

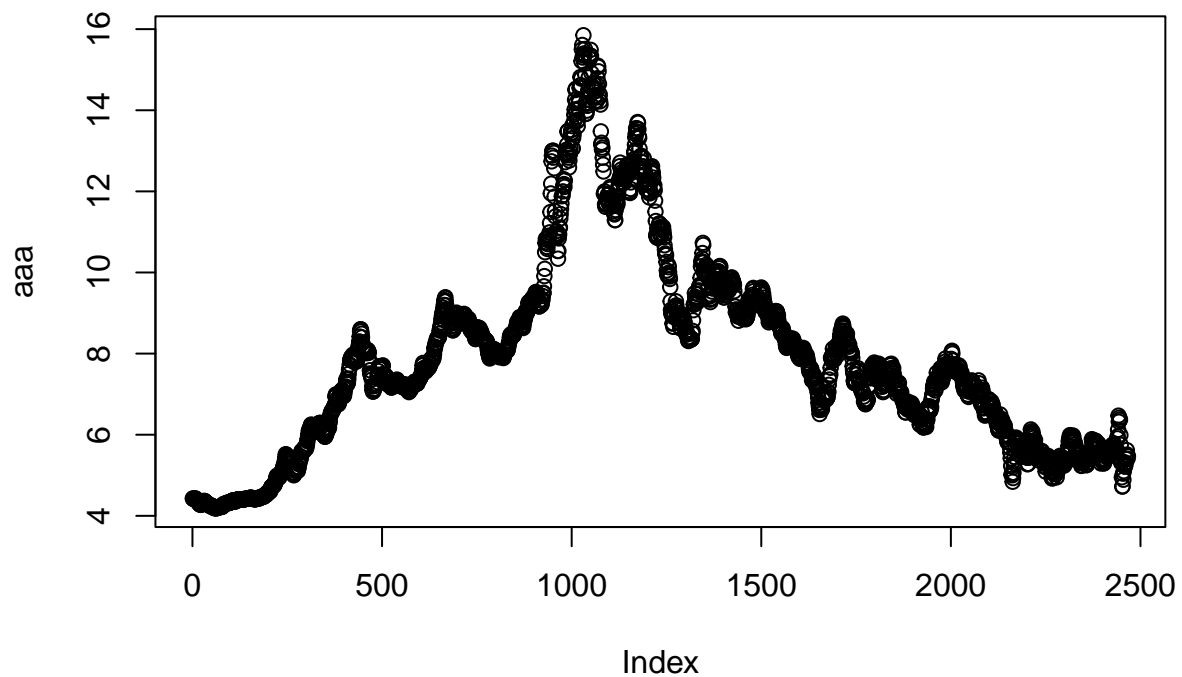
Q7_Regression

Kamin Atsavasirilert

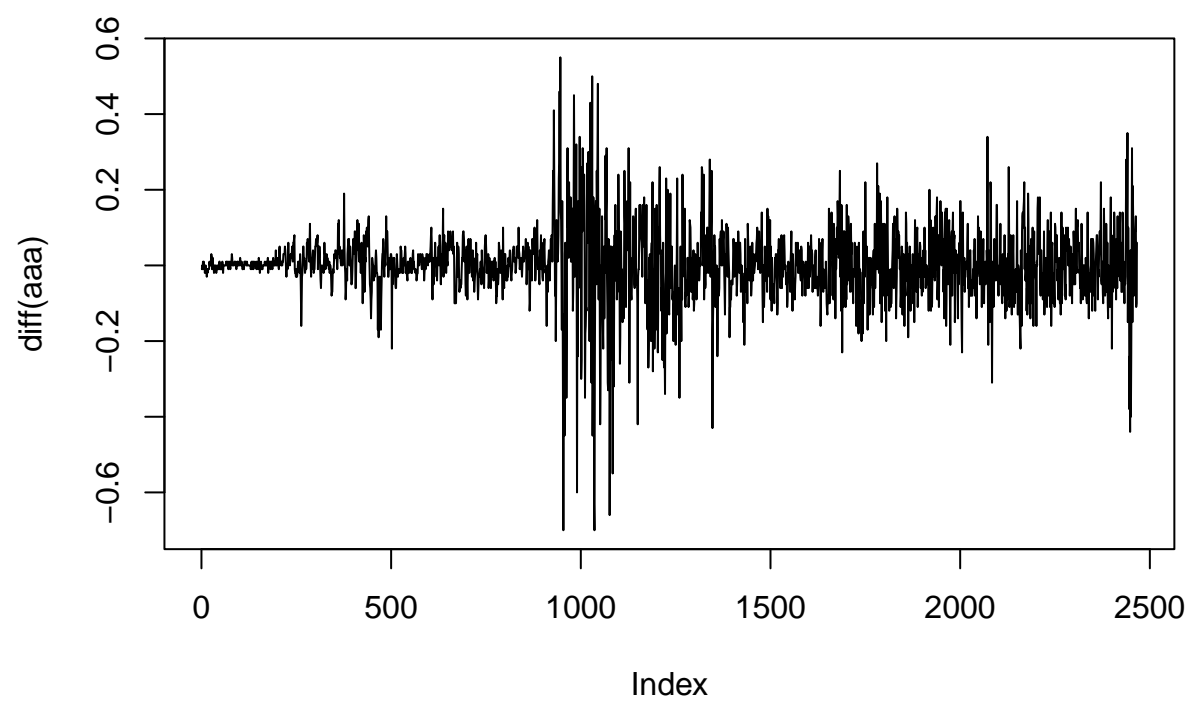
2024-10-09

Date preparation => Removing non-stationarity

