Physics 5B: Sound Waves II

BY KAMERON GILL
Date Febuary 8, 2017

- For Friday: read Ch $16.6 \Rightarrow 16.9$
- $$\begin{split} \bullet & \quad \text{Intensiy } I = 10^{-4} \frac{W}{m^2} \Rightarrow \delta = 10 \text{log} \Big(\frac{I}{I_0} \Big) = 10 \text{log} \big(\frac{10^{-4}}{10^{-12}} \big) = 80 \text{ dB} \\ & \quad I = 10^{-5} \frac{W}{m^2} \Rightarrow 70 \text{ dB} \\ & \quad \frac{1}{10} I \Rightarrow 10 \text{ dB increase} \\ & \quad \frac{1}{100} I \Rightarrow 20 \text{ dB decrease} \end{split}$$
- What about double Intensity? $I_2 = I_1$

$$\begin{split} B_1 &= 10 \log \left(\frac{I_1}{I_0}\right) & B_2 &= 10 \log \left(\frac{I_2}{I_0}\right) \\ B_2 - B_1 &= 10 \log \left(\frac{I_2}{I_0}\right) - 10 \log \left(\frac{I_1}{I_0}\right) = 10 \left(\log \left(\frac{I_2}{I_0}\right) - \log \left(\frac{I_1}{I_0}\right)\right) \\ &= 10 \log \left(\frac{I_2}{I_1}\right) = 10 \log(2) = 3.010 \, \mathrm{dB} \end{split}$$

- Vibrating Strings:
 - I. Frequency (Pitch)

Strings fixed at both ends:

Fundamental:

$$\lambda = 2L$$
 $L = \frac{1}{2}\lambda$

2nd. Harmonic:

$$L{=}\lambda$$
 $\lambda{=}L$

$$f_n = \text{nf}_1 = n \frac{v}{\lambda_1} = n \frac{v}{2L}$$
 Frequency Equation

$$f_{1=\frac{v}{2l}}$$
 $f_{2=\frac{v}{L}}$

To get different Frequencies: we need to change properties of strings!

$$v = \sqrt{\frac{F_T}{\mu}}$$
 via stretching or length by fingering

EXAMPLE:

Guitar string .73m long, tuned to E 330(Hz) Where should you put your finger to play A4 (440 Hz)?

$$f_E = \frac{v}{2L} = \frac{1}{2L} \sqrt{\frac{F_T}{\mu}}$$

$$f_A = \frac{1}{2L'} = \sqrt{\frac{F_T}{\mu}}$$

$$f_A L' = f_E L \Rightarrow L' = \frac{f_E}{f_A} L = \frac{330}{440} (.73m)$$

 $L' = .548 \mathrm{cm}$

II. Vibrating columns of Air

Two cases: At least one is open and stadning wave is formed

Case 1: tube open at both ends

At open ends, air moves freely, but gauge pressure is 0

Anti-node for displacement wave, Node for pressure wave

$$f_1 = \frac{v}{2L}$$
 $f_2 = \frac{v}{L}$ for the 2nd Harmonics

Case 2: tube closed at ends

$$f_1 = \frac{v}{4L} = \frac{v}{\lambda_1}$$

EXAMPLE: What is length of base clarinet (closed at one end) that plays the low D (72.4 Hz)?

Fundamental freequency at one end: $f_1 = \frac{v}{4L}$

$$L = \frac{v}{4f_1} \Rightarrow \frac{343}{4(72.4)} = 1.18m$$