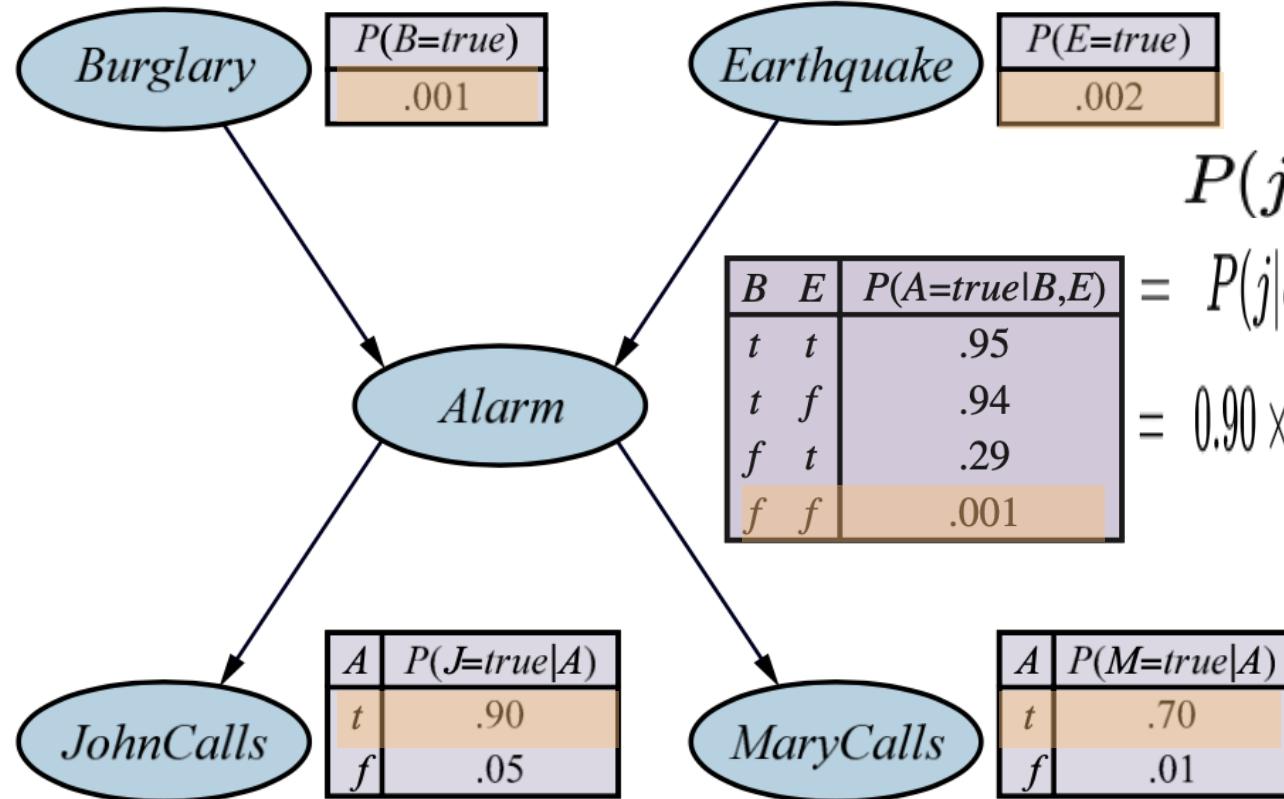


# Example



$$P(x_1, \dots, x_n) = \prod_{i=1}^n P(x_i | parents(X_i))$$

## Example



$$P(j,m,a,\neg b,\neg e)$$

$$= P(j|a)P(m|a)P(a|\neg b \wedge \neg e)P(\neg b)P(\neg e)$$

$$= 0.90 \times 0.70 \times 0.001 \times 0.999 \times 0.998 = 0.000628$$

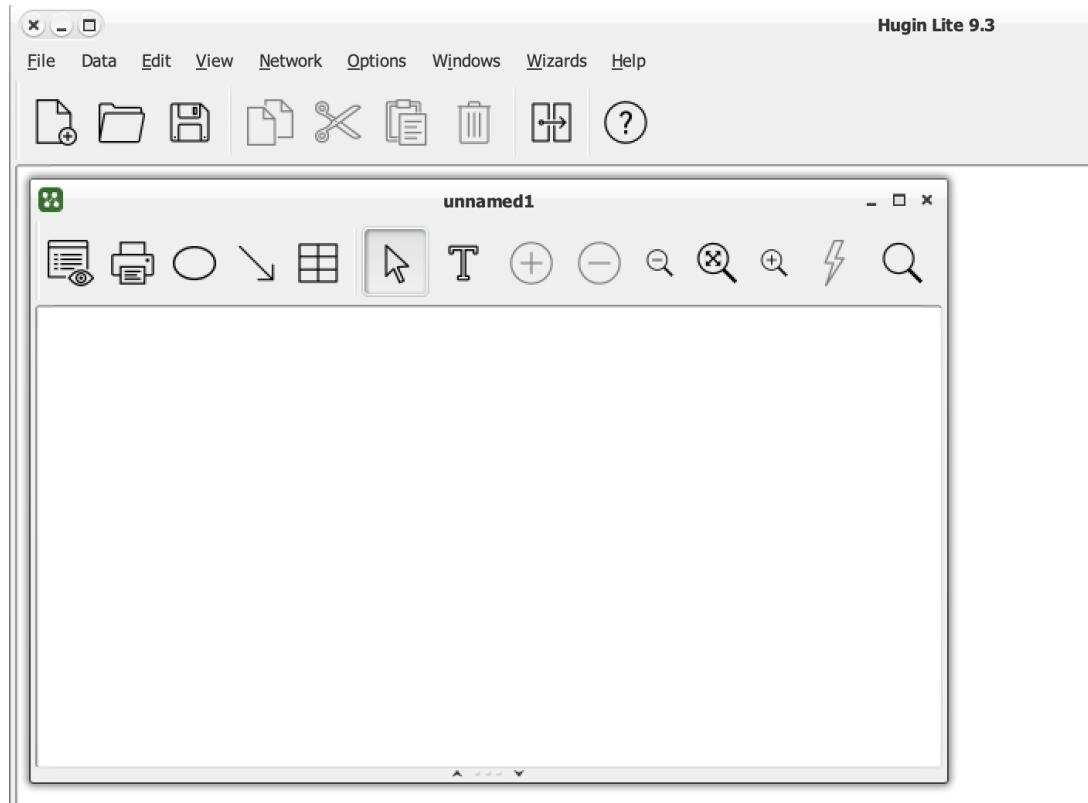
