

Question	The value of x in the equation: $16x + \frac{1}{x} = 8$ is	
Type	multiple_choice	
Option	$\frac{1}{4}, \frac{1}{4}$	correct
Option	$\frac{1}{8}, \frac{1}{4}$	incorrect
Option	$\frac{1}{4}, \frac{1}{8}$	incorrect
Option	$\frac{1}{8}, \frac{1}{8}$	incorrect
Solution	$16x + \frac{1}{x} = 8$ $\frac{16x^2 + 1}{x} = 8$ $16x^2 + 1 = 8x$ $\Rightarrow 16x^2 + 1 - 8x = 0$ $\Rightarrow (4x - 1)^2 = 0$ $\Rightarrow x = \frac{1}{4}, \frac{1}{4}$	
Marks	4	1

Question	The equation whose roots are 4 and 5, is	
Type	multiple_choice	

Option	$x^2+9x-20=0$	incorrect
Option	$x^2+9x+20=0$	incorrect
Option	$x^2-9x+20=0$	correct
Option	$x^2-9x-20=0$	incorrect
Solution	The required equation is: $x^2-(\text{sum of roots})x+\text{product of roots}=0$ $\Rightarrow x^2-(4+5)x+4*5=0$ $\Rightarrow x^2-9x+20=0$	
Marks	4	1

Question	The roots of the equation $(x + 3) (x - 3) = 160$ are	
Type	multiple_choice	
Option	± 13	correct
Option	13,13	incorrect
Option	± 12	incorrect
Option	12,12	incorrect
Solution	$(x + 3) (x - 3) = 160$ $x^2 - 9 = 160$ $x^2 = 169$ $x = +13, - 13$	
Marks	4	1

Question	The solution of $\frac{2x+3}{2x-1} = \frac{3x-1}{3x+1}$ is	
Type	multiple_choice	
Option	$\frac{1}{8}$	incorrect
Option	$-\frac{1}{8}$	correct
Option	$\frac{1}{6}$	incorrect
Option	$-\frac{1}{6}$	incorrect
Solution	Given equation is $(2x+3)(3x+1) = (3x-1)(2x-1)$ $= 6x^2 + 11x + 3$ $= 6x^2 - 5x + 1$ $= 16x + 2$ $16x = -2$ $x = -\frac{1}{8}$	
Marks	4	1

Question	A journey of 300 km takes two hours more when the speed of a care is reduced by 5km/hr. What is the original speed of the car?	
Type	multiple_choice	
Option	30	correct
Option	40	incorrect

Option	70	incorrect
Option	80	incorrect
Solution	<p>Let the speed of the car is x km/hr. Then Speed = distance/ time:</p> $\frac{300}{x-5} - \frac{300}{x} = 2$ $\Rightarrow \frac{x-x+5}{x(x-5)} = \frac{2}{300} = \frac{1}{150}$ $x^2 - 5x - 750 = 0$ $x^2 - 30x + 25x - 750 = 0$ $(x-30)(x+25) = 0$ $x=30 \text{ or } x=-25$ <p>The negative value of x is inadmissible; therefore the speed of the car is 30 km/hr.</p>	
Marks	4	1

Question	<p>Today Madan is 20 years younger than his father. Ten years ago he was one-half as old as his father. How old his father is ten years hence?</p>	
Type	multiple_choice	
Option	40	incorrect
Option	50	correct
Option	60	incorrect

Option	Data not adequate	incorrect
Solution	<p>Let the age of Madan and his father be x and y years respectively. Then</p> $y - x = 20 \text{(i)}$ <p>Ten year ago:</p> $x - 10 = \frac{1}{2} (y - 10)$ $2(x - 10) = y - 10$ $2x - 20 = y - 10$ $2x - y = -10 + 20$ $2x - y = 10$ <p>Now solving eq.1 and eq.2:</p> $y - x = 20$ $-y + 2x = 10$ $x = 30 \text{ (age of Madan)}$ <p>So, age of his father: $y = x + 20$</p> $= 30 + 20 = 50$ <p>Madan's father age after 10 years:</p> $y + 10 = 50 + 10 = 60 \text{ years}$	
Marks	4	1

