

	Belastungsfall	Biegelinie	Durchbiegung	Neigung $w' = \tan \alpha$
1		$w(x) = \frac{1}{6} \frac{F}{EI} a x^2 \left(3 - \frac{x}{a} \right)$	$w(a) = \frac{F a^3}{3EI}$	$w'(a) = \frac{F a^2}{2EI}$
2		$w(x) = \frac{M}{2EI} x^2$	$w(a) = \frac{M a^2}{2EI}$	$w'(a) = \frac{M a}{EI}$
3		$w(x) = \frac{q a^4}{24EI} \left(6 \frac{x^2}{a^2} - 4 \frac{x^3}{a^3} + \frac{x^4}{a^4} \right)$	$w(a) = \frac{q a^4}{8EI}$	$w'(a) = \frac{q a^3}{6EI}$
4		$x \leq \frac{a}{2}$ $w(x) = \frac{F a^3}{16EI} \left(\frac{x}{a} - \frac{4x^3}{3a^3} \right)$	$w\left(\frac{a}{2}\right) = \frac{F a^3}{48EI}$	$w'(a) = \frac{F a^2}{16EI}$
5		$0 \leq x \leq b$ $w(x) = \frac{F b c^2}{6EI} \frac{x}{a} \left(1 + \frac{a}{c} - \frac{x^2}{bc} \right)$ $b \leq x \leq a$ $w(x) = \frac{F c b^2}{6EI} \frac{a-x}{a} \left(\frac{a+b}{b} - \frac{(x-a)^2}{bc} \right)$	$w(b) = \frac{F}{3EI} \frac{b^2 c^2}{a}$ für $b > c$ gilt: $x^* = b \sqrt{\frac{a+c}{3b}}$ $w_{\max} = w(b) \frac{a+c}{3c} \frac{x^*}{a}$	$w'(0) = \frac{w(b)}{2b} \left(1 + \frac{a}{c} \right)$ $w'(a) = \frac{w(b)}{2c} \left(1 + \frac{a}{b} \right)$
6		$w(x) = \frac{M_1 a^2}{6EI} \left(\frac{x}{a} - \frac{x^3}{a^3} \right) + \frac{M_2 a^2}{6EI} \left(2 \frac{x}{a} - 3 \frac{x^2}{a^2} + \frac{x^3}{a^3} \right)$	für $M_1 = M_2$ gilt: $w_{\max} = \frac{M_1 a^2}{8EI}$	$w'(0) = \frac{a}{6EI} (2M_2 + M_1)$ $w'(a) = \frac{a}{6EI} (2M_1 + M_2)$
7		$w(x) = \frac{q a^4}{24EI} \frac{x}{a} \left[1 - 2 \left(\frac{x}{a} \right)^2 + \left(\frac{x}{a} \right)^3 \right]$	$w_{\max} = w\left(\frac{a}{2}\right) = \frac{5 q a^4}{384EI}$	$w'(a) = \frac{q a^3}{24EI}$
8		$0 \leq x \leq a$ $w(x) = -\frac{F a b x}{6EI} \left(1 - \frac{x^2}{a^2} \right)$ $a \leq x \leq a+b$ $w(x) = \frac{F a^2 (x-a)}{6EI} \left(\frac{2b}{a} + \frac{3b(x-a)}{a^2} - \frac{(x-a)^2}{a^2} \right)$	$w(a+b) = \frac{F a b^2}{3EI} \left(1 + \frac{b}{a} \right)$ $w_{\max} = \frac{F a^2 b}{9\sqrt{3}EI}$ $x^* = \frac{a}{\sqrt{3}}$	$w'(0) = \frac{F a b}{6EI}$ $w'(a) = 2 w'(0)$ $w'(a+b) = \frac{F b^2}{2EI} \left(1 + \frac{2a}{3b} \right)$