# Inference in Bayes Net

- Exact inference (AIMA Ch 13.3)
  - Efficient approaches
- Approximate inference (AIMA Ch 13.4)

Sampling {  
Prior  
Rejection  
Likelihood-weighted  
Gibbs

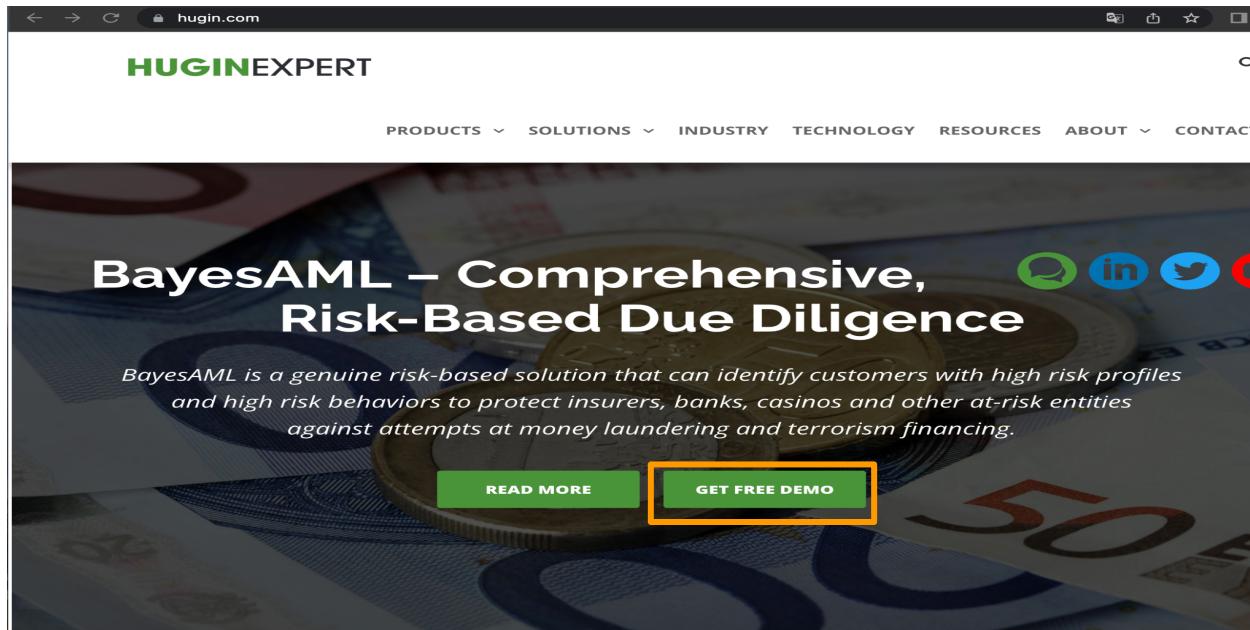
variable elimination (choose the one that creates the smallest factor  $\Rightarrow$  choosing the order of elimination is NP-Hard)