Question	The numerator of a fraction is 3 less than the denominator. If numerator be made 3 times and 20 is added to the denominator, the fraction becomes $\frac{1}{8}$. What is the fraction?	
Type	multiple_choice	
Option	420, 489 cm ²	incorrect
Option	520, 494 cm ²	incorrect
Option	620, 482 cm ²	incorrect
Option	520, 486 cm ²	correct
Solution	<p>Given: Dimension of cuboid = 117 cm × 72 cm × 45 cm Side of a cube = 9 cm Formula used: Volume of the cuboid = (l × b × h) Where, l = length, b = width, h = height Volume of cube = (side)³ Total surface area of cube = 6 × (side)² Calculation: Let the number of cubes be n Volume of cuboid = n × volume of cube $\Rightarrow 117 \times 72 \times 45 = n \times (9)^3$ $\Rightarrow n = 13 \times 8 \times 5$ $\Rightarrow n = 520$ Total surface area of one cube = 6 × (side)² \Rightarrow Total surface area of one cube = 6 × (9)² \Rightarrow Total surface area of one cube = 486 cm² \therefore The number of cubes and the total surface area of a cube are 520 and 486 cm².</p>	
Marks	4	1

Question	If $x = \frac{(\sqrt{2} + 1)}{(\sqrt{2} - 1)}$, then what is the value of $(x^5 + x^4 + x^2 + x)/x^3$?	
Type	multiple_choice	
Option	40	correct
Option	39	incorrect

Option	38.5	incorrect
Option	41	incorrect
Solution	<p>Given: $x = (\sqrt{2} + 1)/(\sqrt{2} - 1)$</p> <p>Multiplying numerator and denominator by $(\sqrt{2} + 1)$, we get</p> $\Rightarrow x = (\sqrt{2} + 1)^2/(\sqrt{2} - 1)(\sqrt{2} + 1) = 3 + 2\sqrt{2}$ <p>To find: $(x^5 + x^4 + x^2 + x)/x^3$</p> $\Rightarrow x^2 + x + 1/x + 1/x^2$ <p>Calculating $x + 1/x$, we get</p> $3 + 2\sqrt{2} + [1/(3 + 2\sqrt{2})] = [(3 + 2\sqrt{2})^2 + 1]/(3 + 2\sqrt{2})$ $\Rightarrow (9 + 8 + 12\sqrt{2} + 1)/(3 + 2\sqrt{2})$ $\Rightarrow 6(3 + 2\sqrt{2})/(3 + 2\sqrt{2})$ $\Rightarrow 6$ <p>Now, $x^2 + x + 1/x + 1/x^2 = (x + 1/x)^2 - 2 + (x + 1/x)$</p> <p>Substituting $(x + 1/x) = 6$, we get</p> $\Rightarrow 6^2 - 2 + 6 = 40$	
Marks	4	1

Question	Find the values of a and b so that $x^4 + x^3 + 8x^2 + ax + b$ is divisible by $x^2 - 1$.	
Type	multiple_choice	
Option	a = 1, b = 7	incorrect
Option	a = -1, b = 7	incorrect
Option	a = -1, b = -7	incorrect
Option	a = -1, b = -9	correct

Solution	<p>We are looking for values of a and b such that the polynomial $x^4 + x^3 + 8x^2 + ax + b$ is divisible by $x^2 - 1$. This means the remainder when dividing this polynomial by $x^2 - 1$ should be 0.</p> <p>We can use the fact that if a polynomial $f(x)$ is divisible by $x^2 - 1$, then the polynomial must have $f(1) = 0$ and $f(-1) = 0$.</p> <p>Calculate $f(1)$ and $f(-1)$</p> <p>Let $f(x) = x^4 + x^3 + 8x^2 + ax + b$.</p> <p>For $f(1) = 0$:</p> $f(1) = 1^4 + 1^3 + 8(1^2) + a(1) + b = 1 + 1 + 8 + a + b = 10 + a + b$ <p>So $10 + a + b = 0$</p> $\Rightarrow a + b = -10 \quad (\text{Equation 1})$ <p>For $f(-1) = 0$:</p> $f(-1) = (-1)^4 + (-1)^3 + 8(-1)^2 + a(-1) + b = 1 - 1 + 8 - a + b = 8 - a + b$ <p>So $8 - a + b = 0$</p> $\Rightarrow -a + b = -8 \quad (\text{Equation 2})$ <p>To solve, add both equations:</p> $(a + b) + (-a + b) = -10 + (-8)$ $\Rightarrow 2b = -18$ $\Rightarrow b = -9$ <p>Substitute $b = -9$ into Equation 1</p> $a + (-9) = -10$ $\Rightarrow a = -1$	
Marks	4	1

