

- Data structure is a method of organising large amount of data more efficiently so that any operation on that data become easy.

• Needs :-

- Provides fast searching & sorting of data.
- It tells how data can be stored & accessed at its elementary level.

• 2 types :-

Primitive

Non- Primitive

- They are fundamental data type which are supported by a programming language

• They are those data structure which are created using primitive data struct.

- int , real , integer, char

- Stack, tree, linked list .

- Operated directly by machine level instructions

- Operated directly by machine level instructions not by machine level.

Non - Linear

④ Linear

→ A data structure that maintains a linear relationship among its elements.

→ Array, linked list, stack, queues.

→ Trees of graph.

→ Deleting: used to delete data item from the given list.

⑤ Static DS.

→ An static data since size of structure is fixed.

⑥ Dynamic DS.

→ Sorting: used for arranging items in asc. or desc. acc to user.

→ Merging: list of 2 sorted items can be combined to form a single list.

⑦ Data Abstraction:

→ Content of ds can be modified without changing memory space allocated to it.

→ Modified & can be changed during run-time.

→ Data Abstraction is reduction of particular body of data to a simplified representation of whole.

Abstraction is the process of removing characteristics from something to reduce it to set of essential elements.

→ Array.

→ Linked list.

Operations on Data Structure:

① Searching

→ Searching: used to find the location of one or more data items.

→ Inserting: used to add new items in given list of data items.

→ Deleting: used to delete data item from the given list.

Data abstraction creates a simplified representation of data, while hiding its complexity & intricacy of operations.

Used in mainly OOPS while working with DBMS.

④ Abstract Data type :-

When data structure do operations like adding or deleting an item from a list, accessing a item in list, or searching & sorting an item in a list. Then it is called abstract data type.

⑤ Algorithm :-

→ It is a step-by-step procedure, which defines a set of instructions to be executed in a certain order to get desired output.

⑥ Time Complexity

Step 4 :- display c

Step 5 :- STOP

Space Complexity

Step 2 :- Get values of a & b

Step 3 :- C \leftarrow a+b

⑦ Algo to add 2 no. :-

Step 1 :- START ADD.

Adv. :- It is easy to understand. Time consuming.

Disadv. :- Step-wise soln to a given problem. Travelling & looping are difficult to show.

$$T(n) = C * n \quad (n = \text{steps})$$

• Sum of fixed part of variable part is the total space required by algo.

$$S(n) = C + S_P(n)$$

fixed : variable.

① Types of Analysis :-

→ Best Case :-

Least amount of time to execute a specific set of input.

→ Average Case :-

Average time taken for input execution.

→ Big - O (O) :-

It is the method used to express the upper bound of running time of an algorithm.

Max amount of time to execute a specific set of input.

→ Omega (Ω) :-

Omega gives the "lower bound" of algo run time.

② Asymptotic Notations :-

→ They are languages that allows us to analyze an algorithm's running time by identifying its behaviour as the input size of algorithm increases.

→ Theta (Θ) :-

It is used when upper bound & lower bound of an algo are in same magnitude

3 Types.

- Big - O :- Specifically describes worst case scenario.
- Omega :- Specifically describes best case scenario.
- Theta :- Represents average complexity of algo.

Time - Space Trade off :-

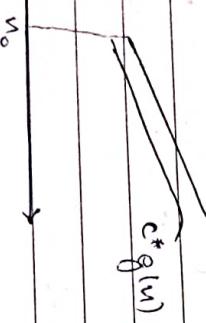
• \rightarrow



$$\underline{\underline{Bog}} - 0 \quad f(u) = \underline{\underline{\Theta(g(u))}}$$

- By solving a problem in very little space by spending a long time.

• \rightarrow



① Recursion:-

→ As it is not possible to achieve both at a same time.

• \rightarrow

$$\text{Omega } f(n) = \underline{\underline{\Omega(g(u))}}$$

At no a process of repeating items in a self-similar way.

If a program allows to call a func inside the same func.

$c_1^*(g(u))$.

$$\underline{\underline{\text{It's like } f(u) = \Theta(g(u))}}$$

25

$f(u)$ \rightarrow $\underline{\underline{f(u) = void u, ()}}$

26

Unit → 5

① factorial using recursion .

```
#include < stdio.h >
#include < conio.h >

int fact (int);
void main()
{
    int n, f;
    printf ("Enter a value");
    scanf ("%d", &n);
    f = fact (n);
    printf ("%s", "The factorial is %d", f);
    getch ();
}

int fact (int n)
{
    if (n == 0)
        return 1;
    else
        return n * fact (n - 1);
}
```

② File :-

It is a collection of records .
the file size is limited by size of memory & storage medium.