# HUGINEXPERT: Bayes Net Software



# HUGINEXPERT: Bayes Net Software

- Hugin Lite (<https://www.hugin.com/>)



# Inference in Bayes Net

$$P(b) = 0.001$$

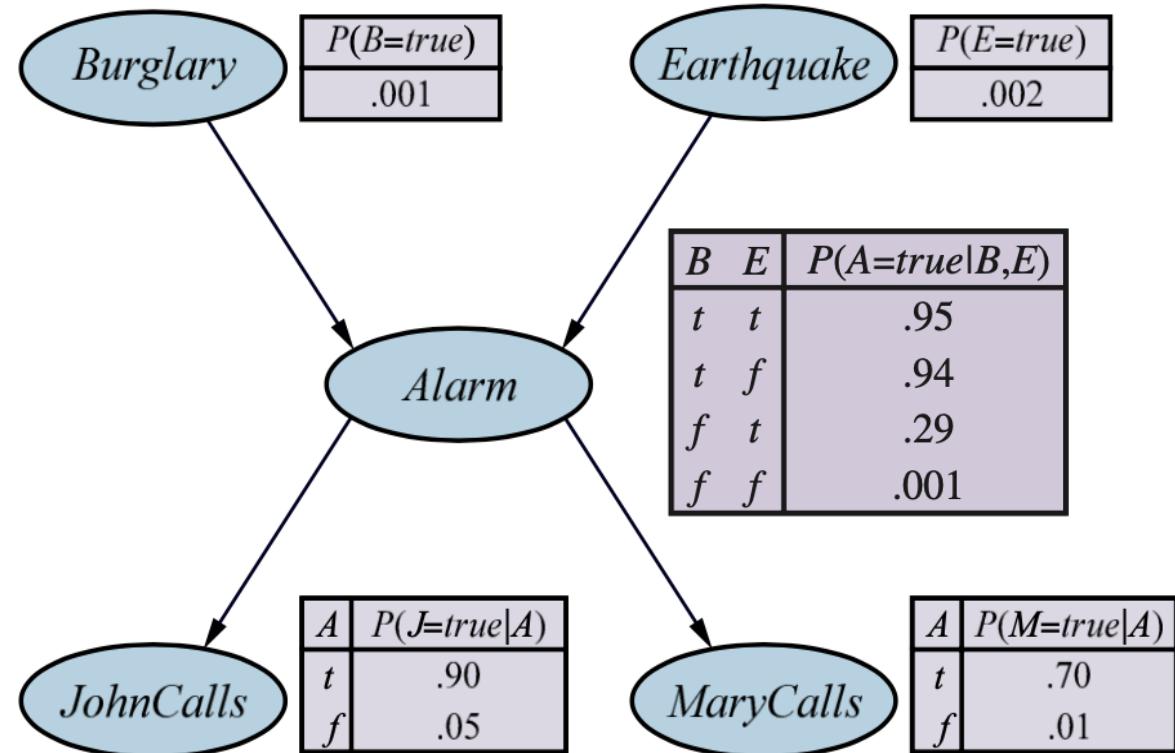
$$P(b | j) = ?$$

$$P(b | m) = ?$$

$$P(b | j, m) = ?$$

$$P(b | j, \neg m) = ?$$

$$P(b | j, m, \neg e) = ?$$





bn\_alarm

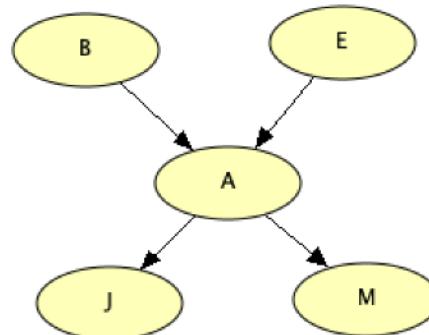


Edit Functions View

Run Mode

B E A J M

A	false	true
false	0.99	0.3
true	0.01	0.7





?



