

## WEEK 7

**Task 1:** Accident Prediction For the table above, find the probability of the scenario being in an accident (YES or NO).

1. Objective: Calculate  $P(C1 | X = (\text{Rain, Good, Normal, No}))$ . Determine how the Bayes classifier would classify the data instance  $X = (\text{Rain, Good, Normal, No})$ .

Total instance = 10

YES = 5

NO = 5

$$P(\text{accident} = \text{yes}) = 5/10 = 0.5$$

$$P(\text{accident} = \text{no}) = 5/10 = 0.5$$

Calculating probabilities when accident = yes where  $X = (\text{rain, good, normal, no})$

$$\text{For rain; } P(\text{rain/accident} = \text{yes}) = 1/5 = 0.2$$

$$\text{For good; } p(\text{good/accident=yes}) = 1/5 = 0.2$$

$$\text{For normal; } p(\text{normal/accident=yes}) = 1/5 = 0.2$$

$$\text{For No; } p(\text{no/accident=yes}) = 2/5 = 0.4$$

Calculating probabilities when accident = No where  $X = (\text{rain, good, normal, no})$

$$\text{For rain; } P(\text{rain/accident} = \text{no}) = 2/5 = 0.4$$

$$\text{For good; } p(\text{good/accident=yes}) = 3/5 = 0.6$$

$$\text{For normal; } p(\text{normal/accident=yes}) = 2/5 = 0.4$$

$$\text{For No; } p(\text{no/accident=yes}) = 4/5 = 0.8$$

Calculating probability of X given that accident = yes,

$$P(X/\text{accident}=\text{yes}) = 0.2 * 0.2 * 0.2 * 0.4 = 0.0032$$

Calculating probability of X given that accident = No,  $P(X/\text{accident} = \text{no}) = 0.4 * 0.6 * 0.4 * 0.8 = 0.0768$

Now,

$$P(\text{accident}=\text{yes}/X) = 0.0032 * 0.5 = 0.0016$$

$$P(\text{accident}=\text{no}/X) = 0.0768 * 0.5 = 0.0384$$

**Task 2:** Weather-Based Game Prediction In this dataset, there are five categorical attributes: outlook, temperature, humidity, windy, and play. We are interested in building a system to classify whether to play based on weather conditions.

1. Question 1: Calculate  $P(C_1 | X = (\text{sunny, hot, high, false}))$ . How would the Bayes classifier classify the data instance  $X = (\text{sunny, hot, high, false})$ ?

Total instance = 14,

Yes = 9

No = 5

$$P(\text{yes}) = 9/14 = 0.64$$

$$P(\text{no}) = 5/14 = 0.36$$

Calculating probabilities for  $X$  (sunny, hot, high, false) given that play = yes

$$P(\text{sunny}/\text{play} = \text{yes}) = 2/9 = 0.2$$

$$P(\text{hot}/ \text{play} = \text{yes}) = 2/9 = 0.2$$

$$P(\text{high} / \text{play} = \text{yes}) = 3/9 = 0.3$$

$$P(\text{false}/ \text{play} = \text{yes}) = 6/9 = 0.67$$

Calculating probabilities for  $X$  (sunny, hot, high, false) given that play = No

$$P(\text{sunny}/\text{play} = \text{no}) = 3/5 = 0.6$$

$$P(\text{hot}/ \text{play} = \text{no}) = 2/5 = 0.4$$

$$P(\text{high} / \text{play} = \text{no}) = 4/5 = 0.8$$

$$P(\text{false}/ \text{play} = \text{no}) = 2/5 = 0.4$$

Calculating probability of  $X$  given that play = yes and play = no

$$P(X/\text{play} = \text{yes}) = 0.2 * 0.2 * 0.3 * 0.67 = 0.00804$$

$$P(X/\text{play} = \text{no}) = 0.6 * 0.4 * 0.8 * 0.4 = 0.0768$$

Calculating probabilities of play = yes and play = no given that  $X$

$$P(\text{play} = \text{yes}/X) = 0.00804 * 0.64 = 0.0051$$

$$P(\text{play} = \text{no}/X) = 0.0768 * 0.36 = 0.028$$

2. Question 2: Does this agree with the classification in Table 1 for  $X = (\text{sunny}, \text{hot}, \text{high}, \text{false})$ ?  
=> NO

3. Question 3: Consider a new data instance  $X' = (\text{overcast}, \text{cool}, \text{high}, \text{true})$ . How would the Bayes classifier classify  $X'$ ?

Total instance = 14,

Yes = 9

No = 5

$$P(\text{yes}) = 9/14 = 0.64$$

$$P(\text{no}) = 5/14 = 0.36$$

Calculating probabilities for  $X$  (overcast, cool, high, True) given that play = yes

$$P(\text{overcast}/\text{play} = \text{yes}) = 4/9 = 0.44$$

$$P(\text{cool}/\text{play=yes}) = 3/9 = 0.33$$

$$P(\text{high} / \text{play=yes}) = 3/9 = 0.33$$

$$P(\text{true} / \text{play=yes}) = 3/9 = 0.33$$

Calculating probabilities for  $X$  (overcast, cool, high, True) given that play = No

$$P(\text{overcast}/\text{play} = \text{no}) = 0/5 = 0$$

$$P(\text{cool} / \text{play=no}) = 1/5 = 0.2$$

$$P(\text{high} / \text{play=no}) = 4/5 = 0.8$$

$$P(\text{true} / \text{play=no}) = 3/5 = 0.6$$

Calculating probability of  $X$  given that play = yes and play = no

$$P(X/\text{play=yes}) = 0.44 * 0.33 * 0.33 * 0.33 = 0.0158$$

$$P(X/\text{play=no}) = 0 * 0.2 * 0.8 * 0.6 = 0$$

Calculating probabilities of play=yes and play=no given that  $X$

$$P(\text{play=yes}/X) = 0.0158 * 0.64 = 0.0051$$

$$P(\text{play=no}/X) = 0 * 0.36 = 0$$