③ File Organisation :-

It is used to describe the way in which the records are stored in terms of blocks , if the blocks are placed on storage medium .

→ 3 types of organizing file :-

- Sequential access file organisation
- Direct access "
- Indexed sequential access "

④ Sequential :-

- In this , all records are stored in a sequential order .
- Storing & reading in contiguous block within files on tape or disk .
- In this , search start from beg. & add " of records at end of file .

Disadv.

Adv.

Disadv.

Adv.

- It is simple to program

• Sequential file is time consuming process.

- Sorting of records are not reqd.

• It is expensive

- Does not provide back-up facility

- It is easy to design.

• Random searching is not possible.

- It updates several files quickly.

• Access the records(desire) immediately.

- Zero storage than sequential.

- Sequential file is best use of storage.

• Random searching is not possible.

- It updates several files quickly.

• Access the records(desire) immediately.

- Zero storage than sequential.

① Direct access fo :-

② Indexed sequential :-

- In this, all records are stored in direct-access storage device such as hard disk.

• This type of fo.0 contains both seq. files & direct access fo.0. data can be accessed using index both (seq. or random).

- Randomly placed throughout the file.

• Two file have multiple keys. Records are stored randomly on direct access(hard disk) by primary key.

- This is useful for immediate access to large amount of information.

- It is also called as hashing.

Adv.

Disadv.

- Used in accessing large database.

• Records can be inserted at middle of file.

- Req. more storage.

- Access records very fast.

• Expensive.

AVL Tree

- A tree is a collection of nodes.

- Height of tree is total no. of nodes from root to a leaf in longest path.

AVL Tree is a self-balancing BST where the difference between heights of left & right subtree cannot be more than one for all nodes.

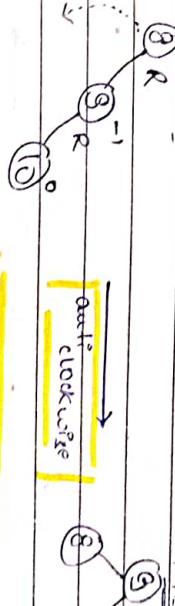
- AVL Tree :-

$$Q. \quad 55, 25, 65, 9, 8, 15 ?$$

→ Balanced factor should be -1, 0, 1 taken as balanced.

$$Q. \quad 8, 9, 10$$

$$0-2 = -2 \checkmark$$



anti clockwise

RR Rotation

RR Rotation

$$10, 9, 8$$

$$0-2 = -2 \checkmark$$

$$8$$

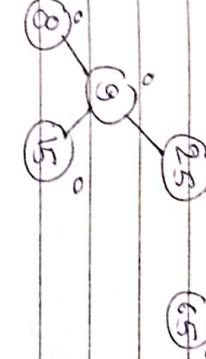
clockwise

LL

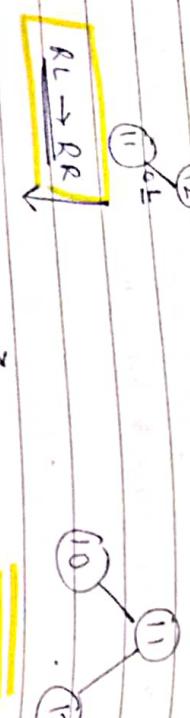
$$3-0 = 3 \checkmark$$

RL Rotation

2 Rotations



X wrong way



→ So after we insert new element we will right it by rotations.

LR Rotation

2 Rotations



$$2-1=1$$

$$3-1=2$$

Binary Tree

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- ① If all the nodes in a tree has atmost 2 children.

Struct node

f

int data;

Struct node * left;

Struct node * right;

y;

→ Strictly Binary tree :-

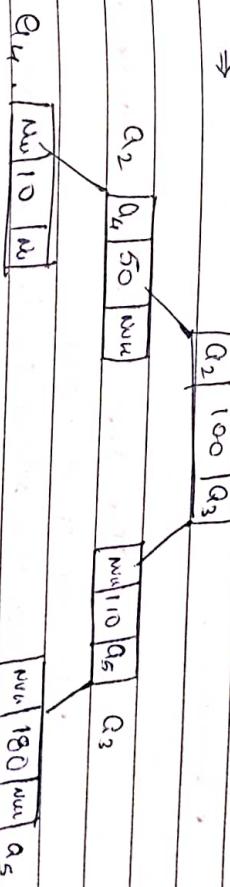
A BT in which every node has either 0 or 2 no of children.

② Linked representation :-

→ 100, 50, 10, 110, 180.

