

Gauss forward interpolation formula implementation

	0	1	2	3	4	5
	x	y	Δy	$\Delta^2 y$	$\Delta^3 y$	$\Delta^4 y$
0	0	14	10	-2	-3	10
1	4	24	8	-5	7	
2	8	32	3	2		
3	12	35	5			
4	16	40				

$n=5$, find value at $x=9 \Rightarrow 33.11$

using Gauss forward interpolation formula.

$$f(x) = y_0 + \frac{u}{1!} \Delta y_0 + \frac{u(u-1)}{2!} \Delta^2 y_{-1} + \frac{u(u+1)(u-1)}{3!} \Delta^3 y_{-1} + \frac{u(u+1)(u-1)(u-2)}{4!} \Delta^4 y_{-2} + \dots$$

works for mid value

	x	y	Δy	$\Delta^2 y$	$\Delta^3 y$	$\Delta^4 y$
0	0	14 y_{-2}	10 Δy_{-1}	-2	-3	10 $\Delta^4 y_{-2}$
1	4	24 y_{-1}	8 Δy_{-1}	-5 $\Delta^2 y_{-1}$	7 $\Delta^3 y_{-1}$	
2	8	32 y_0	3 Δy_0	2		
3	12	35 y_1	5 Δy_1			
4	16	40 y_2				

$9 \Rightarrow 18$

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#include <stdio.h>

#include <math.h>

int main()
{
    float a[10][10],x,u1,u,y;

    int i,j,n,n1,fact=1;

    printf("enter the n\n");

    scanf("%d",&n);

    printf("enter the x");

    for(i=0;i<n;i++)

        scanf("%f",&a[i][0]);

    printf("enter the y");

    for(i=0;i<n;i++)

        scanf("%f",&a[i][1]);

    printf("enter the value to predict\n");

    scanf("%f",&x);

    for(j=2;j<n+1;j++)

    {

        for(i=0;i<n-j+1;i++)

            a[i][j]=a[i+1][j-1]-a[i][j-1];

    }

    printf("the differnce table is \n");

    for(i=0;i<n;i++)

    {

        for(j=0;j<=n-i;j++)

            printf("%.2f\t",a[i][j]);

        printf("\n");

    }

    y=a[n/2][1];

    printf("%f",y);

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u=(x-a[n/2][0])/(a[1][0]-a[0][0]);
printf("%f",u);

u1=u;
for(i=2;i<=n;i++)
{
y=y+(((i/3)*(u+1))*u1*a[n/i][i])/fact;
fact=fact*i;
u1=u1*(u-(i-1));

}
printf("the desired value is %f",y);

return 0;
}

```