```
In [1]:
```

```
from sklearn.datasets import load_iris
import numpy as np
import matplotlib.pyplot as plt
plt.rcParams['figure.figsize'] = (12, 8)
```

```
In [2]:
```

```
X, y = load_iris(return_X_y=True)
```

In [3]:

```
c1 = np.array([X[i] for i in range(len(y)) if y[i] == 0])
c2 = np.array([X[i] for i in range(len(y)) if y[i] == 1])
c3 = np.array([X[i] for i in range(len(y)) if y[i] == 2])
```

In [4]:

```
def cov(data):
    X = data - data.mean(axis=0, keepdims=True)
    return 1.0/len(data)*np.dot(X.transpose(), X)
```

In [5]:

```
a1, cov1 = c1.mean(axis=0), cov(c1)
a2, cov2 = c2.mean(axis=0), cov(c2)
a3, cov3 = c3.mean(axis=0), cov(c3)
```

Матожидания:

In [6]:

```
print a1
print a2
print a3
```

```
[ 5.006 3.418 1.464 0.244]
[ 5.936 2.77 4.26 1.326]
[ 6.588 2.974 5.552 2.026]
```

Матрицы ковариаций:

In [7]:

```
print cov1, '\n\n'
print cov2, '\n\n'
print cov3
[[ 0.121764
             0.098292
                       0.015816
                                  0.010336]
[ 0.098292
             0.142276
                       0.011448
                                  0.011208]
 [ 0.015816
             0.011448
                       0.029504
                                  0.005584]
 [ 0.010336
             0.011208
                       0.005584
                                  0.011264]]
[[ 0.261104
             0.08348
                       0.17924
                                  0.054664]
 [ 0.08348
             0.0965
                       0.081
                                  0.04038 ]
 [ 0.17924
                       0.2164
                                  0.07164 ]
             0.081
 [ 0.054664
             0.04038
                       0.07164
                                  0.038324]]
[[ 0.396256
             0.091888
                       0.297224
                                  0.048112]
 [ 0.091888
             0.101924
                       0.069952
                                  0.046676]
 [ 0.297224
             0.069952
                       0.298496
                                  0.047848]
 [ 0.048112
                       0.047848
                                  0.073924]]
             0.046676
```

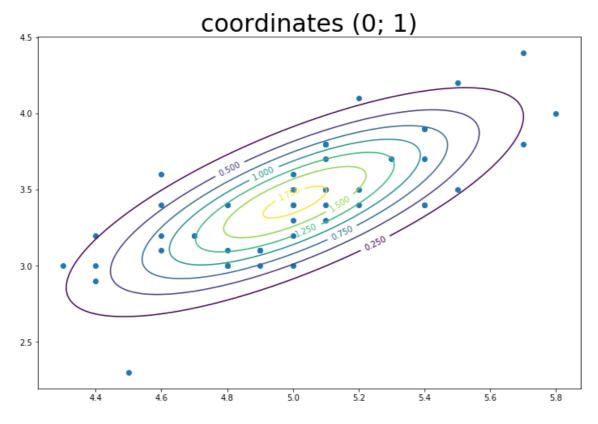
In [8]:

