

1.1:

$$P(\text{Jerry}) = 12/100 \quad P(\text{Susan}) = 22/100 \quad P(\text{Jerry} \cap \text{Susan}) = 8/100$$

- a. $P(\text{Jerry at bank} \mid \text{Susan was at bank}) = P(\text{Jerry} \cap \text{Susan}) / P(\text{Susan at bank})$
 $P(\text{Jerry} \cap \text{Susan}) = 8/100$
 $P(\text{Susan at bank}) = 22/100$
 $P(\text{Jerry at bank} \mid \text{Susan was at bank}) = P(\text{Jerry} \cap \text{Susan}) / P(\text{Susan at bank}) = 8/22 = 0.367$
- b. **$P(\text{Only Jerry At Bank}) = P(\text{Jerry}) = 12/100 = 0.12$**
- c. $P(\text{Both at bank} \mid \text{Atleast one at bank}) = P(\text{Both} \cap \text{Atleast one at bank}) / P(\text{Atleast one})$
 $P(\text{Atleast one at bank}) = 1 - P(\text{No one at bank})$
 $P(\text{No one at bank}) = (100 - (12 + 8 + 22)) / 100$
 $= (100 - 42) / 100$
 $= 58/100$
 $P(\text{Atleast one at bank}) = 1 - P(\text{No one at bank}) = 1 - (58/100)$
 $= 42/100$

$$**P(\text{Both at bank} \mid \text{Atleast one at bank}) = 8/42 = 0.190**$$

1.2:

$$\begin{aligned} P(\text{Harold} \cap \text{Sharon}) &= P(\text{Harold Getting B}) + P(\text{Sharon Getting B}) - \\ &P(\text{Harold Getting B} \cup \text{Sharon Getting B}) \\ &= 80/100 + 90/100 - 91/100 \\ &= 79/100 \end{aligned}$$

- a. $P(\text{Only Harold Will Get B}) = P(\text{Harold Getting B}) - P(\text{Harold} \cap \text{Sharon})$
 $= 80/100 - 79/100$
 $= 1/100 = \mathbf{0.01}$
- b. $P(\text{Only Sharon Will get B}) = P(\text{Sharon Getting B}) - P(\text{Harold} \cap \text{Sharon})$
 $= 90/100 - 79/100$
 $= 11/100 = \mathbf{0.11}$
- c. $P(\text{No One Getting B}) = 1 - P(\text{Atleast one})$
 $= 1 - 91/100$
 $= 9/100 = \mathbf{0.09}$

1.3:

$$P(\text{Jerry}) = 20/100$$

$$P(\text{Susan}) = 30/100$$

$$P(\text{Jerry} \cap \text{Susan}) = 8/100 = 0.08$$

$$P(\text{Jerry}) * P(\text{Susan}) = 0.06$$

$$P(\text{Jerry} \cap \text{Susan}) \text{ is not equal to } P(\text{Jerry}) * P(\text{Susan})$$

Hence, they are not independent.

1.4:

1. "The sum is 6 And "The second die shows 5" **are not independent** as there is a chance of getting a combination of (1, 5).
2. "The sum is 7" And "The first die shows 5" **are not independent** as there is a chance of getting a combination of (5, 2).

1.5:

$$P(\text{Choosing TX}) = 60/100$$

$$P(\text{Choosing NJ}) = 10/100$$

$$P(\text{Choosing AK}) = 30/100$$

$$P(\text{Finding Oil} \mid \text{In TX}) = 30/100$$

$$P(\text{Finding Oil} \mid \text{In AK}) = 20/100$$

$$P(\text{Finding Oil} \mid \text{In NJ}) = 10/100$$

a.
$$\begin{aligned} P(\text{Finding Oil}) &= P(\text{Finding Oil} \mid \text{In TX}) + P(\text{Finding Oil} \mid \text{In AK}) + P(\text{Finding Oil} \mid \text{In NJ}) \\ &= 0.3 + 0.2 + 0.1 \\ &= \mathbf{0.6} \end{aligned}$$

b.
$$\begin{aligned} P(\text{Choosing TX} \mid \text{Finding Oil}) &= (P(\text{Choosing TX}) * P(\text{Finding Oil} \mid \text{In TX})) \\ &\quad \text{-----} \\ &\quad (P(\text{Choosing AK}) * P(\text{Finding Oil} \mid \text{In TX}) + \\ &\quad P(\text{Choosing NJ}) * P(\text{Finding Oil} \mid \text{In NJ}) + \\ &\quad P(\text{Choosing AK}) * P(\text{Finding Oil} \mid \text{In AK})) \\ &= 0.6 * 0.3 / (0.6 * 0.3 + 0.1 * 0.1 + 0.3 * 0.2) \\ &= 0.18 / 0.25 \\ &= \mathbf{0.72} \end{aligned}$$

1.6:

a. $P(\text{Did not survive}) = 1490/2201 = \mathbf{0.676}$

b. $P(\text{Was In First Class}) = 325/2201 = \mathbf{0.147}$

c. $P(\text{Staying in first} \mid \text{Survived}) = P(\text{First} \cap \text{Survived}) / P(\text{Survived})$

$$P(\text{Survived}) = 711/2201$$

$$P(\text{First} \cap \text{Survived}) = 203/2201$$

$$P(\text{Staying in first} \mid \text{Survived}) = P(\text{First} \cap \text{Survived}) / P(\text{Survived}) = 203/711 = \mathbf{0.285}$$

d. $P(\text{Survival}) = 711/2201 = 0.32$

$$P(\text{First Class}) = 325/2201 = 0.14$$

$$P(\text{Survival} \cap \text{First Class}) = 203/2201 = 0.09$$

$$P(\text{Survival}) * P(\text{First Class}) = 0.04$$

$$P(\text{Survival} \cap \text{First Class}) \text{ not equal to } P(\text{Survival}) * P(\text{First Class})$$

Hence they are not independent.

e. $P(\text{First class child} \mid \text{Survived}) = P(\text{First class child} \cap \text{Survived}) / P(\text{Survived})$

$$P(\text{Survived}) = 711/2201$$

$$P(\text{First class child} \cap \text{Survived}) = 6/2201$$

$$P(\text{First class child} \mid \text{Survived}) = P(\text{First class child} \cap \text{Survived}) / P(\text{Survived}) = 6/711 =$$

0.0084

f. $P(\text{Adult} \mid \text{Survived}) = P(\text{Adult} \cap \text{Survived}) / P(\text{Survived})$

$$P(\text{Survived}) = 711/2201$$

$$P(\text{Adult} \cap \text{Survived}) = 197/2201$$

$$P(\text{Adult} \mid \text{Survived}) = P(\text{Adult} \cap \text{Survived}) / P(\text{Survived}) = 197/711 = \mathbf{0.277}$$

g. $P(A \cap B \mid C) = P(A \mid C) * P(B \mid C)$

$$P(\text{Age} \cap \text{Staying In First Class} \mid \text{Survived}) =$$

$$P(\text{Age} \mid \text{Survived}) * P(\text{Staying In First Class} \mid \text{Survived})$$

$$P(\text{Age} \cap \text{Staying In First Class} \mid \text{Survived}) = 203/2201$$

$$P(\text{Age} \mid \text{Survived}) = 711/2201$$

$$P(\text{Staying In First Class} \mid \text{Survived}) = 203/2201$$

$$P(\text{Age} \mid \text{Survived}) * P(\text{Staying In First Class} \mid \text{Survived}) \text{ not equal to } P(\text{Age} \cap \text{Staying In First Class} \mid \text{Survived})$$

Hence not independent.