Question	Three consecutive integers add up to 54. What is the largest integer?	
Type	multiple_choice	
Option	18	incorrect
Option	15	incorrect

Option	17	incorrect
Option	19	correct
Solution	<p> x (the smallest integer), $x + 1$ (the middle integer), $x + 2$ (the largest integer). </p> <p>The sum of these three integers is given as 54:</p> $x + (x + 1) + (x + 2) = 54$ $\Rightarrow x + x + 1 + x + 2 = 54$ <p>This simplifies to:</p> $3x + 3 = 54$ $\Rightarrow 3x = 51$ $\Rightarrow x = \frac{51}{3} = 17$ <p>The first integer $x = 17$,</p> <p>The second integer is $x + 1 = 18$,</p> <p>The third (largest) integer is $x + 2 = 19$.</p>	
Marks	4	1

Question	The difference between the squares of two consecutive numbers is 95. Find the numbers.	
Type	multiple_choice	
Option	29,30	incorrect
Option	47,48	correct
Option	45,46	incorrect
Option	48,49	incorrect

Solution	<p>Let the two consecutive numbers be x and $x + 1$.</p> <p>Expanding the squares:</p> $a^2 - b^2 = (a - b)(a + b)$ $(x + 1)^2 - x^2$ $\Rightarrow (x + 1)^2 - x^2 = (x + 1 - x)(x + 1 + x) = 1(2x + 1) = 2x + 1$ $\Rightarrow 2x + 1 = 95$ $\Rightarrow x = \frac{94}{2} = 47$ <p>The two consecutive numbers are $x = 47$ and $x + 1 = 48$.</p> <p>The two numbers are 47 and 48 .</p>	
Marks	4	1

Question	If $x = \sqrt{10 + 3}$ then find the value of $x^3 - 1/x^3$	
Type	multiple_choice	
Option	210	incorrect
Option	234	correct
Option	220	incorrect
Option	235	incorrect

Solution	$x = \sqrt{10} + 3$ Formula used: If $x - \frac{1}{x} = a$ $\Rightarrow x^3 - \frac{1}{x^3} = a^3 + 3a$ Calculation: $x = \sqrt{10} + 3$ $\Rightarrow 1/x = \sqrt{10} - 3$ $\Rightarrow x - \frac{1}{x} = 6$ $\Rightarrow x^3 - \frac{1}{x^3} = 6^3 + 3 \times 6$ $\Rightarrow x^3 - \frac{1}{x^3} = 234$ \therefore The required value is 234.	
Marks	4	1

Question	If $a = 2.234$, $b = 3.121$ and $c = -5.355$, then the value of $a^3 + b^3 + c^3 - 3abc$ is	
Type	multiple_choice	
Option	1	incorrect
Option	-1	incorrect
Option	2	incorrect
Option	0	correct
Solution	$a + b + c = 2.234 + 3.121 - 5.355 = 0$ If $a + b + c = 0$, then $a^3 + b^3 + c^3 - 3abc = 0$, which can be proved as under $a + b = -c$ Cubing both sides, we get $(a + b)^3 = (-c)^3$	

	$\Rightarrow a^3 + b^3 + 3ab(a + b) = -c^3$ $\Rightarrow a^3 + b^3 + 3ab(-c) = -c^3$ $\Rightarrow a^3 + b^3 - 3abc = -c^3$ $\Rightarrow a^3 + b^3 + c^3 - 3abc = 0$	
Marks	4	1

Question	<p>Consider the following statements</p> <p>I. $x + 3$ is the factor of $x^3 + 2x^2 + 3x + 8$.</p> <p>II. $x - 2$ is the factor of $x^3 + 2x^2 + 3x + 8$.</p> <p>Which of the statements given above is/are correct?</p>	
Type	multiple_choice	
Option	Only I	incorrect
Option	Only II	incorrect
Option	Both I and II	incorrect
Option	Neither I nor II	correct

Solution	<p>Put $x = -3$ in equation $x^3 + 2x^2 + 3x + 8$</p> $= (-3)^3 + 2(-3)^2 + 3(-3) + 8$ $= -10 \neq 0$ <p>So, $(x + 3)$ is not the factor of $x^3 + 2x^2 + 3x + 8$</p> <p>Similarly, put $x = 2$ in above equation</p> $= (2)^3 + 2(2)^2 + 3(2) + 8$ $= 30 \neq 0$ <p>So, $(x - 2)$ is also not the factor of $x^3 + 2x^2 + 3x + 8$.</p>	
Marks	4	1