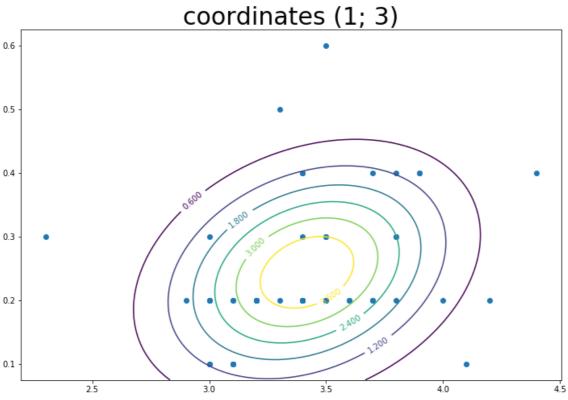
```
from scipy.stats import multivariate normal
import matplotlib.cm as cm
import matplotlib.mlab as mlab
def countur(pdf, data, i, j):
    imin, imax, jmin, jmax = np.min(data[:,i]), np.max(data[:,i]),
np.min(data[:,j]), np.max(data[:,j])
    imin, imax = imin - 0.05*(imax-imin), imax + 0.05*(imax-imin)
    jmin, jmax = jmin - 0.05*(jmax-jmin), jmax + 0.05*(jmax-jmin)
    X, Y = np.meshgrid(np.linspace(imin, imax, 1000), np.linspace(jmin, jmax, 1000)
00))
    Z = np.zeros like(X)
    for k in range(X.shape[0]):
        for l in range(Y.shape[1]):
            Z[k][l] = pdf((X[k][l], Y[k][l]))
    plt.figure()
    plt.scatter(data[:, i], data[:, j])
    CS = plt.contour(X, Y, Z)
    plt.clabel(CS, inline=1, fontsize=10)
    plt.title('coordinates (' + str(i) + '; ' + str(j) + ')', fontsize=30)
    plt.show()
def coord pdf(a, cov m, i, j):
    ij a = np.array([a[i], a[i]])
    ij_cov = np.array([[cov_m[i][i], cov_m[i][j]], [cov_m[j][i], cov_m[j][j]]])
    rv = multivariate normal(ij a, ij cov)
    return rv.pdf
def deal with component(data, a, cov m):
    pdf1 = coord pdf(a, cov m, 0, 1)
    pdf2 = coord pdf(a, cov m, 1, 3)
    pdf3 = coord pdf(a, cov m, 2, 3)
    countur(pdf1, data, 0, \overline{1})
    countur(pdf2, data, 1, 3)
    countur(pdf3, data, 2, 3)
```

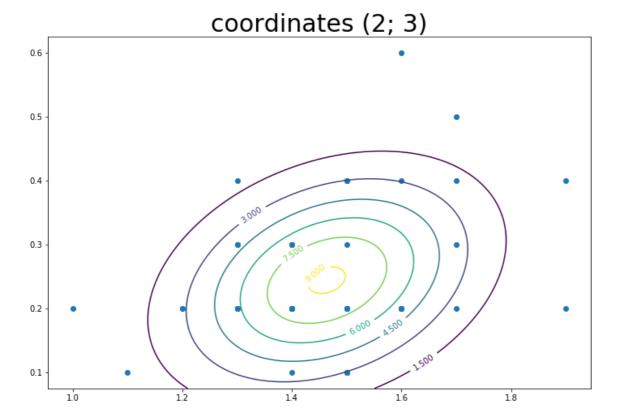
Компонента 0

In [10]:

deal_with_component(c1, a1, cov1)



