

Lengstu vaxandi hlutrunur

Bergur Snorrason

January 28, 2024

- ▶ Við höfum nú þegar skoðað hvernig finna megí lengstu vaxandi hlutrunur með tæmandi leit.

- ▶ Við höfum nú þegar skoðað hvernig finna megi lengstu vaxandi hlutrunur með tæmandi leit.
- ▶ Sjáum núna hvernig við getum gert það með kvikri bestun.

Hlutrúður

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- ▶ Við viljum nú, fyrir gefna runu, finna lengdina á lengstu vaxandi hlutrunum hennar.
- ▶ Það er oft talað um að finna „lengstu vaxandi hlutrununa“ þó það geti verið margar jafn langar „lengstu vaxandi hlutrúnur“.

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- ▶ Þá fáum við

$$f(x) = \begin{cases} 1, & \text{ef } x = 1, \\ \max_{\substack{1 \leq k < x \\ a_k \leq a_x}} f(k) + 1, & \text{annars.} \end{cases}$$

```

6  int v[MAXN], d[MAXN];
7  int dp_lookup(int x)
8  {
9      if (d[x] != -1) return d[x];
10     if (x == 0) return 1;
11     int i;
12     for (d[x] = 1, i = 0; i < x; i++) if (v[i] <= v[x])
13         d[x] = max(d[x], dp_lookup(i) + 1);
14     return d[x];
15 }
16
17 int lis(int *a, int n)
18 {
19     int i, r = 1;
20     for (i = 0; i < n; i++) d[i] = -1, v[i] = a[i];
21     for (i = 0; i < n; i++) r = max(r, dp_lookup(i));
22     return r;
23 }

```

- ▶ Við erum með einvítt stöðurúm af stærð n og hver uppfærsla er í $\mathcal{O}(\quad)$.

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- ▶ Við getum bætt þetta, en fyrst þurfum við að leysa þetta aftur með kvikri bestun, en annarri rakningarformúlu.

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$$f(x, y) = \begin{cases} -\infty, & \text{ef } x = 0 \text{ og } y = 0, \\ \infty, & \text{annars, ef } x = 0, \\ f(x-1, y), & \text{ef } a_x < f(x-1, y-1), \\ \min(f(x-1, y), a_x), & \text{annars.} \end{cases}$$

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- ▶ Grunntilvikin eru til að auðvelda útfærslu.

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- ▶ Grunntilvikin eru til að auðvelda útfærslu.
- ▶ Lengd lengstu vaxandi hlutrunanna er þá stærsta ℓ þannig að $f(n, \ell) < \infty$.

```

7 int v[MAXN], d[MAXN][MAXN];
8 int dp_lookup(int x, int y)
9 {
10     if (x == -1) return y == 0 ? -INF : INF;
11     if (d[x][y] != -1) return d[x][y];
12     if (v[x] < dp_lookup(x - 1, y - 1)) return d[x][y] = dp_lookup(x - 1, y);
13     return d[x][y] = min(dp_lookup(x - 1, y), v[x]);
14 }
15
16 int lis(int *a, int n)
17 {
18     int i, j, x;
19     for (i = 0; i < n; i++) v[i] = a[i];
20     for (i = 0; i < n; i++) for (j = 0; j < n + 1; j++) d[i][j] = -1;
21     for (x = n; dp_lookup(n - 1, x) == INF; x--);
22     return x;
23 }

```

- ▶ Við erum með tvívítt stöðurúm af stærð $(n + 1) \cdot (n + 1)$ og hver uppfærsla er í $\mathcal{O}(\quad)$.

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- ▶ En þetta er sama tímaflækja og við fengum áðan.

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- ▶ Heildartímaflækjan er því $\mathcal{O}(n^2)$.
- ▶ En þetta er sama tímaflækja og við fengum áðan.
- ▶ Prófum að útfæra þetta neðansækið og sjáum hvað við fáum.

► Rifjum upp að

$$f(x, y) = \begin{cases} -\infty, & \text{ef } x = 0 \text{ og } y = 0, \\ \infty, & \text{annars, ef } x = 0, \\ f(x-1, y), & \text{ef } a_x < f(x-1, y-1), \\ \min(f(x-1, y), a_x), & \text{annars.} \end{cases}$$

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- Sjáum að fallgildi $f(x, y)$ ákvarðast af $f(x-1, y)$ og $f(x-1, y-1)$.

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- Sjáum að fallgildi $f(x, y)$ ákvarðast af $f(x-1, y)$ og $f(x-1, y-1)$.
- Svo við getum fyllt í töfluna í lestrarröð.


```

7 int lis(int *a, int *b, int n)
8 {
9     int i, j, x, y, d[n + 1][n + 1];
10    for (i = 0; i < n + 1; i++) d[0][i] = INF;
11    for (i = 0; i < n + 1; i++) d[i][0] = -INF;
12    for (i = 1; i < n + 1; i++) for (j = 0; j < n + 1; j++)
13    {
14        if (a[i - 1] < d[i - 1][j - 1]) d[i][j] = d[i - 1][j];
15        else d[i][j] = min(d[i - 1][j], a[i - 1]);
16    }
17    for (x = n; d[n][x] == INF; x--);
18    for (i = 0; i < x; i++) b[i] = d[n - x + i + 1][i + 1];
19    return x;
20 }

```

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- ▶ Skoðum núna hvernig uppfærslan á töflunni fer fram og sjáum hvort við getum bætt tímaflækjuna.

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- Þetta getur þó bara átt sér stað, í mesta lagi, einu sinni í röðuðum lista.

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- ▶ En þar sem línurnar eru allar raðaðar getum við í staðinn framkvæmt helmingunarleit.

```

10 int lis(int *a, int *b, int n)
11 {
12     int i, j, x, y, d[n + 1], e[n];
13     for (i = 0; i < n + 1; i++) d[i] = i == 0 ? -INF : INF;
14     for (i = 0; i < n; i++)
15     {
16         int r = -1, s;
17         for (s = n + 1; s >= 1; s /= 2)
18             while (r + s < n + 1 && d[r + s] < a[i]) r += s;
19         d[r + 1] = a[i], e[i] = d[r];
20     }
21     for (x = n; d[x] == INF; x--);
22     for (i = n - 1, j = x - 1, y = d[x]; j >= 0; i--) if (a[i] == y)
23         y = e[i], b[j--] = a[i];
24     return x;
25 }

```


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