Question	If $3x^4 - 2x^3 + 3x^2 - 2x + 3$ is divided by $(3x + 2)$, then the remainder is	
Type	multiple_choice	
Option	0	incorrect
Option	181/27	incorrect
Option	185/27	correct
Option	$\frac{3}{4}$	incorrect

Solution	$f(x) = 3x^4 - 2x^3 + 3x^2 - 2x + 3$ $(3x + 2) = 0 \Rightarrow x = -\frac{2}{3}$ $\text{Remainder} = f\left(-\frac{2}{3}\right) = 3\left(-\frac{2}{3}\right)^4 - 2\left(-\frac{2}{3}\right)^3 + 3\left(-\frac{2}{3}\right)^2 - 2\left(-\frac{2}{3}\right) + 3$ $= 3 \times \frac{16}{81} - 2 \times \frac{-8}{27} + 3 \times \frac{4}{9} + \frac{4}{3} + 3$ $= \frac{16}{27} + \frac{16}{27} + \frac{4}{3} + \frac{4}{3} + 3 = \frac{32}{27} + \frac{8}{3} + 3$ $= \frac{32 + 72 + 81}{27} = \frac{185}{27}$	
Marks	4	1

Question	<p>If $\frac{5x}{2x^2 + 5x + 1} = \frac{1}{3}$, then the value of $\left(x + \frac{1}{2x}\right)$ is</p>	
Type	multiple_choice	
Option	10	incorrect
Option	20	incorrect
Option	5	correct
Option	0	incorrect

Solution

$$\frac{5x}{2x^2 + 5x + 1} = \frac{1}{3}$$

Dividing numerator & denominator by $2x$

$$= \frac{\frac{5}{2}}{x + \frac{5}{2} + \frac{1}{2x}} = \frac{1}{3}$$

$$= \frac{\frac{5}{2}}{x + \frac{1}{2x} + \frac{5}{2}} = \frac{1}{3}$$

$$\Rightarrow \left(x + \frac{1}{2x}\right) + \frac{5}{2} = \frac{15}{2}$$

$$\Rightarrow \left(x + \frac{1}{2x}\right) = \frac{15}{2} - \frac{5}{2}$$

$$\Rightarrow \left(x + \frac{1}{2x}\right) = 5$$

Marks

4

1

Question	If $p^3 + 3p^2 + 3p = 7$, then the value of $p^2 + 2p$ is	
Type	multiple_choice	
Option	3	correct
Option	2	incorrect
Option	5	incorrect
Option	1	incorrect
Solution	$p^3 + 3p^2 + 3p = 7$ $\Rightarrow p^3 + 3p^2 + 3p + 1 = 7 + 1 = 8$ $\Rightarrow (p + 1)^3 = (2)^3$ $\Rightarrow p + 1 = 2 \Rightarrow p = 1$ $\therefore p^2 + 2p = 1 + 2 \times 1 = 1 + 2 = 3.$	
Marks	4	1

Question	If $a + b + c = 0$, then the value of $(a + b - c)^2 + (b + c - a)^2 + (c + a - b)^2$ is	
Type	multiple_choice	
Option	8 abc	incorrect
Option	$4(a^2 + b^2 + c^2)$	correct
Option	$4(ab + bc + ca)$	incorrect
Option	0	incorrect

Solution	<p>Given, $a + b + c = 0$</p> <p>$\therefore a + b = -c, b + c = -a, c + a = -b$</p> <p>$\therefore (a + b - c)^2 + (b + c - a)^2 + (c + a - b)^2$</p> <p>$\Rightarrow (-c - c)^2 + (-a - a)^2 + (-b - b)^2$</p> <p>$\Rightarrow (-2c)^2 + (-2a)^2 + (-2b)^2$</p> <p>$\Rightarrow 4c^2 + 4a^2 + 4b^2 = 4(a^2 + b^2 + c^2)$</p>	
Marks	4	1

Question	<p>If $x + \frac{1}{x} = 2$ and x is real, then the value of $x^{17} + \frac{1}{x^{19}}$ is</p>	
Type	multiple_choice	
Option	2	correct
Option	64	incorrect
Option	1	incorrect
Option	0	incorrect

