

GATE 11.9.4 Q-1

EE23BTECH11207 -KAILASH.C*

In the block diagram shown below, an infinite tap FIR filter with transfer function $H(z) = \frac{Y(z)}{X(z)}$ is realized. If $H(z) = \frac{1}{1-0.5z^{-1}}$, the value of α is

Dividing by $X(z)$ in both sides:

$$\frac{Y(z)}{X(z)} = \sum_{n=0}^{\infty} (z^{-1}\alpha^2)^n \quad (2)$$

$$H(z) = \sum_{n=0}^{\infty} (z^{-1}\alpha^2)^n \quad (3)$$

$$\frac{1}{1-0.5z^{-1}} = \sum_{n=0}^{\infty} (z^{-1}\alpha^2)^n \quad (4)$$

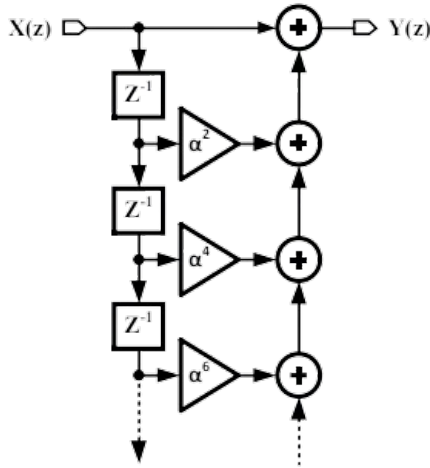
$$\frac{1}{1-0.5z^{-1}} = \frac{1}{1-z^{-1}\alpha^2} \quad (5)$$

$$1-0.5z^{-1} = 1-z^{-1}\alpha^2 \quad (6)$$

$$\alpha^2 = 0.5 \quad (7)$$

$$\alpha = \sqrt{0.5} \quad (8)$$

$$\alpha = \frac{1}{\sqrt{2}} \quad (9)$$



Solution:

Parameter	Definition	Value
$H(z)$	Input Transfer Function	$\frac{1}{1-0.5z^{-1}}$
a	First Term of G.P	
r	Common Ratio of G.P	
S_r	Sum of infinite terms in G.P	

TABLE 0
PARAMETER TABLE

From diagram we have:

$$Y(z) = X(z) \left(\sum_{n=0}^{\infty} (z^{-1}\alpha^2)^n \right) \quad (1)$$