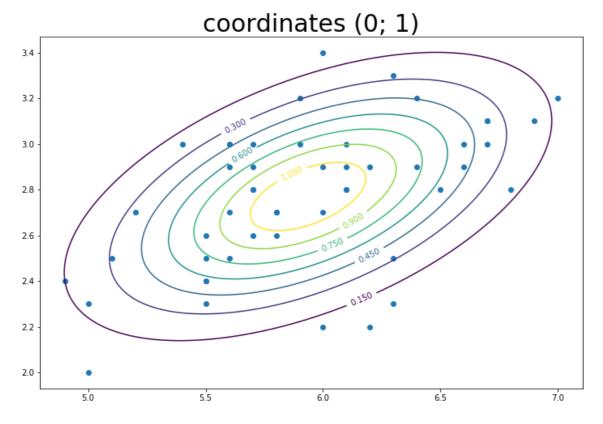


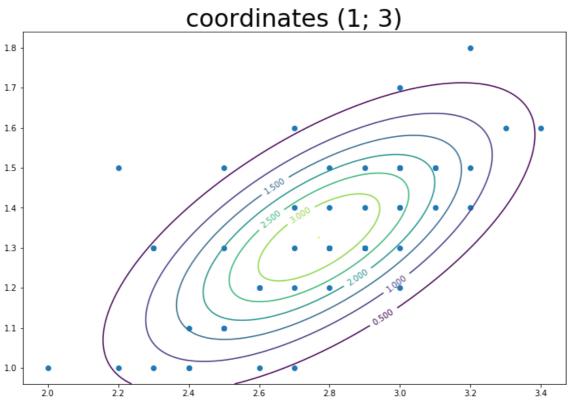


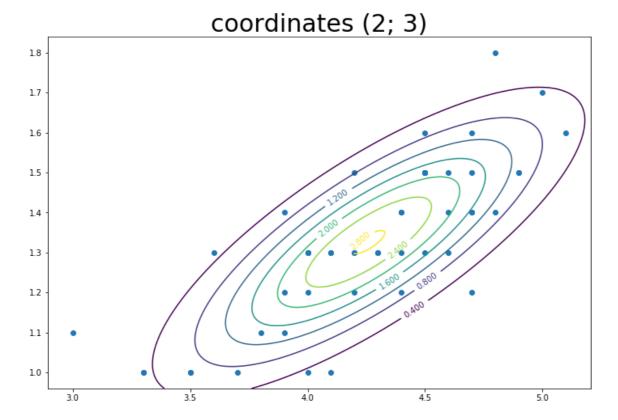
Компонента 1

In [11]:

deal_with_component(c2, a2, cov2)



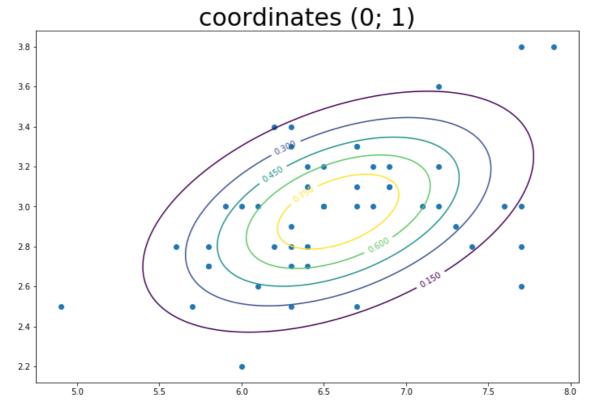


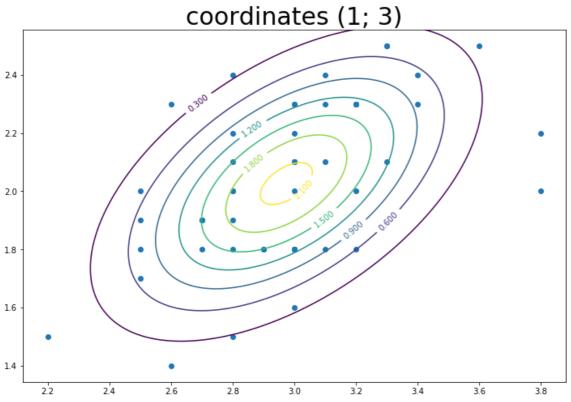


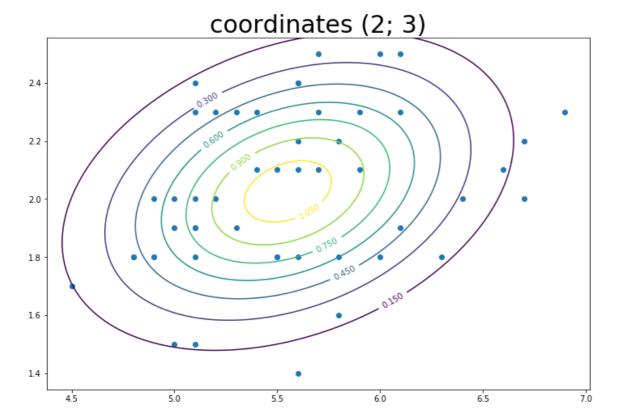
Компонента 2

In [12]:

deal_with_component(c3, a3, cov3)







Оценка P(t=k)