Solution	<p>Given, $x + \frac{1}{x} = 2$</p> $\Rightarrow x^2 + 1 = 2x \Rightarrow x^2 + 1 - 2x = 0$ $\Rightarrow x^2 - 2x + 1 = 0 \Rightarrow (x - 1)^2 = 0 \Rightarrow x = 1$ $\therefore x^{17} + \frac{1}{x^{19}} = 1 + 1 = 2.$	
Marks	4	1

Question	If $X + 1/X = \sqrt{5}$ then find $\sqrt{x}(\sqrt{x}-1)$	
Type	multiple_choice	
Option	1	correct
Option	5	incorrect
Option	2	incorrect
Option	4	incorrect

Solution	$x^2 + \frac{1}{x^2} = 7$ $x + \frac{1}{x} = 3$ $x - \frac{1}{x} = \sqrt{5}$ $2x = 3 + \sqrt{5}$ $x = \frac{3 + \sqrt{5}}{2}$ $x = \frac{6 + 2\sqrt{5}}{4}$ $x = \left(\frac{\sqrt{5} + 1}{2}\right)^2$ $\sqrt{x} = \frac{\sqrt{5} + 1}{2}$ $\sqrt{x} (\sqrt{x} - 1) = \left(\frac{\sqrt{5} + 1}{2}\right) \left(\frac{\sqrt{5} + 1}{2} - 1\right)$ $= \frac{\sqrt{5} + 1}{2} \times \frac{\sqrt{5} - 1}{2} = \frac{5 - 1}{4} = 1$	
Marks	4	1

Question	If $\frac{a^2 + b^2 + c^2}{a^2 - b^2 - c^2} + \frac{b^2 + c^2 + a^2}{b^2 - c^2 - a^2} + \frac{c^2 + a^2 + b^2}{c^2 - a^2 - b^2} = ?$	
Type	multiple_choice	
Option	4	incorrect
Option	8	incorrect
Option	2	incorrect
Option	0	correct
Solution	$\frac{a^2 + b^2 + c^2}{a^2 - b^2 - c^2} + \frac{b^2 + c^2 + a^2}{b^2 - c^2 - a^2} + \frac{c^2 + a^2 + b^2}{c^2 - a^2 - b^2} - 3 + 3$ $= \frac{a^2 + b^2 + c^2 + a^2 - b^2 - c^2}{a^2 - b^2 - c^2} + \frac{b^2 + c^2 + a^2 + b^2 - c^2 - a^2}{b^2 - c^2 - a^2}$ $+ \frac{c^2 + a^2 + b^2 + c^2 - a^2 - b^2}{c^2 - a^2 - b^2} - 3$	

$$= \frac{2a^2}{a^2 - b^2 - c^2} + \frac{2b^2}{b^2 - c^2 - a^2} + \frac{2c^2}{c^2 - a^2 - b^2} - 3$$

Now, $a + b = c$

$$a = c - b$$

$$a^2 - b^2 - c^2 = -2bc \dots\dots\dots(i)$$

and $a + b = c$

$$b = c - a$$

$$b^2 - c^2 - a^2 = -2ac \dots\dots\dots(ii)$$

and $a + b = c$

$$c^2 - a^2 - b^2 = 2ab \dots\dots\dots(iii)$$

$$a + b = c$$

$$a + b - c = 0$$

$$a^3 + b^3 - c^3 = -3abc \dots\dots\dots(iv)$$

$$-a^3 - b^3 + c^3 = 3abc$$

	$= \frac{2a^2}{-2bc} + \frac{2b^2}{-2ac} + \frac{2c^2}{2ab} - 3$ $= \frac{-a^2}{bc} - \frac{b^2}{ac} + \frac{c^2}{ab} - 3$ $= \frac{-a^3 - b^3 + c^3}{abc} - 3$ $= \frac{3abc}{abc} - 3$ $= 0$	
Marks	4	1

Question	If $x + \frac{1}{x} = 0$ then $x^{12} + x^{14} + x^{16} + x^{18} = ?$	
Type	multiple_choice	
Option	1	incorrect
Option	-1	incorrect
Option	2	incorrect
Option	0	correct

