

# "Hypothesis testing"

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Hypothesis  $\rightarrow$  statement (question)

- i)  $H_0$   $\rightarrow$  original hypothesis  
 $H_A$   $\rightarrow$  Alternative hypothesis

ii) Level of significance:  $\alpha = 0.05$

iii) Test - Statistic:

formula  
to calculate

iv) Computation:

Substitute the values  
in test-statistics (formula).

v) Critical region:

$\rightarrow$  Rejection Region (a table value)  
(a probability value)

vi) Conclusion:

Accept  $H_0$ .

or

Reject  $H_0$ .

Type I error:

true null hypothesis is rejected.

Type II error:

false null hypothesis is accepted.

Conditions of  $H_0$ .

	True	False
accept $H_0$	Correct	Type II error
Reject $H_0$	Type I error	correct

"Revision"

	$n < 30$	$n \geq 30$
$\sigma$ known	$Z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}}$	$Z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}}$
$\sigma$ unknown = $s$	$t = \frac{\bar{x} - \mu}{s/\sqrt{n}}$	$Z = \frac{\bar{x} - \mu}{s/\sqrt{n}}$

P values: → Probability values

↳ how unusual sample results are, given that the null hypothesis is true.

↓  
P value is the smallest value of  $\alpha$  for which we can reject a null hypothesis. probability of not confidence

## Hypothesis Testing about a single population Mean (i.e; $\mu$ ):

i)  $H_0: \mu \leq \mu_0$

$H_0: \mu \geq \mu_0$

$H_0: \mu = \mu_0$

$H_A: \mu \geq \mu_0$

$H_A: \mu \leq \mu_0$

$H_A: \mu \neq \mu_0$

(a)

(b)

(c)

ii) Level of Significance:  $\alpha =$

iii) Test - Statistics:

$$Z = \frac{\bar{X} - \mu_0}{\sigma / \sqrt{n}}$$

or

$$Z = \frac{\bar{X} - \mu_0}{s / \sqrt{n}}$$

or

$$t = \frac{\bar{X} - \mu_0}{s / \sqrt{n}}$$

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#### iv) Computations:

$$n = ?$$

$$\bar{X} = ?$$

$$\mu_0 = ?$$

$$s = ? \text{ or } \sigma = ?$$

#### v) Critical region:

Case a:

$$Z > Z_{1-\alpha}$$

or

$$t > t_{1-\alpha}$$

Case b:

$$Z < -Z_{1-\alpha}$$

or

$$t < -t_{1-\alpha}$$

Case c:

$$|Z| > Z_{1-\alpha/2}$$

$$\text{i.e.; } Z < -Z_{1-\alpha/2}$$

or

$$Z > Z_{1-\alpha/2}$$

or

$$|t| > t_{1-\alpha/2}$$

$$\text{i.e.; } t < -t_{1-\alpha/2}$$

$$\text{or } t > t_{1-\alpha/2}$$

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