→ Complete Binary tree :-

A BT in which every internal node has exactly 2 children & all leaf nodes are at same level.



③ Representation :-

④ A tree contain following parts :-

- Data
- Pointer to left-child
- Pointer to right child.

⑤ Tree Traversal :-

Process of visiting each node exactly once.

- Breadth tree traversal :- level by level traversal
- Depth tree traversal :-
 - Pre
 - Post
 - In

Binary Search Tree

It is a binary tree in which value of left child to the parent node is less than the value of right child to its parent node.

① Inorder (root)

if (root ≠ NULL)

Inorder (root → left)

Print (root → data)

Inorder (root → right).

j.

② Traversing Algo:-

→ we start searching from root node, then if item is less than root's data, we search for empty location in root's left subtree & insert the item.

Inorder :-

Traverse the left sub-tree Inorder.

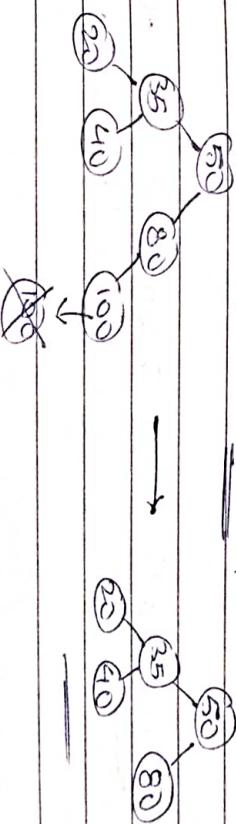
Visit the root node.

Traverse the right sub-tree Inorder.

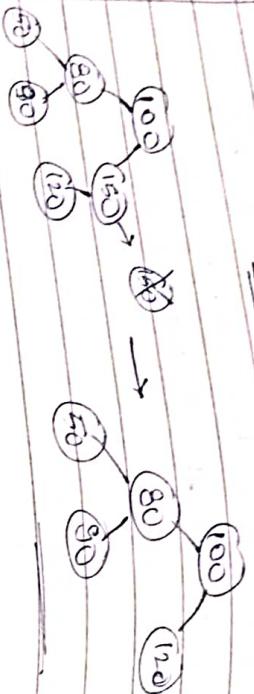
→ otherwise we search for empty location in root's right subtree & insert item.

③ Insertion :-

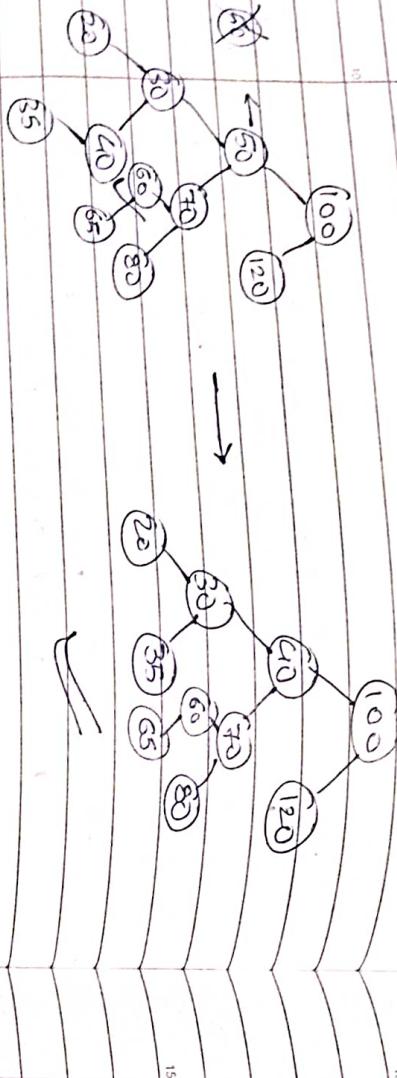
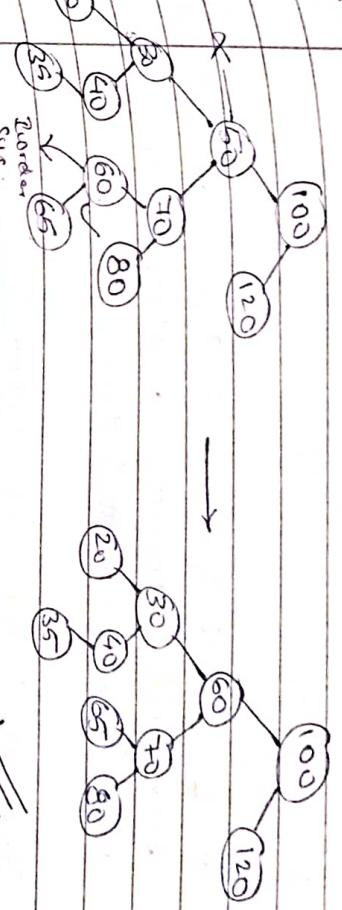
No child



1 circ.