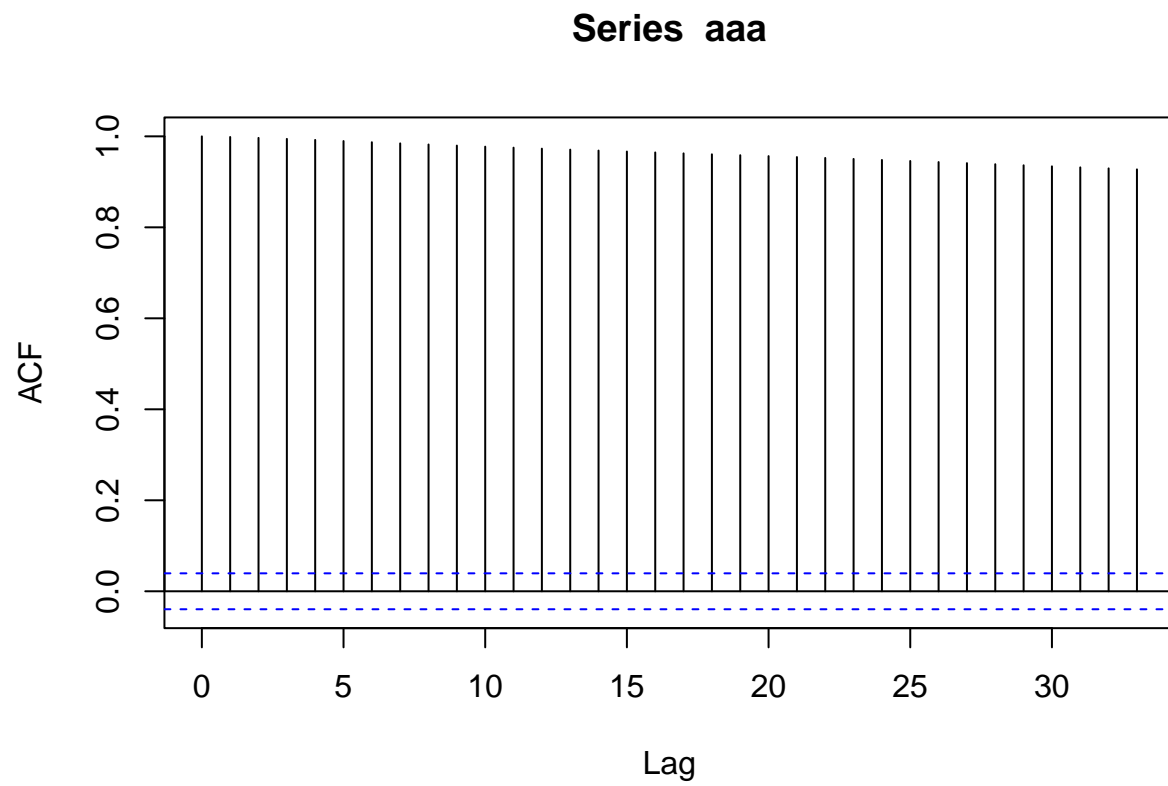
```
df=read.table("w-Aaa.txt",sep = "")  
aaa = df$V4  
plot(aaa)
```



```
plot(diff(aaa),type="l")
```