Solution	$x + \frac{1}{x} = 0$ $x^2 + 1 = 0$ $x^2 = -1$ $x^4 = 1$ $x^{12} + x^{14} + x^{16} + x^{18} = (x^4)^3 + (x^2)^7 + (x^4)^4 + (x^2)^9$ $= 1 - 1 + 1 - 1$ $= 0$	
Marks	4	1

Question	(x - 3) (y + 4) = 12. How many pairs of integers (x,y) satisfy this equation?	
Type	multiple_choice	
Option	10	correct
Option	8	incorrect
Option	9	incorrect
Option	12	incorrect

Solution	<p>If x and y are integers, so are $x - 3$ and $y + 4$. So, we start by finding out in how many ways 12 can be written as the product of two integers.</p> <p>12 can be written as $12 * 1$, or $6 * 2$, or $3 * 4$. To start with, we can eliminate the possibilities where the two terms are negative as $y + 4$ cannot be negative.</p> <p>Further, we can see that $y + 4$ cannot be less than 4. So, among the values, we can have $y + 4$ take values 4, 6 or 12 only, or y can take values 0, 2 and 8 only.</p> <p>When $y = 0$, $x - 3 = 3$, $x = 6$, x can be +6 or -6. Two pairs of values are possible: (6, 0) and (-6, 0)</p> <p>When $y = 2$, $x - 3 = 2$, $x = 5$, x can be +5 or -5. There are four possible pairs here: (5, 2), (-5, 2), (5, -2), (-5, -2)</p> <p>When $y = 8$, $x - 3 = 1$, $x = 4$, x can be +4 or -4. There are four possible pairs here: (4, 8), (-4, 8), (4, -8), (-4, -8)</p> <p>The question is "$(x - 3)(y + 4) = 12$. How many pairs of integers (x,y) satisfy this equation?"</p> <p>Hence the answer is "10"</p>	
Marks	4	1

Question	$x + y = 8$, $ x + y = 6$. How many pairs of x, y satisfy these two equations?	
Type	multiple_choice	
Option	1	correct
Option	0	incorrect
Option	2	incorrect
Option	4	incorrect

Solution	<p>The first equation is a pair of lines defined by the equations</p> $y = 8 - x \text{ ----- (i) (when y is positive)}$ $y = x - 8 \text{ ----- (ii) (when y is negative)}$ <p>With the condition that $x \leq 8$ (because if x becomes more than 8, y will be forced to be negative, which is not allowed)</p> <p>The second equation is a pair of lines defined by the equations:</p> $y = 6 - x \text{ ----- (iii) (when x is positive)}$ $y = 6 + x \text{ ----- (iv) (when x is negative)}$ <p>with the condition that y cannot be greater than 6, because if $y > 6$, x will have to be negative.</p> <p>On checking for the slopes, you will see that lines (i) and (iii) are parallel. Also (ii) and (iv) are parallel (same slope).</p> <p>Lines (i) and (iv) will intersect, but only for $x = 1$; which is not possible as equation (iv) holds good only when x is negative.</p> <p>Lines (ii) and (iii) do intersect within the given constraints. We get $x = 7, y = -1$. This satisfies both equations. Only one solution is possible for this system of equations.</p> <p>The question is "$x + y = 8, x + y = 6$. How many pairs of x, y satisfy these two equations?"</p> <p>Hence the answer is "1"</p>	
Marks	4	1

Question	$X^2 - 9x + k = 0$ has real roots. How many integer values can 'k' take?	
Type	multiple_choice	
Option	45	incorrect
Option	43	incorrect
Option	42	incorrect
Option	41	correct

Solution	<p>Discriminant, $D = 81 - 4 k$</p> <p>If roots are real, $D > 0$</p> $81 - 4 k > 0$ $4 k < 81$ $ k < 20.25$ <p>Hence, $-20.25 < k < 20.25$</p> <p>The integer values that k can take are $-20, -19, -18 \dots 0 \dots 18, 19$ and 20.</p> <p>41 different values (Remember to include 0.)</p> <p>The question is "$x^2 - 9x + k = 0$ has real roots. How many integer values can 'k' take?"</p> <p>Hence the answer is "41"</p>	
Marks	4	1