bn\_alarm



bn\_alarm

A



B



E



J



M



Toggle Node List



Expand node list

Collapse node list

99.80 false

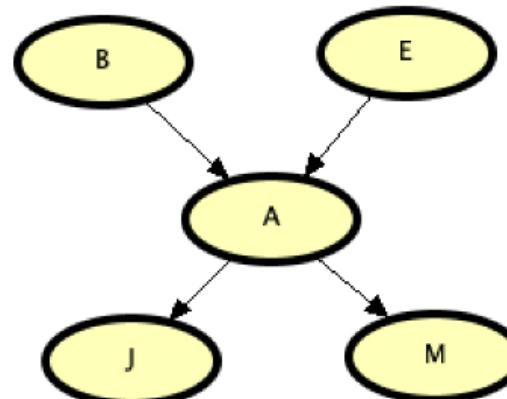
0.20 true

94.79 false

5.21 true

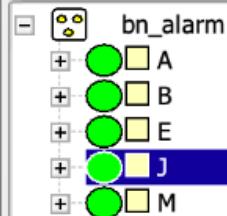
98.83 false

1.17 true





bn\_alarm



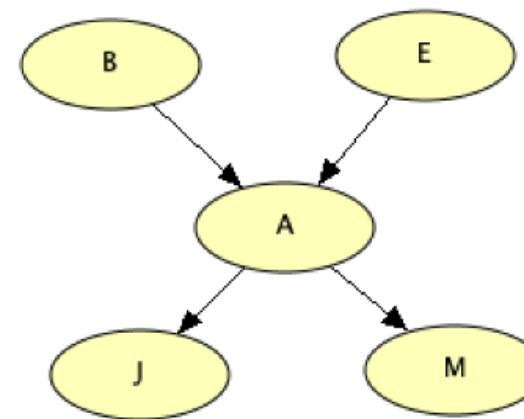
Toggle Node List