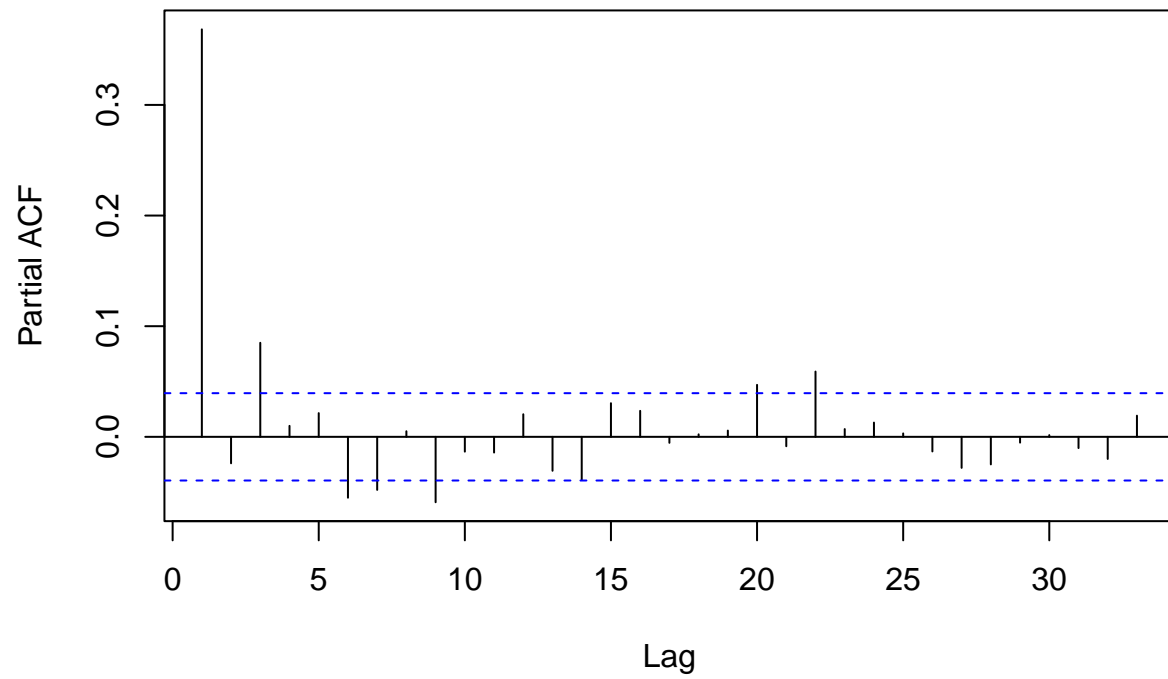


```
acf(aaa)
```

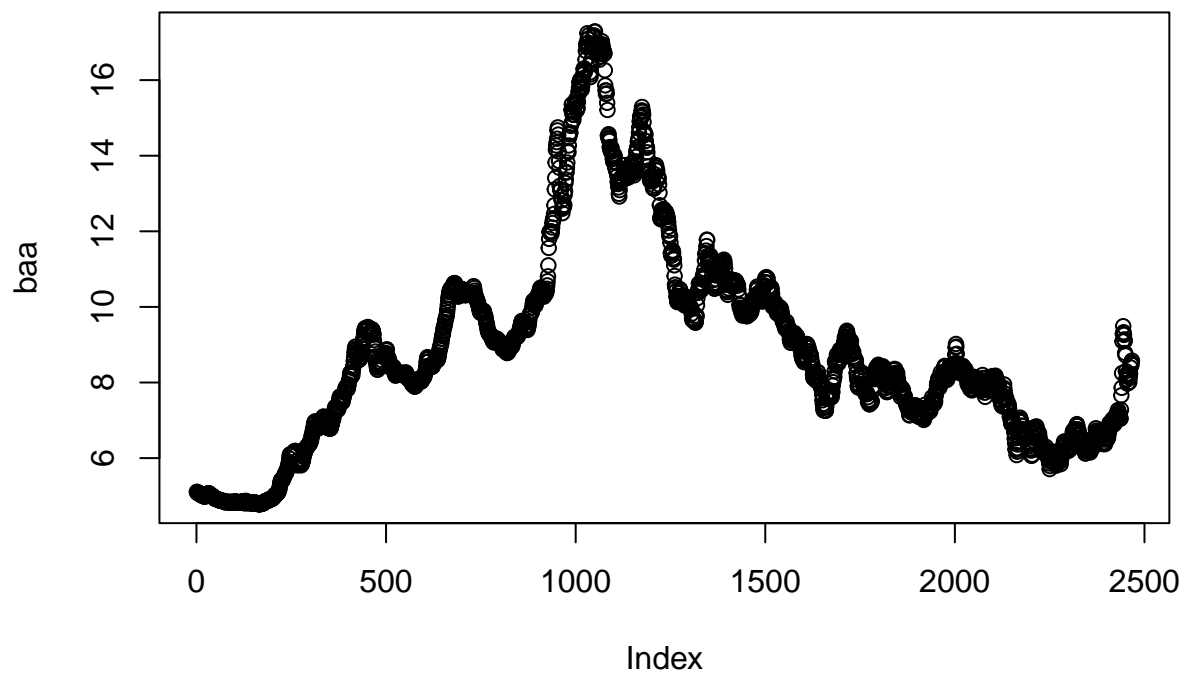


```
pacf(diff(aaa))
```

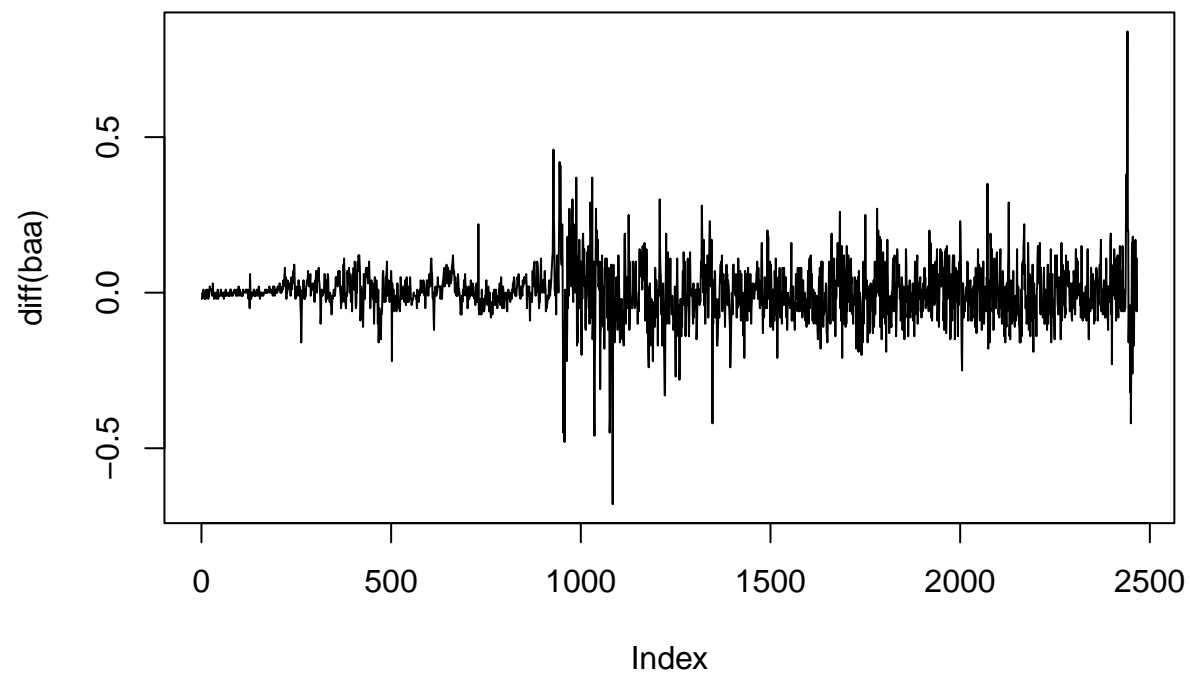
Series diff(aaa)



```
df=read.table("w-Baa.txt",sep = "")  
baa = df$V4  
plot(baa)
```