2 children.



- 1st method :- Left subtree in slow data member. (Inorder predecessor)
- 2nd method :- Right subtree in slow data member. (Inorder successor)

① B-Tree :-

It is a self balanced search tree in which every node contains multiple keys & has more than 2 children.

- Construct B-tree of order 3 ?

$$m=3 \rightarrow \max \text{ child} = 3$$

- 1, 2, 3, 4, 5, 6, 7, 8, 9, 10

$$\max \text{ Key} \rightarrow m_1 = 2$$

8th.



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Searching

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① Threaded Binary tree :-

- this search is applicable to a noble organized either on a array or a linked list.
- $\text{Complexity} = O(n)$.

Prog :-

```
int RecLinearSearch( int arr[], int size,
                     int key )
{
    int loc;
    if (arr[ size ] == key)
        return size;
    else if (size == -1)
        return -1;
    else
        return RecLinearSearch( arr, size - 1, key );
}
```

① Binary Search :-

- For binary search, list of elements should be sorted.

• → Binary search looks for selected element by comparing the middle most element of list.

→ If match occurs, new index of item is returned

→ If middle element is greater than item, then item is searched in sub array to left of middle element.

→ Otherwise the item is searched in the sub array to right of middle element.

→ Process continues until size of subarray reduces to zero.

$$\text{Complexity} = O(\log n)$$

② int RecBinarySearch (int a[], int lb, int ub, int item)

if (lb <= ub)

int mid = (lb + ub) / 2 ;
if (item == a[mid])
return mid;

else if (item < a[mid])

return RecBinarySearch (a, lb, mid - 1, item);

else return RecBinarySearch (a, mid + 1, ub, item);

$$mid = \frac{\text{first} + \text{last}}{2} = \frac{0 + 4}{2} = 2 \checkmark$$

1	2	3	5	6
0	1	2	3	4

Comparing to mid if yes then searching is completed

but it greater than .

① Algo for Linear Search :-

- (i) $i = 0$ \rightarrow ~~max size~~
- (ii) If $A[i] = x$, go to step 6
- (iii) $i = i + 1$
- (iv) Go to step 2
- (v) Print element x found at i .
- (vi) Print element not found.
- (vii) Exit .

Q.

2	4	6	3	1	5
i = 0	0	1	2	3	4

$n = 6$.

- $i = 0$
- $0 > 6$ false
- $A[i] = 3$
- $A[0] = 3$
- $2 = 3$ false .

Q.

2	4	6	3	1	5
i = 0	0	1	2	3	4

$x = 3 \rightarrow$ to search.

- $i = 0$ \rightarrow ~~max size~~
- (i) Set $begin = 1$ $b = 1$ $end = 6$ $wid = (1+6)/2$
- (ii) Repeat step 3 & 4 while $begin < end$ & $A[wid] \neq x$.
- (iii) If $A[wid] < x$ set $end = wid - 1$
- (iv) Else set $begin = wid + 1$
- (v) Set $wid = \frac{begin + end}{2}$ Go to step 2 .

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- $i = 0$ \rightarrow ~~max size~~
- (i) Set $begin = 1$ $b = 1$ $end = 6$ $wid = (1+6)/2$
- (ii) If $A[wid] = x$ then set $loc = wid$
- else set $loc = NULL$
- (iii) x print .
- (iv) $0 <= 4$ true $A[2] != 8$ true .
- (v) Else $begin = wid + 1$ $end = 4$.

Q.

2	3	5	8	9
wid = 2 .	0	1	2	3 4

Q.

2	3	5	8	9
wid = 2 .	0	1	2	3 4

$x = 8 \rightarrow$ to search.

- $i = 0$ \rightarrow ~~max size~~
- (i) $0 < 4$ true $A[2] != 8$ false .
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- $i = 0$ \rightarrow ~~max size~~
- (i) $0 < 4$ true $A[2] != 8$ false .
- (ii) Else $begin = wid + 1$

Sorting

$a[3] = \text{true}$
 $8 = 8$ true:

① BFS

② DFS

③ Bubble Sorting :-

This sorting algorithm is comparison-based algorithm in which each pair of adjacent element is compared & elements are swapped if they are not in order.

Ex:- 10 14 2 11 6

→ 10 14 2 11 6
comp.

→ 10 14 2 11 6
comp.

