

# CE 107:

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## I. Probability Theory

- Probability of an event - Number assigned to the event reflecting the likelihood with which it can occur or has been observed to occur
- A Probability law for random experiment is a rule that assigns the probability of a certain event follows three conditions
  - i. An event A may or may not take place; and it has some likelihood, which is 0 if it never occurs
  - ii. Something must occur in our experiment
  - iii. If one event negates another, then the likelihood that either occurs is the likelihood that one occurs plus the likelihood that the other occurs
- Random Experiment
  - a) A random experiment is specified by stating an experimental procedure and a set of measurements and observations
- Sample Space
  - a) Any set of elements can be a sample space
  - b) We only require that performing our experiment must result in one outcome
  - c) We denote sample space by S or  $\Omega$
- Events
  - a) An event associated with a random experiment corresponds to a proposition
  - b) the event occurs if ANY of the outcomes that makes the proposition “true” takes place
  - c) So, any event is associated with a subset of the sample space S and can be empty
  - d) An impossible event corresponds to the empty set  $\emptyset$
- Example
  - a) Life of a light bulb
  - b) sample space:  $S = \{x \in R | x \geq 0\}$
- Prob Theory
  - a) Consists of: Sample Space, set of events F, probability measure

- Probability law:

$$\text{AI: } 0 \leq P(A)$$

$$\text{AII: } P(\Omega) = 1$$

$$\text{AIII: if } A \cap B = \emptyset \text{ then } P(A \cup B) = P(A) + P(B)$$

## II. Algebra of Events

A) Natural Numbers:  $[0, \infty)$

B)  $\mathbb{R}$ :  $(-\infty, \infty)$

## III. SMT

Contradiction is F

True is T

$$\text{IV. } \left\{ \bigcup_{f=1}^k A_f \right\} \cap B = \bigcup_{f=1}^k (A_f \cap B)$$

Base case: let  $k = 1$  then  $A_1 \cap B = A_1 \cap B$ . we assume that the result is true for  $n \geq 1$

We need to show that it also true for  $n+1$ . using the recursive definition of union of sets we have

## V. Corollary

A) Corollary  $P(A^c) = 1 - P(A)$  Chance of something NOT happening

B)  $P(A) \leq 1$

C)  $P(\emptyset) = 0$

D)  $P[A \cup B] = P[A] + P[B] - P[A \cap B]$