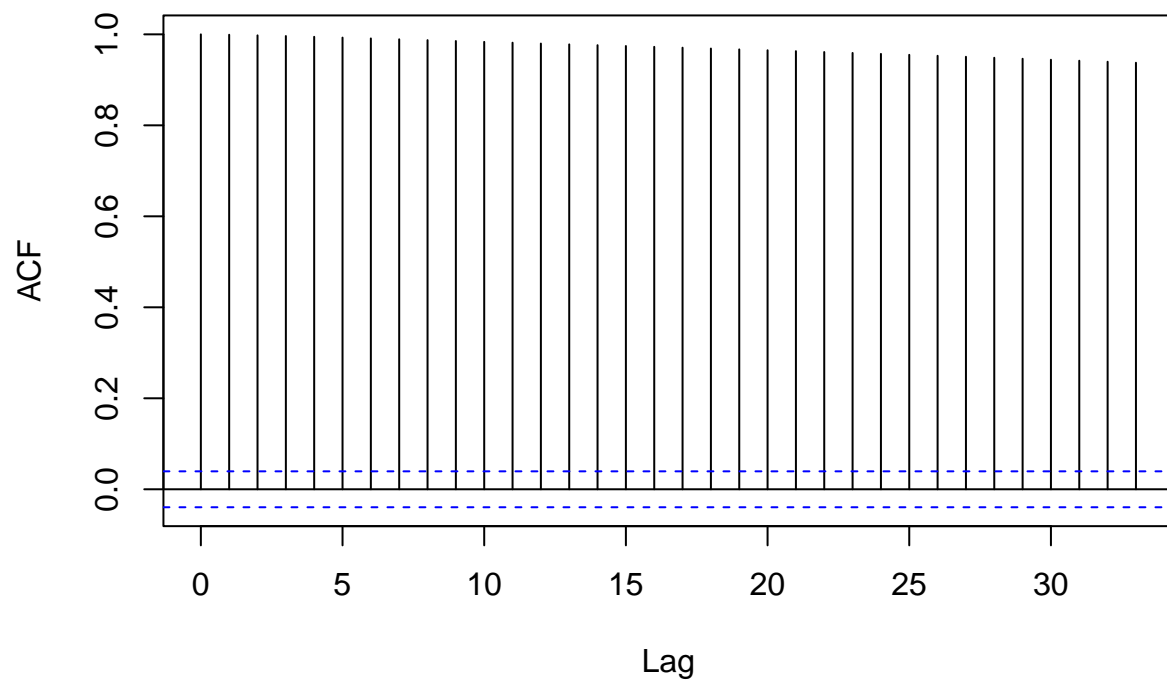


```
plot(diff(baa),type="l")
```



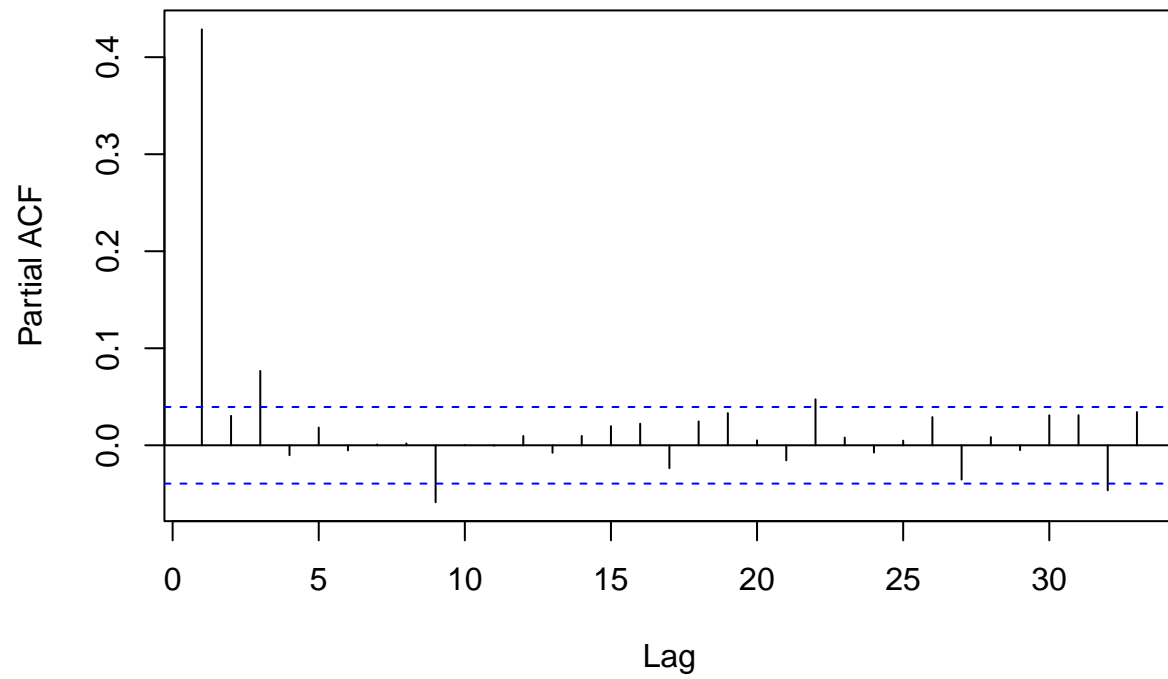
```
acf(baa)
```

Series baa



```
pacf(diff(baa))
