

WEEK 7

Task 1: Accident Prediction For the table above, find the probability of the scenario being in an accident (YES or NO).

1. Objective: Calculate $P(C1 | X = (\text{Rain, Good, Normal, No}))$. Determine how the Bayes classifier would classify the data instance $X = (\text{Rain, Good, Normal, No})$.

Total instance = 10

YES = 5

NO = 5

$$P(\text{accident} = \text{yes}) = 5/10 = 0.5$$

$$P(\text{accident} = \text{no}) = 5/10 = 0.5$$

Calculating probabilities when accident = yes where $X = (\text{rain, good, normal, no})$

$$\text{For rain; } P(\text{rain/accident} = \text{yes}) = 1/5 = 0.2$$

$$\text{For good; } p(\text{good/accident}=\text{yes}) = 1/5 = 0.2$$

$$\text{For normal; } ,p(\text{normal/accident}=\text{yes}) = 1/5 = 0.2$$

$$\text{For No; } p(\text{no/accident}=\text{yes}) = 2/5 = 0.4$$

Calculating probabilities when accident = No where $X = (\text{rain, good, normal, no})$

$$\text{For rain; } P(\text{rain/accident} = \text{no}) = 2/5 = 0.4$$

$$\text{For good; } p(\text{good/accident}=\text{yes}) = 3/5 = 0.6$$

$$\text{For normal; } ,p(\text{normal/accident}=\text{yes}) = 2/5 = 0.4$$

$$\text{For No; } p(\text{no/accident}=\text{yes}) = 4/5 = 0.8$$

Calculating probability of X given that accident =yes,

$$P(X/\text{accident}=\text{yes}) = 0.2*0.2*0.2*0.4 = 0.0032$$

Calculating probability of X given that accident =No, $P(X/\text{accident} = \text{no}) = 0.4*0.6*0.4*0.8 = 0.0768$

Now,

$$P(\text{accident}=\text{yes}/X) = 0.0032*0.5 = 0.0016$$

$$P(\text{accident}=\text{no}/X) = 0.0768*0.5 = 0.0384$$

Task 2: Weather-Based Game Prediction In this dataset, there are five categorical attributes: outlook, temperature, humidity, windy, and play. We are interested in building a system to classify whether to play based on weather conditions.

1. Question 1: Calculate $P(C1 \mid X = (\text{sunny, hot, high, false}))$. How would the Bayes classifier classify the data instance $X = (\text{sunny, hot, high, false})$?

Total instance = 14,

Yes = 9

No = 5

$P(\text{yes}) = 9/14 = 0.64$

$P(\text{no}) = 5/14 = 0.36$

Calculating probabilities for $X = (\text{sunny, hot, high, false})$ given that $\text{play} = \text{yes}$

$P(\text{sunny}/\text{play} = \text{yes}) = 2/9 = 0.2$

$P(\text{hot}/\text{play} = \text{yes}) = 2/9 = 0.2$

$P(\text{high}/\text{play} = \text{yes}) = 3/9 = 0.3$

$P(\text{false}/\text{play} = \text{yes}) = 6/9 = 0.67$

Calculating probabilities for $X = (\text{sunny, hot, high, false})$ given that $\text{play} = \text{No}$

$P(\text{sunny}/\text{play} = \text{no}) = 3/5 = 0.6$

$P(\text{hot}/\text{play} = \text{no}) = 2/5 = 0.4$

$P(\text{high}/\text{play} = \text{no}) = 4/5 = 0.8$

$P(\text{false}/\text{play} = \text{no}) = 2/5 = 0.4$

Calculating probability of X given that $\text{play} = \text{yes}$ and $\text{play} = \text{no}$

$P(X/\text{play} = \text{yes}) = 0.2 * 0.2 * 0.3 * 0.67 = 0.00804$

$P(X/\text{play} = \text{no}) = 0.6 * 0.4 * 0.8 * 0.4 = 0.0768$

Calculating probabilities of $\text{play} = \text{yes}$ and $\text{play} = \text{no}$ given that X

$P(\text{play} = \text{yes}/X) = 0.00804 * 0.64 = 0.0051$

$P(\text{play} = \text{no}/X) = 0.0768 * 0.36 = 0.028$

2. Question 2: Does this agree with the classification in Table 1 for $X = (\text{sunny, hot, high, false})$?
=> NO

3. Question 3: Consider a new data instance $X' = (\text{overcast, cool, high, true})$. How would the Bayes classifier classify X' ?

Total instance = 14,

Yes = 9

No = 5

$P(\text{yes}) = 9/14 = 0.64$

$P(\text{no}) = 5/14 = 0.36$

Calculating probabilities for X (overcast, cool, high, True) given that play = yes

$P(\text{overcast}/\text{play} = \text{yes}) = 4/9 = 0.44$

$P(\text{cool}/\text{play} = \text{yes}) = 3/9 = 0.33$

$P(\text{high} / \text{play} = \text{yes}) = 3/9 = 0.33$

$P(\text{true}/\text{play} = \text{yes}) = 3/9 = 0.33$

Calculating probabilities for X (overcast, cool, high, True) given that play = No

$P(\text{overcast}/\text{play} = \text{no}) = 0/5 = 0$

$P(\text{cool}/\text{play} = \text{no}) = 1/5 = 0.2$

$P(\text{high} / \text{play} = \text{no}) = 4/5 = 0.8$

$P(\text{true}/\text{play} = \text{no}) = 3/5 = 0.6$

Calculating probability of X given that play = yes and play = no

$P(X/\text{play} = \text{yes}) = 0.44 * 0.33 * 0.33 * 0.33 = 0.0158$

$P(X/\text{play} = \text{no}) = 0 * 0.2 * 0.8 * 0.6 = 0$

Calculating probabilities of play = yes and play = no given that X

$$P(\text{play}=\text{yes}/X) = 0.0158 \cdot 0.64 = 0.0051$$

$$P(\text{play}=\text{no}/X) = 0 \cdot 0.36 = 0$$