In [9]:

$$p1,\ p2,\ p3=float(len(c1))/len(X),\ float(len(c2))/len(X),\ float(len(c3))/len(X)$$

$$p(x|T
eq l)=rac{p(x,T
eq l)}{p(T
eq l)}$$

$$p(x,T
eq l) = \sum_{k=1,k
eq l}^3 p_k(x) P(T=k)$$

$$p(T
eq l) = \sum_{k=1, k
eq l}^3 P(T=k)$$

$$E(x|T
eq l) = rac{1}{p(T
eq l)} \sum_{k=1, k
eq l}^3 a_k P(T=k)$$
, где a_k - матожидание соответствующей компоненты

$$E(x|T \neq 0)$$

In [10]:

$$E(x|T \neq 1)$$

Условные распределения

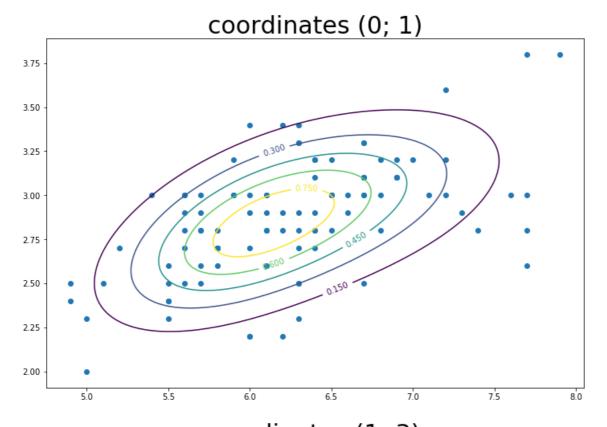
In [13]:

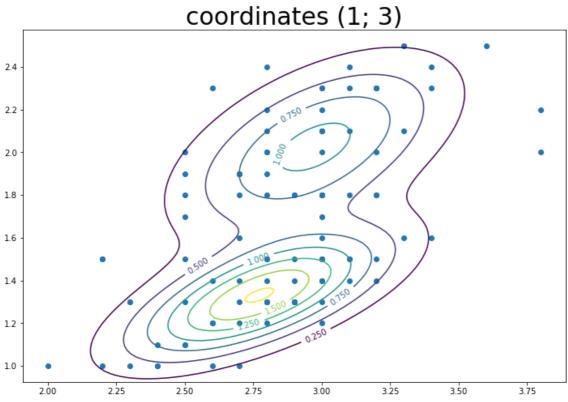
```
def countur(pdf, data, i, j):
    imin, imax, jmin, jmax = np.min(data[:,i]), np.max(data[:,i]),
np.min(data[:,j]), np.max(data[:,j])
    imin, imax = imin - 0.05*(imax-imin), imax + 0.05*(imax-imin)
    jmin, jmax = jmin - 0.05*(jmax-jmin), jmax + 0.05*(jmax-jmin)
    X, Y = np.meshgrid(np.linspace(imin, imax, 100), np.linspace(jmin, jmax,
100))
    Z = np.zeros like(X)
    for k in range(X.shape[0]):
        for l in range(Y.shape[1]):
            Z[k][l] = pdf((X[k][l], Y[k][l]))
    plt.figure()
    CS = plt.contour(X, Y, Z)
    plt.scatter(data[:, i], data[:, j])
    plt.clabel(CS, inline=1, fontsize=10)
    plt.title('coordinates (' + str(i) + '; ' + str(j) + ')', fontsize=30)
    plt.show()
arra, arrcov, arrp, arrdata = [a1, a2, a3], [cov1, cov2, cov3], [p1, p2, p3], [c
1, c2, c3]
def deal with k(k):
    i, j = [n \text{ for } n \text{ in } range(3) \text{ if } n != k-1]
    pdf1 = lambda vec: 1./(arrp[i] + arrp[j])*(arrp[i]*coord pdf(arra[i],
arrcov[i], 0, 1)(vec) + arrp[j]*coord pdf(arra[j], arrcov[j], 0, 1)(vec))
    pdf2 = lambda vec: 1./(arrp[i] + arrp[j])*(arrp[i]*coord_pdf(arra[i],
arrcov[i], 1, 3)(vec) + arrp[j]*coord_pdf(arra[j], arrcov[j], 1, 3)(vec))
    pdf3 = lambda vec: 1./(arrp[i] + arrp[j])*(arrp[i]*coord_pdf(arra[i],
arrcov[i], 2, 3)(vec) + arrp[j]*coord pdf(arra[j], arrcov[j], 2, 3)(vec))
    countur(pdf1, np.concatenate([arrdata[i], arrdata[i]], axis=0), 0, 1)
    countur(pdf2, np.concatenate([arrdata[i], arrdata[j]], axis=0), 1, 3)
    countur(pdf3, np.concatenate([arrdata[i], arrdata[j]], axis=0), 2, 3)
```