```

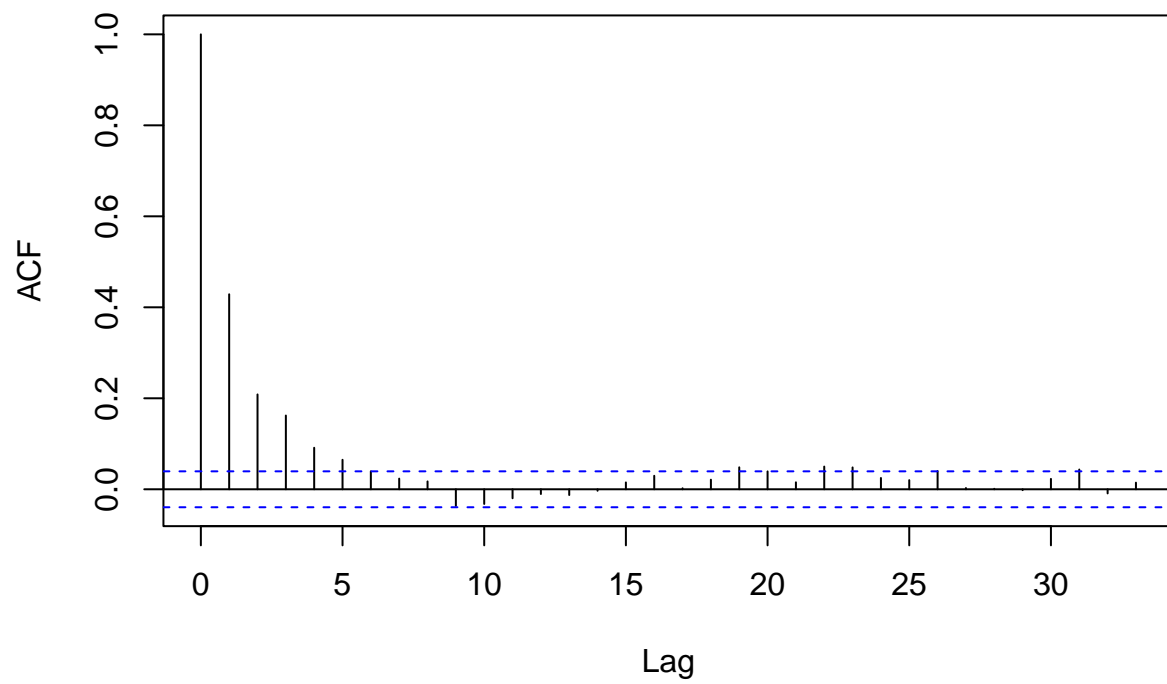
Series diff(baa)



```
d_baa = diff(baa)
d_aaa = diff(aaa)

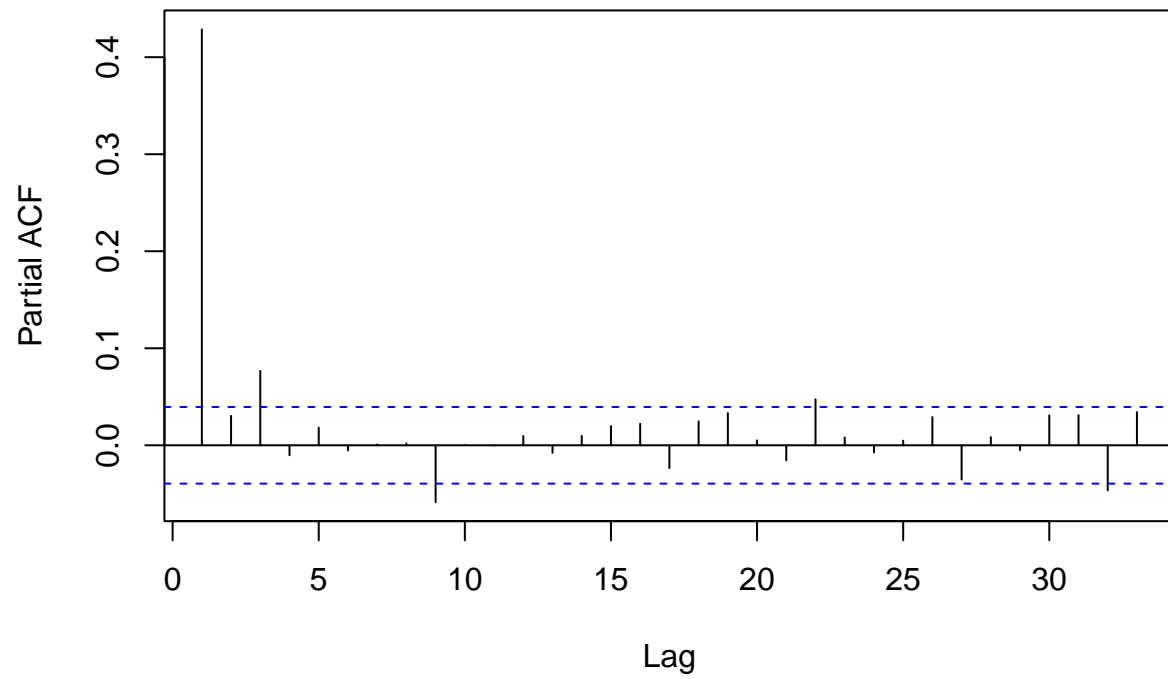
acf(d_baa)
```


