

```
import numpy as np import matplotlib.pyplot
```

```
as plt
```

```
# Step 1: Input x and y values x = np.array(list(map(float, input("Enter the values of x
(separated by spaces): ").split())) y = np.array(list(map(float, input("Enter the values of y
(separated by spaces): ").split()))
```

```
# Step 2: Calculate the slope (m) and intercept (b) n = len(x)
```

```
# Calculate sums sum_x = np.sum(x)
```

```
sum_y = np.sum(y) sum_x_squared
```

```
= np.sum(x**2) sum_xy = np.sum(x
```

```
* y)
```

```
# Calculate slope (m) m = (n * sum_xy - sum_x * sum_y) / (n * sum_x_squared
- sum_x**2)
```

```
# Calculate intercept (b) b =
```

```
(sum_y - m * sum_x) / n
```

```
# Step 3: Print intermediate values and final results print(f"Sum of x:
```

```
{sum_x}")
```

```
print(f"Sum of y: {sum_y}") print(f"Sum of x^2: {sum_x_squared}") print(f"Sum of xy:
```

```
{sum_xy}") print(f"Slope (m) = (n * sum(xy) - sum(x) * sum(y)) / (n * sum(x^2) -
```

```
(sum(x)^2)") print(f"Slope (m) = ({n} * {sum_xy} - {sum_x} * {sum_y}) / ({n} *
```

```
{sum_x_squared} - {sum_x}^2)")
```

```
print(f"Slope
```

```
(m) = {m:.2f}")
```

```
print(f"Intercept (b) = (sum(y) - m * sum(x)) / n") print(f"Intercept
```

```
(b) = ({sum_y} - {m:.2f} * {sum_x}) / {n}") print(f"Intercept (b) =
```

```
{b:.2f}")
```

```
# Step 4: Print the equation of the line print(f"The equation of the regression
```

```
line is: y = {m:.2f}x + {b:.2f}")
```

```
# Step 5: Plot the data points and the regression line plt.scatter(x, y, color='blue',
```

```
label='Data points') # Scatter plot for the data points plt.plot(x, m * x + b, color='red',
```

```
label='Regression line') # Plot the regression line plt.xlabel('x') plt.ylabel('y')
```

```
plt.legend() plt.title('Linear Regression: Data Points & Regression Line') plt.grid(True)
```

```
plt.show()
```

Enter the values of x (separated by spaces): 1 2 3 4 5 6 7 8 9

Enter the values of y (separated by spaces): 9 8 7 6 5 4 3 2 1

Sum of x: 45.0

Sum of y: 45.0

Sum of x<sup>2</sup>: 285.0

Sum of xy: 165.0

Slope (m) = (n \* sum(xy) - sum(x) \* sum(y)) / (n \* sum(x<sup>2</sup>) - (sum(x))<sup>2</sup>)

Slope (m) = (9 \* 165.0 - 45.0 \* 45.0) / (9 \* 285.0 - 45.0<sup>2</sup>)