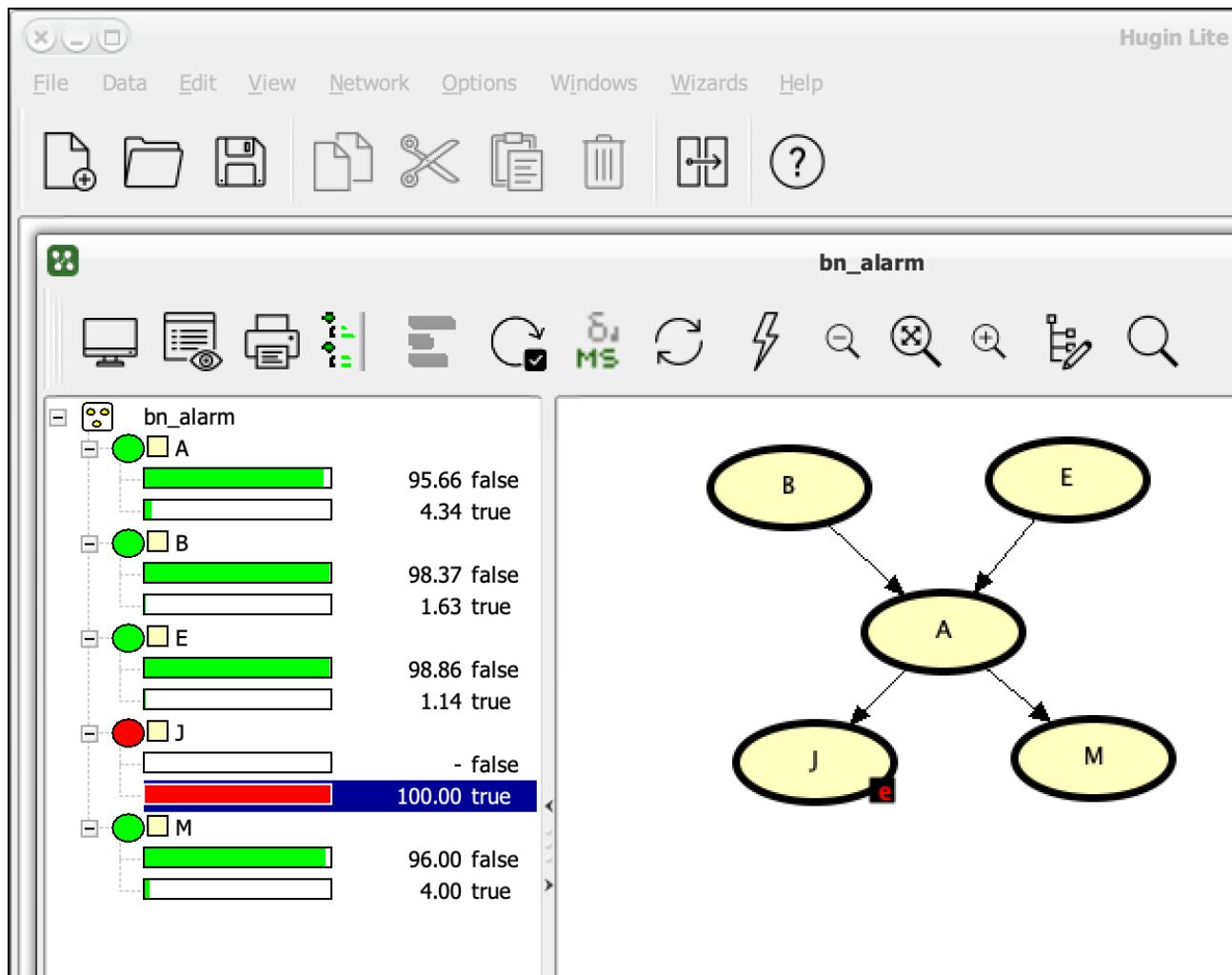


Expand node list



Collapse node list





File Data Edit View Network Options Windows Wizards Help



bn\_alarm

- □ ×



MS



bn\_alarm

A

95.66 false

4.34 true

B

98.37 false

1.63 true

E

98.86 false

1.14 true

J

- false

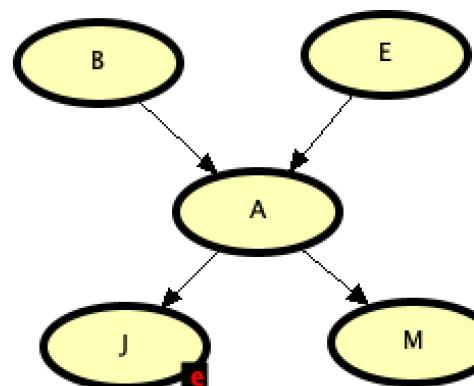