Series d_baa



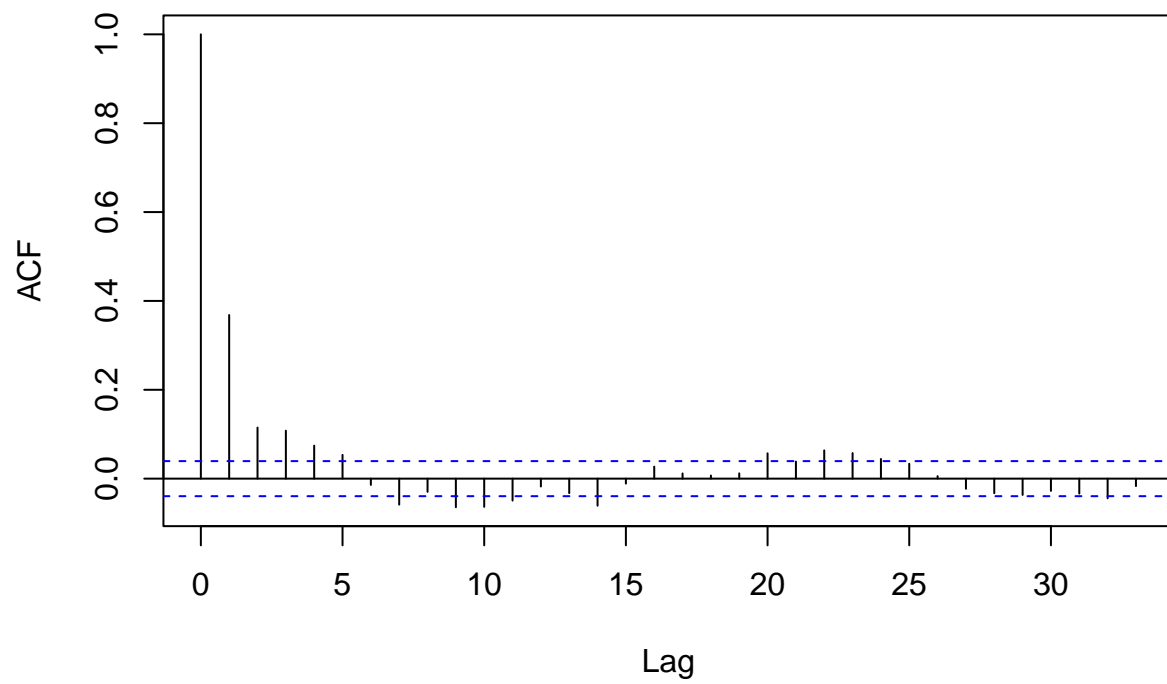
```
pacf(d_baa)
```

Series d_baa



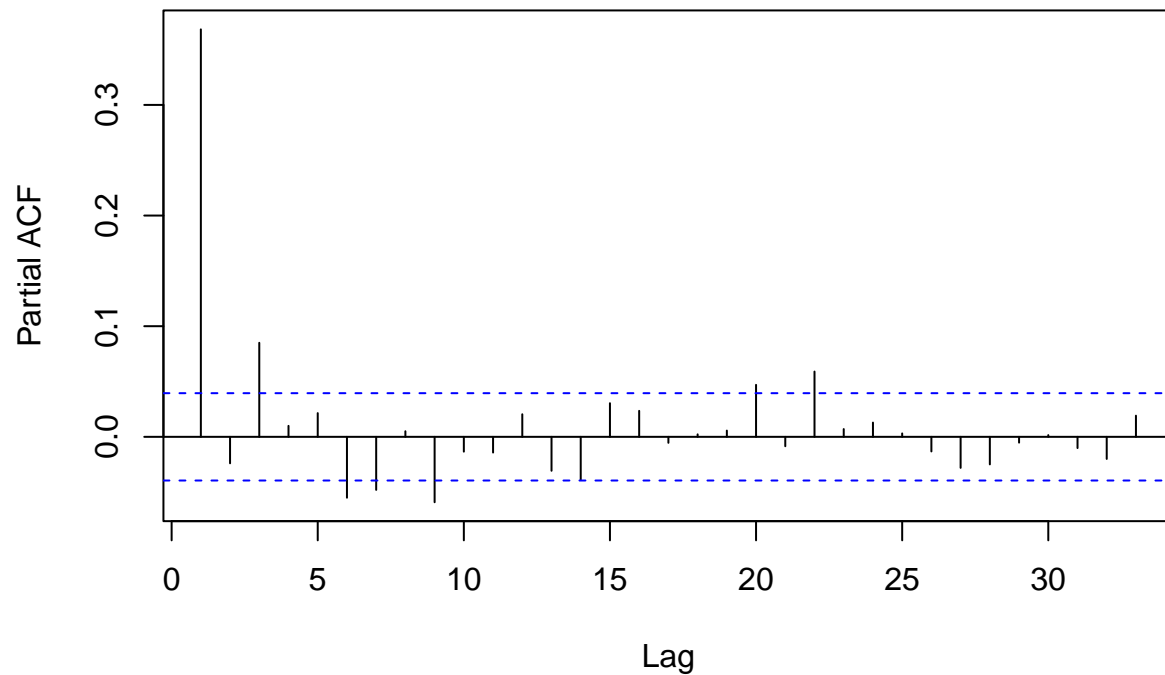
```
acf(d_aaa)
```

Series d_aaa



```
pacf(d_aaa)
```

Series d_aaa



Simple regression model and model checking

```
##
## Call:
## arima(x = d_aaa, order = c(0, 0, 0), xreg = d_baa, include.mean = F)
##
## Coefficients:
##      d_baa
##      0.9461
## s.e.  0.0126
##
## sigma^2 estimated as 0.002851:  log likelihood = 3726.22,  aic = -7448.45

## Warning in adfTest(model$residuals, lags = 2, type = ("c")): p-value smaller
## than printed p-value

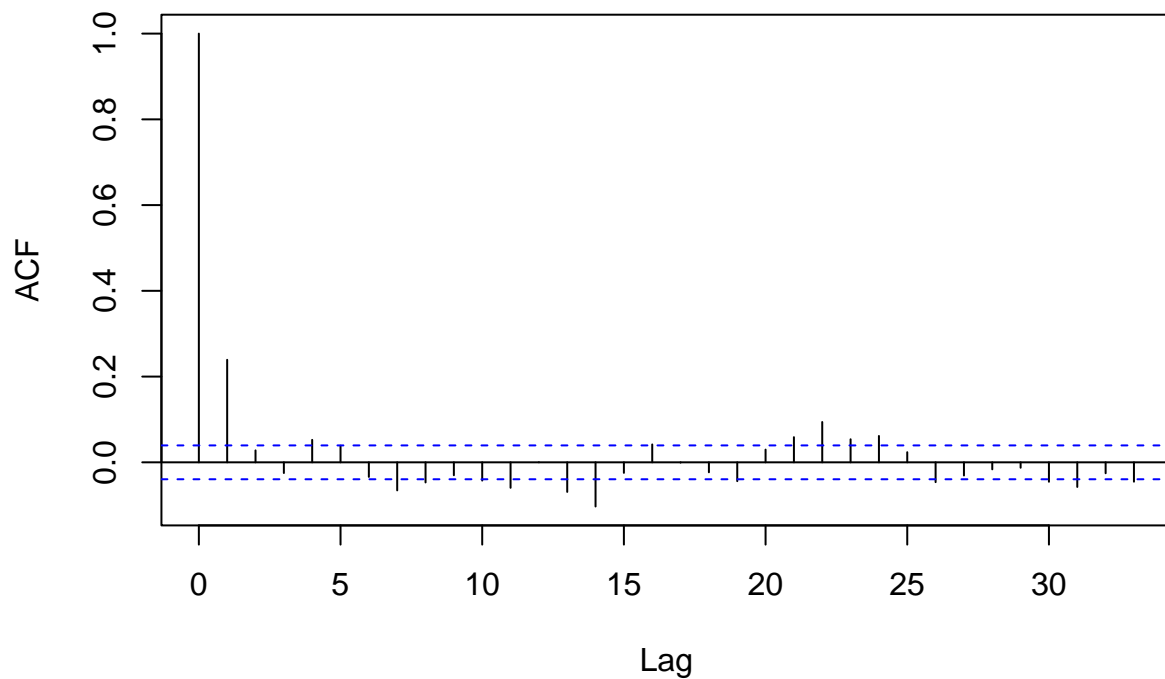
##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
## PARAMETER:
## Lag Order: 2
## STATISTIC:
## Dickey-Fuller: -27.2846
```

```
## P VALUE:
## 0.01
##
## Description:
## Tue Oct 8 23:02:59 2024 by user: kamin

## Warning in adfTest(model$residuals, lags = 2, type = ("ct")): p-value smaller
## than printed p-value

##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
## PARAMETER:
## Lag Order: 2
## STATISTIC:
## Dickey-Fuller: -27.3062
## P VALUE:
## 0.01
##
## Description:
## Tue Oct 8 23:02:59 2024 by user: kamin
```