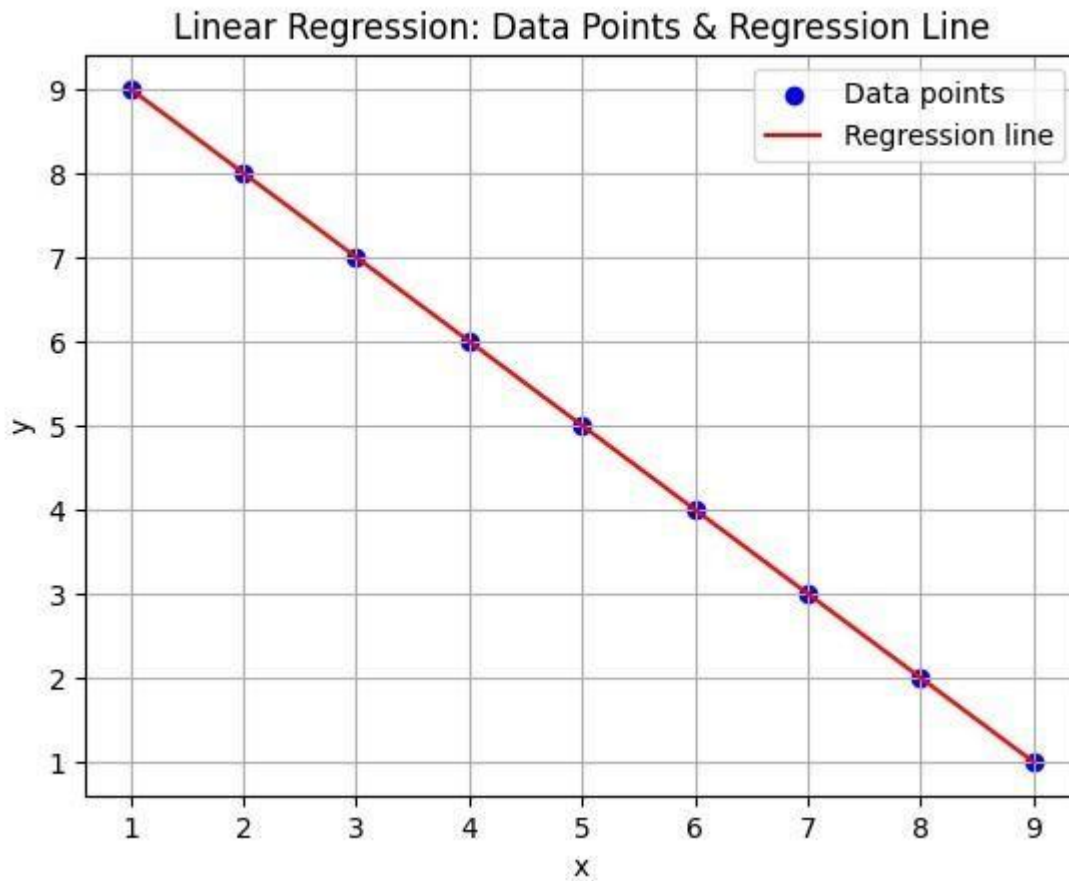
Slope (m) = -1.00

Intercept (b) = (sum(y) - m \* sum(x)) / n

Intercept (b) =  $(45.0 - -1.00 * 45.0) / 9$

Intercept (b) = 10.00

The equation of the regression line is:  $y = -1.00x + 10.00$



```
import numpy as np import matplotlib.pyplot
```

```
as plt
```

```
# Step 1: Input the number of independent variables (features) num_features =  
int(input("Enter the number of features (independent variables): "))
```

```
# Step 2: Input x values (features) and y values (dependent variable) x  
= [] for i in range(num_features):
```

```
x_i = list(map(float, input(f"Enter the values for x{i+1} (separated by spaces): ").split()))
x.append(x_i)
```

```
x = np.array(x).T # Transpose the input to make each row a data point y =
np.array(list(map(float, input("Enter the values of y (dependent variable, separated by
spaces): ").split()))
```

```
# Step 3: Add a column of ones to x for the intercept term (bias)
```

```
X = np.c_[np.ones(x.shape[0]), x]
```

```
# Step 4: Calculate the coefficients using the Normal Equation
```

```
# The normal equation is:  $\theta = (X^T * X)^{-1} * X^T * y$ 
```

```
X_transpose = X.T
```

```
X_transpose_X = X_transpose @ X
```

```
X_transpose_X_inv = np.linalg.inv(X_transpose_X)
```

```
X_transpose_y = X_transpose @ y theta =
```

```
X_transpose_X_inv @ X_transpose_y
```

```
# Step 5: Print the intermediate calculations print("\nIntermediate
```

```
Calculations:") print(f" $X^T$ 
```

```
(Transposed X):  $\{X_{transpose}\}$ ") print(f" $X^T *$ 
```

```
X:  $\{X_{transpose\_X}\}$ ") print(f" $(X^T * X)^{-1}$ :
```

```
 $\{X_{transpose\_X\_inv}\}$ ") print(f" $X^T * y$ :
```

```
 $\{X_{transpose\_y}\}$ ") print(f"Coefficients (theta):
```

```
 $\{\theta\}$ ")
```

```
# Step 6: Print the regression equation
```

```
print("\nRegression Equation:") print("The
```

```

regression equation is: y = ", end="") for i in range(1,
len(theta)):
    print(f"{theta[i]:.2f}*x{i} + ", end="") print(f"{theta[0]:.2f}")

# Intercept term

# Step 7: Plotting

# Since it's difficult to visualize in higher dimensions, we'll just plot the first two features for
demonstration if num_features >= 2:

fig = plt.figure() ax = fig.add_subplot(111, projection='3d') ax.scatter(x[:,
0], x[:, 1], y, color='blue', label='Data points')

# Create a meshgrid for prediction surface x0_vals = np.linspace(np.min(x[:,
0]), np.max(x[:, 0]), 10) x1_vals = np.linspace(np.min(x[:, 1]), np.max(x[:, 1]),
10)

X0, X1 = np.meshgrid(x0_vals, x1_vals)

Z = theta[0] + theta[1]*X0 + theta[2]*X1

# Plot the regression plane ax.plot_surface(X0, X1, Z, color='red', alpha=0.5)
ax.set_xlabel('Feature 1') ax.set_ylabel('Feature 2') ax.set_zlabel('y')
plt.title('Multivariable Regression: Data points and Regression Plane')
plt.show()

```

Intermediate Calculations:

$X^T$  (Transposed X):

```

[[1. 1. 1. 1. 1. 1. 1. 1. 1.]
 [1. 2. 3. 4. 5. 6. 7. 8. 9.] [2.
 3. 5. 6. 7. 8. 5. 6. 3.]]  $X^T$  *

```

X:

```
[[ 9. 45. 45.]
```

```
 [45. 285. 240.]
```

```
 [45. 240. 257.]]
```

$(X^T X)^{-1}$ :

```
[[ 1.02556539 -0.05014749 -0.13274336]
```

```
 [-0.05014749  0.01887906 -0.00884956] [-0.13274336 -
```

```
 0.00884956  0.03539823]]
```

$X^T y$ :

```
[ 84. 464. 452.]
```

Coefficients (theta):

```
[2.87905605 0.54749263 0.74336283]
```

Regression Equation:

The regression equation is:  $y = 0.55 \cdot x_1 + 0.74 \cdot x_2 + 2.88$

### Multivariable Regression: Data points and Regression Plane