100.00 true

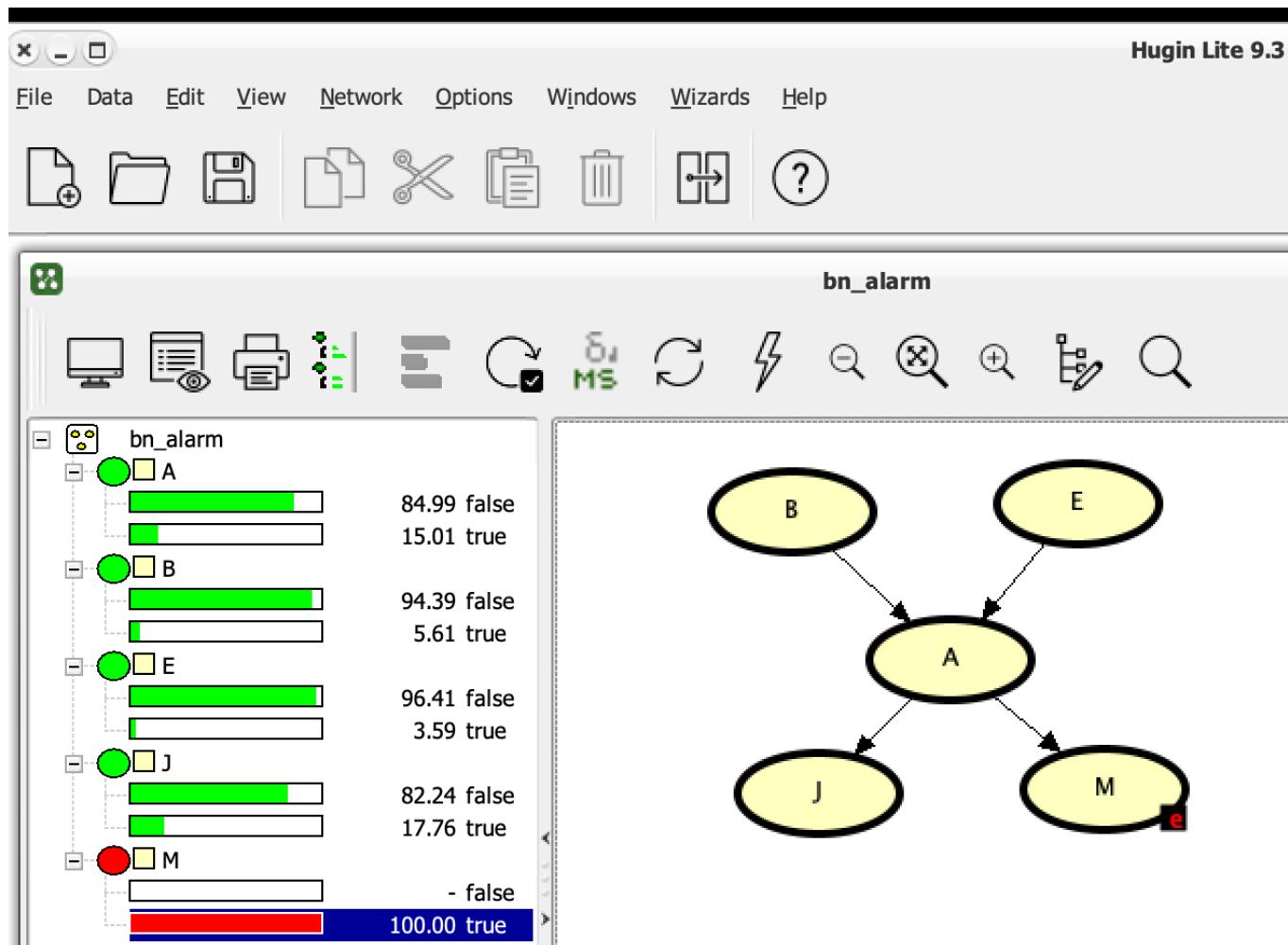
M

96.00 false

4.00 true

Initialize network





File Data Edit View Network Options Windows Wizards Help

bn\_alarm

bn\_alarm

A 29.00 false  
A 71.00 true  
B 65.58 false  
B 34.42 true  
E 100.00 false  
E - true  
J - false  
J 100.00 true  
M - false  
M 100.00 true

