## CPS843 Introduction to Computer Vision, Winter 2020: Assignment 4

Due: April 24th, 11:59pm

All programming questions are to be completed in MATLAB. You will be working individually on this assignment. Include a file that will step through the answers to the entire assignment, and name this file a4\_script.m.

Do not discuss or share code with others or use code from the web (other than the code instructed to use). We will be checking for plagiarism using MOSS and reserve the right to give offenders (both copier and source) a zero on this assignment and pursue academic sanctions. Finally, we may ask you to explain the details about the answers in your submission. If you cannot explain how you arrived at the answer, you will receive a zero on that part of the assignment.

## 1 Convolution (15 points)

In MATLAB, if you place the command tic before your script and toc after your script, MATLAB will return the total execution time.

- 1. **[5 points]** Use conv2 to convolve an image by a 2D Gaussian kernel in the spatial domain. Plot the execution time to perform convolution on a 640×480 image using the following dimensions for the Gaussian kernel: 3×3, 5×5, 7×7, 13×13, 21×21, 31×31, 41×41, 51×51 and 71×71. Use MATLAB's plot function to plot the kernel size (horizontal dimension) vs. the execution time (vertical dimension).
- 2. **[5 points]** Perform convolution in the frequency domain (i.e., DFT, multiply and inverse DFT), plot the time taken to convolve a  $640 \times 480$  image with a 2D Gaussian kernel with the following dimensions:  $3 \times 3$ ,  $5 \times 5$ ,  $7 \times 7$ ,  $13 \times 13$ ,  $21 \times 21$ ,  $31 \times 31$ ,  $41 \times 41$ ,  $51 \times 51$  and  $71 \times 71$ . Overlay this plot onto the spatial convolution plot from the previous question using MATLAB's hold on function.
- 3. **[5 points]** Describe the plots you just generated. What conclusions can you draw between spatial- and frequency-based convolution?

## 2 Hybrid Image (20 points)

1. **[20 points]** For this question you will create a *Hybrid image* as described in the lecture, e.g., Marilyn Monroe + Albert Einstein. The images used to generate this illusion are of your own choosing. To optimize the appeal of the illusion, you may have to: (i) adjust the alignment of the images using photo editing software (or MATLAB) and (ii) adjust the lowpass and highpass cutoff frequencies by varying the standard deviations of the Gaussians used to generate the respective filters. All filtering and image compositing should be performed in the frequency domain. Beyond technical correctness, marks will be awarded for the appeal of the illusion, so be creative.

## 3 Optical flow estimation (35 points)

In this part, you will implement the Lucas-Kanade optical flow algorithm that computes the pixelwise motion between two images in a sequence. Compute the optical flow fields for the three image sets labeled **synth**, **sphere and corridor**. Before running your code on the images, you should first convert your images to grayscale and map the intensity values to the range [0, 1].

1. [20 points] Recall from lecture, to compute the optical flow at a pixel, compute the spatial derivatives (in the first frame),  $I_x$  and  $I_y$ , compute the temporal derivative,  $I_t$ , and then over a window centred around each pixel solve the following:

$$\begin{pmatrix} \sum \sum I_x I_x & \sum \sum I_x I_y \\ \sum \sum I_x I_y & \sum \sum I_y I_y \end{pmatrix} \begin{pmatrix} u \\ v \end{pmatrix} = -\begin{pmatrix} \sum \sum I_x I_t \\ \sum \sum I_y I_t \end{pmatrix}. \tag{1}$$

Write a MATLAB function, call it myFlow, that takes as input two images, img1 and img2, the window length used to compute flow around a point, and a threshold,  $\tau$ . The function should return three images, u and v, that contain the horizontal and vertical components of the estimated optical flow, respectively, and a binary map that indicates whether the flow is valid.

To compute spatial derivatives, use the five-point derivative of Gaussian convolution filter  $(1/12)*[-1\ 8\ 0\ -8\ 1]$  (make sure the filter is flipped correctly); the image origin is located in the top-left corner of the image, with the positive direction of the x and y axes running to the right and down, respectively. To compute the temporal derivative, apply Gaussian filtering with a small  $\sigma$  value (e.g.,  $3\times 3$  filter with  $\sigma=1$ ) to both images and then subtract the first image from the second image. Since Lucas-Kanade only works for small displacements (roughly a pixel or less), you may have to resize the input images (use MATLAB's imresize) to get a reasonable flow field. Hint: The (partial) derivatives can be computed once by applying the filters across the entire image. Further, to efficiently compute the component-wise summations in (1), you can apply a smoothing filter (e.g., box filter, Gaussian, etc.) on the image containing the product of the gradients.

Recall, the optical flow estimate is only valid in regions where the  $2 \times 2$  matrix on the left side of (1) is invertible. Matrices of this type are invertible when their smallest eigenvalue is not zero, or in practice, greater than some threshold,  $\tau$ , e.g.,  $\tau = 0.01$ . At image points where the flow is not computable, set the flow value to zero.

- 2. **[5 points]** Visualize the flow fields using the function **flowToColor**. Play around with the window size and explain what effect this parameter has on the result.
- 3. [10 points] Another way to visualize the accuracy of the computed flow field is to warp img2 with the computed optical flow field and compare the result with img1. Write a function, call it myWarp, that takes img2 and the estimated flow, u and v, as input and outputs the (back)warped image. If the images are identical except for a translation and the estimated flow is correct then the warped img2 will be identical to img1 (ignoring discretization artifacts). Hint: Use MATLAB's functions interp2 (try bicubic and bilinear interpolation) and meshgrid. Be aware that interp2 may return NaNs. In particular, this may occur around the image boundaries, since data is missing to perform the interpolation. Make sure your code handles this situation in a reasonable way.

Visualize the difference between the warped img2 and img1 by: (i) take the difference between the two images and display their absolute value output (use an appropriate scale factor for imshow) and (ii) using imshow display img1 and the warped img2 consecutively in a loop for a few iterations, the output should appear approximately stationary. When running imshow in a loop, you will need to invoke the function draw now to force MATLAB to render the new image to the screen.