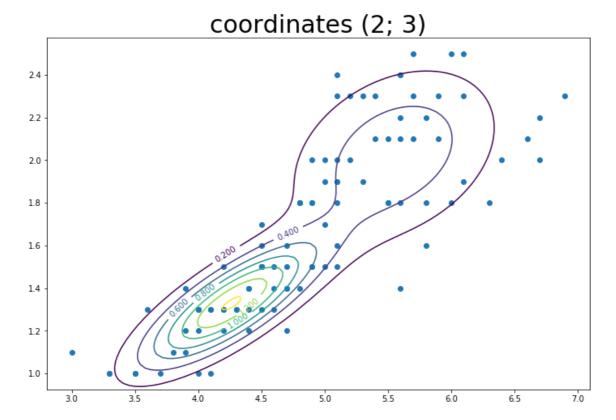
 $T \neq 1$

In [35]:

 $deal_with_k(1)$



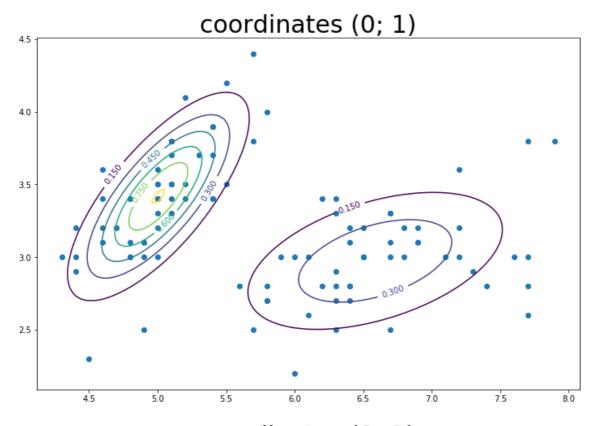


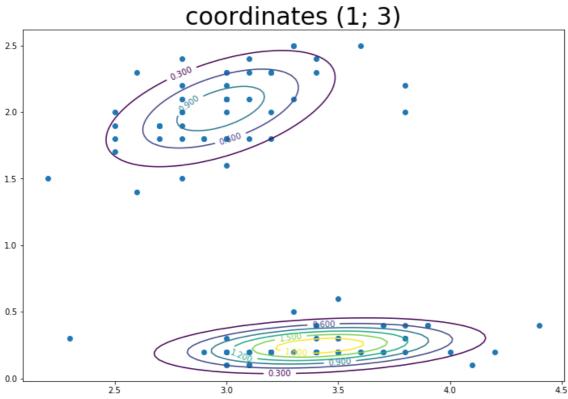


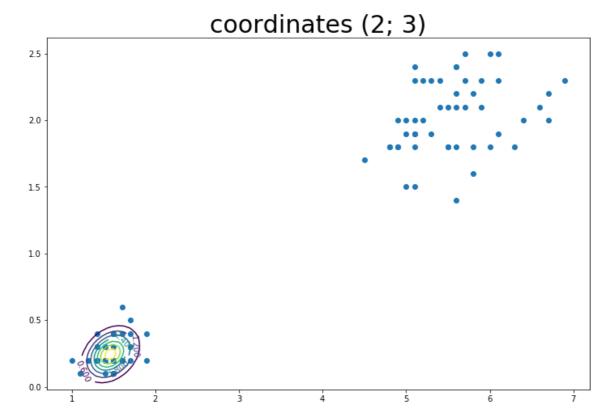
T
eq 2

In [36]:

deal_with_k(2)







T
eq 3

In [37]:

 $deal_with_k(3)$