B → A → J → M  
E → A → M

```
graph TD; B((B)) --> A((A)); E((E)) --> A; A --> J((J)); A --> M((M));
```

# Inference in Bayes Net

$$P(b) = 0.001$$

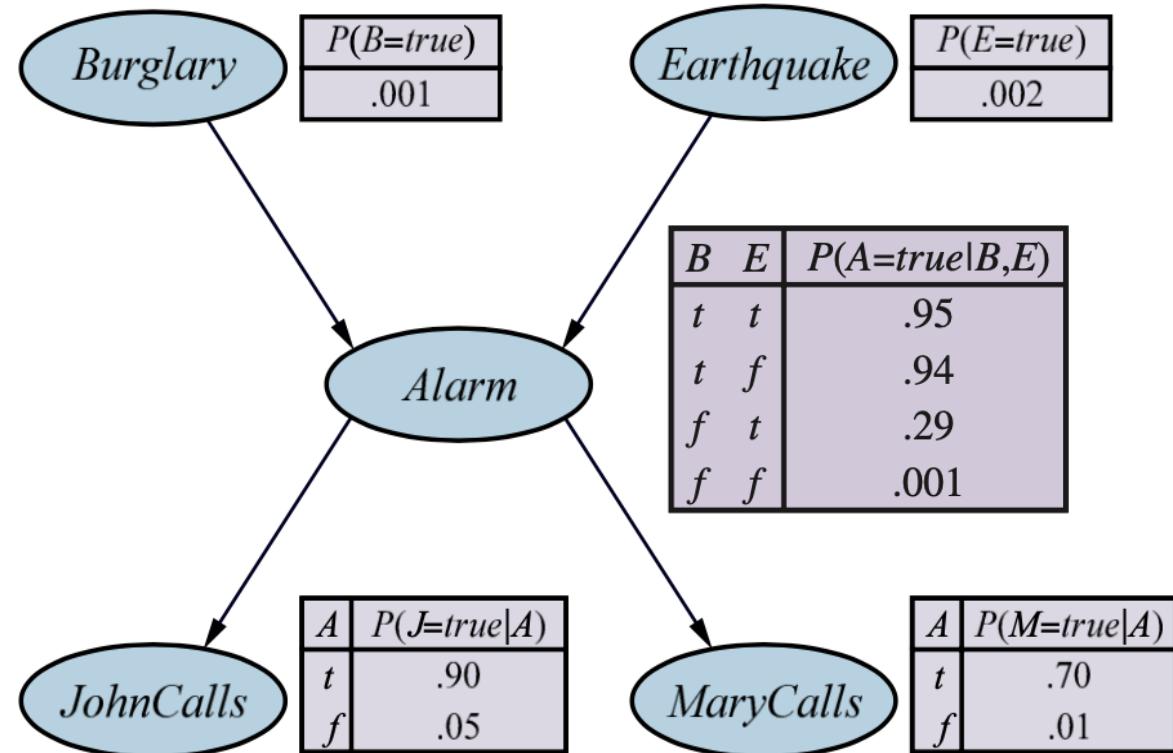
$$P(b | j) = ? 0.0163$$

$$P(b | m) = ? 0.0561$$

$$P(b | j, m) = ? 0.2842$$

$$P(b | j, \neg m) = ? 0.0051$$

$$P(b | j, m, \neg e) = ? 0.3442$$



# Toy Example (in HW3)

- Variables and domains
  - Disease: {covid-19, flu, cold}
  - Symptoms:
    - Running nose: {true, false}
    - Fever: {true, false}
    - Cough: {true, false}
- Questions
  - Patient 1: running nose and fever
    - $P(\text{covid-19} | r, f) = ?$
  - Patient 2: cough
    - $P(\text{covid-19} | c) = ?$
    - $P(\text{flu} | c) = ?$
    - $P(\text{cold} | c) = ?$

$$P(D=\text{covid-19}) = 0.2$$

$$P(D=\text{flu}) = 0.3$$

$$P(D=\text{cold}) = 0.5$$

$$P(r | \text{covid-19}) = 0.6$$

$$P(r | \text{flu}) = 0.4$$

$$P(r | \text{cold}) = 0.5$$

$$P(f | \text{covid-19}) = 0.8$$

$$P(f | \text{flu}) = 0.3$$

$$P(f | \text{cold}) = 0.2$$

$$P(c | \text{covid-19}) = 0.6$$

$$P(c | \text{flu}) = 0.2$$

$$P(c | \text{cold}) = 0.4$$