

# Quiz 1

MACHINE LEARNING, SUMMER 2019

Name:

UID:

**Problem 1.**(2=.5+.5+1 points.)

1a. Let say  $\mathbf{x} = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix}$  be a vector containing n observations and  $\mathbf{1} = \begin{bmatrix} 1 \\ 1 \\ \vdots \\ 1 \end{bmatrix}$  be vector of ones of size  $n$ . is mean of  $x_1, \dots, x_n$  is given by  $\mathbf{x}^T \mathbf{1}$ ? (True/False)

1b. What is the support of binomial random variable with parameters  $N$ (Total trials) and  $p$  (probability of success). Recall by support, we mean the values taken by a random variable.

1c. Let say  $\mathbf{D} = [\mathbf{a}_1, \mathbf{a}_2, \dots, \mathbf{a}_k]$  be the matrix with  $k$  columns  $\mathbf{a}_i$  for  $i \in \{1, \dots, k\}$ .

Let  $\mathbf{x} = \begin{bmatrix} x_1 \\ x_2 \\ \vdots \\ x_n \end{bmatrix}$  be a vector. Write the expression for  $\mathbf{D}\mathbf{x}$ (Matrix, vector product) using  $\mathbf{a}_i$  (columns of matrix) and  $x_i$ (coordinates of vector  $\mathbf{x}$ ).

**Problem 2.**(1.5= .25+.25+.25+.25+.25+.25 points) Using bayes rules write, right hand side of conditional probability  $P(\mathbf{X}|\boldsymbol{\theta})$ . Also, using arrows highlight posterior probability, likelihood and prior terms.

$P(\mathbf{X}|\boldsymbol{\theta})=$