Question	$2x + 5y = 103$. Find the number of pairs of positive integers x and y that satisfy this equation?	
Type	multiple_choice	
Option	20	incorrect
Option	8	incorrect
Option	12	incorrect
Option	10	correct
Solution	<p>Rearranging the equation, we get:</p> $2x = 103 - 5y$ <p>This says that when you subtract a multiple of 5 from 103, you get an even number. You have to subtract an odd multiple of 5 from 103 in order to get an even number. There are 20 multiples of 5 till 100, ten of which are odd. (Note that you cannot subtract 105, or higher multiples as they result in a negative value for x.)</p> <p>So, y can have ten integer values. x also has 10 integer values, each corresponding to a particular value of y. $y = 1$, gives us a potential value for x, so do $y = 3, 5, 7 \dots 19$. y can take 10 values totally.</p> <p>The question is "Find the number of pairs of positive integers x and y that satisfy this equation? "</p> <p>Hence the answer is "10"</p>	

Marks	4	1
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Question	Equation $x^2 + 5x - 7 = 0$ has roots a and b. Equation $2x^2 + px + q = 0$ has roots a + 1 and b + 1. Find p + q?	
Type	multiple_choice	
Option	2	incorrect
Option	0	incorrect
Option	16	incorrect
Option	-16	correct
Solution	<p>Given, $x^2 + 5x - 7 = 0$ has roots a and b. We know that,</p> <p>Sum of roots in a quadratic equation = $a+b = \frac{(-5)}{1} = -5$.</p> <p>Product of the roots = $ab = \frac{(-7)}{1} = -7$.</p> <p>Now, The second equation $2x^2 + px + q = 0$ has roots a + 1 and b + 1.</p> <p>Sum of the roots = $a+1+b+1 = a+b+2 = \frac{(-p)}{2} = -5+2 = -3 = \frac{(-p)}{2} \Rightarrow -p = -6 \Rightarrow p = 6$.</p> <p>Product of the roots = $(a+1)(b+1) = ab+a+b+1 = \frac{q}{2}$. We know the values of ab and a+b. Substituting this, we get, $-7+(-5)+1 = \frac{q}{2} \Rightarrow -11 = \frac{q}{2} \Rightarrow q = -22$.</p> <p>Hence, p = 6 and q = -22. $\Rightarrow p+q = 6+(-22) = -16$.</p> <p>The question is "Equation $x^2 + 5x - 7 = 0$ has roots a and b. Equation $2x^2 + px + q = 0$ has roots a + 1 and b + 1. Find p + q?"</p> <p>Hence the answer is "-16"</p>	
Marks	4	1

Question	Calculate the value of r from the equation $ab - 3a + 5b + r$?
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Type	multiple_choice	
Option	-15	incorrect
Option	7	incorrect
Option	-9	incorrect
Option	31	correct
Solution	<p>On factorizing the equation $ab - 3a + 5b + r$ we get</p> $= a(b-3)+5(b-3)= ab - 3a + 5b - 15$ <p>Therefore $r = -15$</p>	
Marks	4	1

Question	<p>A mother said to her daughter, "When you were born, I was as old as you are now." If the mother's age is 36 years at present, find the daughter's age four years back.</p>	
Type	multiple_choice	
Option	8 years	incorrect
Option	10 yeas	incorrect
Option	12 years	incorrect
Option	14 years	correct
Solution	<p>If we mark a daughter's current age as x.</p> <p>Then, her mother's age at the time of her daughter's birth will be,</p> $(36-x) = x$ $2x = 36$ $X = 18.$	

	<p>Therefore, if the daughter is 18 years old at present then her age four years back will be,</p> $18 - 4 = 14 \text{ years}$	
Marks	4	1

Question	The sum of values of x satisfying $x^{2/3} + x^{1/3} = 2$ is:	
Type	multiple_choice	
Option	-3	incorrect
Option	3	incorrect
Option	7	incorrect
Option	-7	correct
Solution	<p>$(a + b)^3 = a^3 + b^3 + 3ab(a + b)$</p> <p>Calculation:</p> $\Rightarrow x^{2/3} + x^{1/3} = 2$ $\Rightarrow (x^{2/3} + x^{1/3})^3 = 2^3$ $\Rightarrow x^2 + x + 3x(x^{2/3} + x^{1/3}) = 8$ $\Rightarrow x^2 + 7x - 8 = 0$ $\Rightarrow x^2 + 8x - x - 8 = 0$ $\Rightarrow x(x + 8) - 1(x + 8) = 0$ $\Rightarrow x = -8 \text{ or } x = 1$ <p>\therefore Sum of values of x = $-8 + 1 = -7$.</p>	
Marks	4	1