Series model\$residuals



Try joint estimation with MA(1)

```
##
## Call:
## arima(x = d_aaa, order = c(0, 0, 1), xreg = d_baa, include.mean = F)
##
## Coefficients:
##          ma1    d_baa
##      0.2335  0.9436
## s.e.  0.0185  0.0132
##
## sigma^2 estimated as 0.00269:  log likelihood = 3797.81,  aic = -7589.62

## [1] 0.7117952

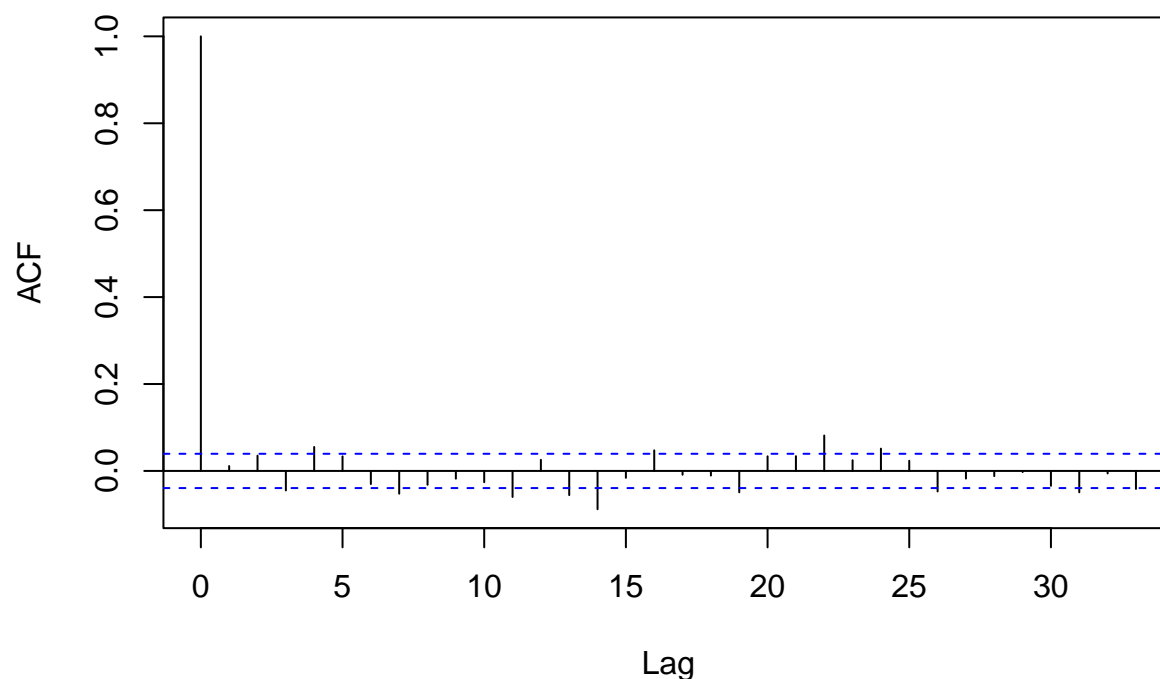
## Warning in adfTest(new_model1$residuals, lags = 2, type = ("c")): p-value
## smaller than printed p-value

##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
## PARAMETER:
## Lag Order: 2
## STATISTIC:
## Dickey-Fuller: -29.1319
## P VALUE:
## 0.01
##
## Description:
## Tue Oct 8 23:02:59 2024 by user: kamin

## Warning in adfTest(new_model1$residuals, lags = 2, type = ("ct")): p-value
## smaller than printed p-value

##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
## PARAMETER:
## Lag Order: 2
## STATISTIC:
## Dickey-Fuller: -29.1527
## P VALUE:
## 0.01
##
## Description:
## Tue Oct 8 23:02:59 2024 by user: kamin
```