→ 10 2 14 11 6 again swap

→ 10 2 11 14 6

→ 10 2 11 6 14 .

Selection Sort :-

Pass 1 : 2, 4, 13, 15, 16, 1

→ An aux sorting list is derived upto 2 parts :-

Pass 2 : 1, 2, 4, 13, 15, 16 → sorted.

Sorted & unsorted part.

$$\text{Complexity} = O(n^2)$$

The smallest element is selected from unsorted array & swapped with leftmost element

→ See :-

Pass 1 : 15, 1, 14, 12, 13, 14
swap

Pass 2 : 2, 4, 11, 15, 13, 14
swap

Pass 3 : 2, 4, 13, 15, 14
swap

Pass 4 : 2, 4, 13, 14, 15 → sorting.

① Merge Sort :-

Merge Sort is a sorting technique based on divide & conquer rule.
divide it conquer into equal parts, sort elements of it and merge them.

② Quick Sort :-

In this a range array is partitioned into 2 arrays one of which holds the value smaller than the specified value (pivot) based on which Partition is done by another part holds value greater than pivot element.

To sort the sub arrays.

Partition 1st	key value	Partition 2nd
---------------	-----------	---------------

Key > values. Pivot. Key < values.

Ex :- 42, 184, 45, 20, 60, 10, 5, 30
max size = 10.

Let's take key value 2nd elem → 42.

→ if $a[j] < \text{key}$ it not the $j++$.
it true $i++$.

Ex :- 42 84 20 45 10 60 5 30

42 < 84 false .

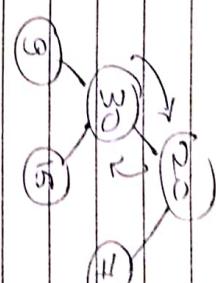
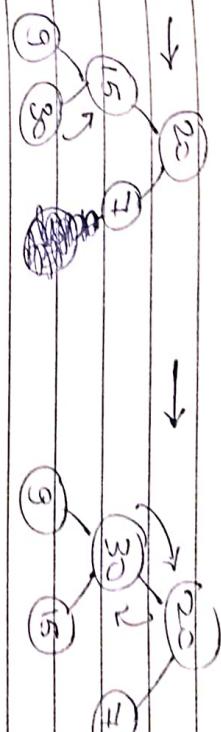
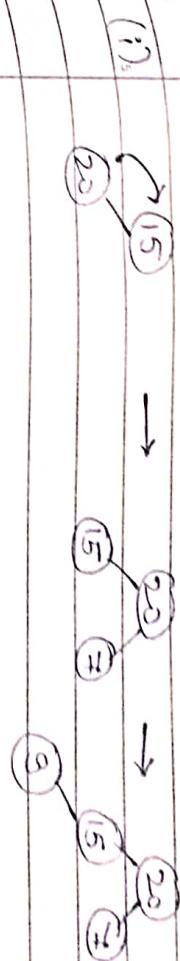
5, 10, 20, 30, 60, 45, 84.

42 84 20 45 10 60 5 30

Heap Sort

15	20	7	9	30
----	----	---	---	----

max heap.



we have to do deletion.
~~15 | 20 | 7 | 9 | 30~~ ~~20 | 15 | 7 | 9 | 30~~
 swapped.
deletion.

15	20	7	9	30
----	----	---	---	----

sooted ✓
~~15 | 20 | 7 | 9 | 30~~ ← ~~15 | 9 | 7 | 20 | 30~~

15	20	7	9	30
----	----	---	---	----

15	20	7	9	30
----	----	---	---	----

Well Sort

Current Page	1
Date	

Hashing

Current Page	1
Date	

Q. 23 29 15 19 31 4 9 5 2 ?

- Hashing is a technique what is used to uniquely identify a specific object from a group of similar objects.

• Scatter key \Rightarrow 24, 52 table size = 10.
91, 64

By K mod Tsize or Division rule.

$$24 \text{ mod } 10 = 4 \rightarrow \underline{\text{mean value}}$$

$$\frac{24}{2} \text{ rows} \Rightarrow 4$$

15	0
31	1
52	2
64	3
24	4
91	5
67	6
50	7
20	8
80	9

Haus functions :-

- Disj : K mod n.

- Mid square \Rightarrow $\begin{array}{c} 1 \\ 2 \\ 3 \end{array}$

\downarrow
 $0^2 \rightarrow$ 4th position:

- folding $\therefore 123456 \rightarrow 123$

456
 $543 \rightarrow$ part.

(4) Collision :-

\rightarrow Agr 62 & 52. no does same pos in range to psko bolte in collision.

\rightarrow cluster is the collection of hash collided values.