Series new_model1\$residuals



Try joint estimation with AR(1)

```
##
## Call:
## arima(x = d_aaa, order = c(1, 0, 0), xreg = d_baa, include.mean = T)
##
## Coefficients:
##          ar1  intercept    d_baa
##      0.2392   -0.0009   0.9473
## s.e.  0.0195     0.0014   0.0133
##
## sigma^2 estimated as 0.002687:  log likelihood = 3799.21,  aic = -7590.42

## [1] 0.7121225

## Warning in adfTest(new_model2$residuals, lags = 2, type = ("c")): p-value
## smaller than printed p-value

##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
##  PARAMETER:
```

```

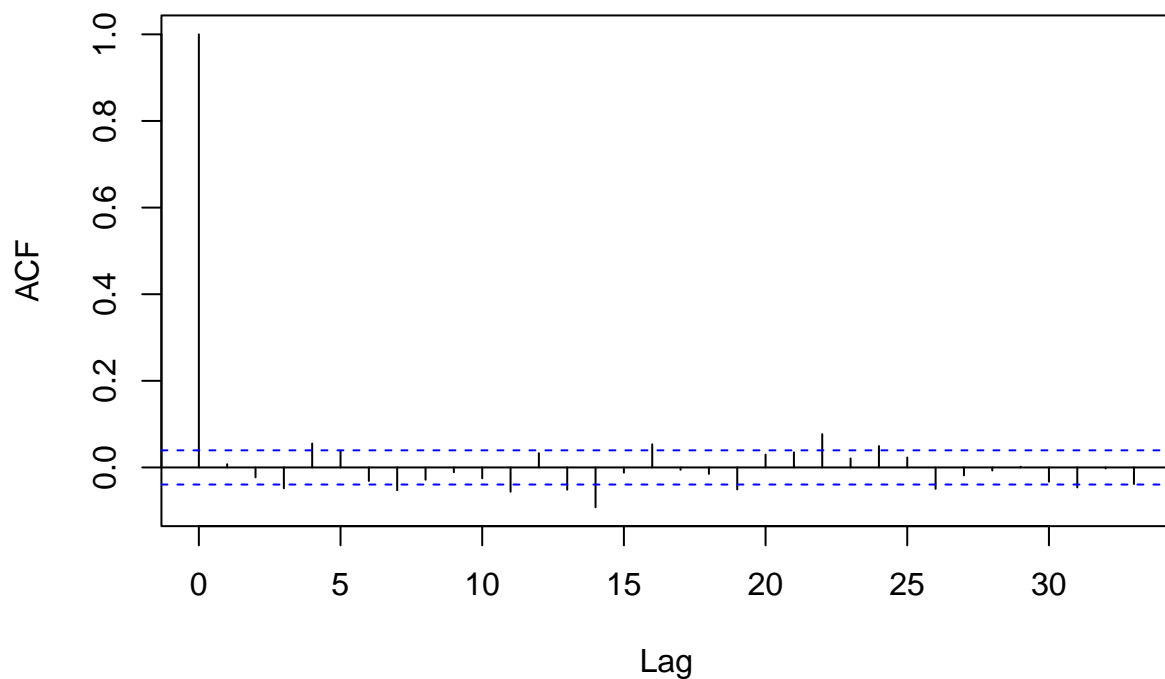
##      Lag Order: 2
##      STATISTIC:
##      Dickey-Fuller: -30.3965
##      P VALUE:
##      0.01
##
## Description:
## Tue Oct  8 23:03:00 2024 by user: kamin

## Warning in adfTest(new_model2$residuals, lags = 2, type = ("ct")): p-value
## smaller than printed p-value

##
## Title:
## Augmented Dickey-Fuller Test
##
## Test Results:
## PARAMETER:
##      Lag Order: 2
##      STATISTIC:
##      Dickey-Fuller: -30.4162
##      P VALUE:
##      0.01
##
## Description:
## Tue Oct  8 23:03:00 2024 by user: kamin

```

Series new_model2\$residuals



Conclusion: Based on the information criteria (AIC), I chose the joint estimation with AR(1) term.

The final relationship is: $d_aaa_t = 0.2394 * d_aaa_t[-1] + 0.9472 * d_baa_t + \text{epsilon}$.
Where the epsilon is the forecast error (no guarantee to be iid).