Homework 3

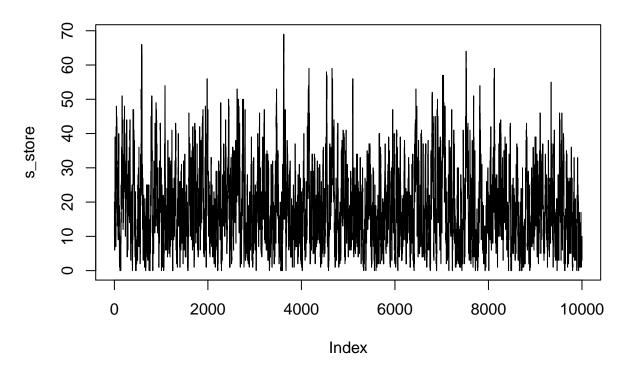
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Answer to the Question Number 1

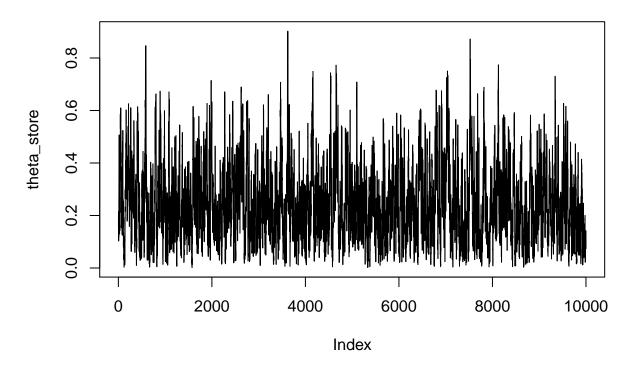
```
set.seed(7)
# Initial values
a0 = 2.0
b0 = 6.4
n = 74
s = 16
MLE_theta <- s/n</pre>
{\tt MLE\_theta}
## [1] 0.2162162
M = 10000
# storing simulated samples
s_store = matrix(0,M)
theta_store = matrix(0,M)
# for loop start
for (iter in 1:M)
 theta = rbeta(1, a0+s, b0+n-s)
 s = rbinom(1, n, theta)
 theta_store[iter,] = theta
  s_store[iter,] = s
density_s = table(s_store)/M
plot(s_store,type = "l", main = "Trace plot for s")
```

Trace plot for s



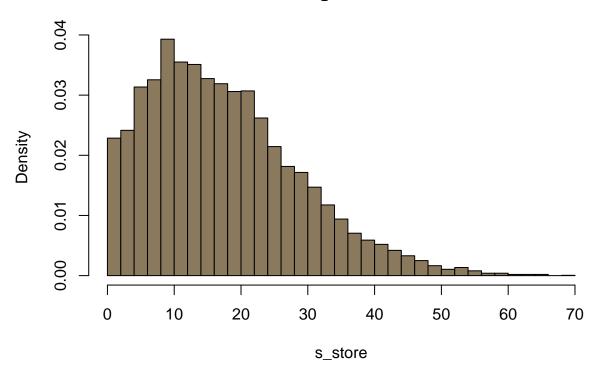
plot(theta_store,type = "1", main = "Trace plot for theta")

Trace plot for theta



hist(s_store, breaks = 30, freq = F, col = "navajowhite4", main = "Histogram for s")

Histogram for s



```
posterior_median_theta <- median(theta_store)
posterior_median_theta</pre>
```

[1] 0.2211888

So, posterior median of θ based on is closed to the maximum likelihood estimate s/n.

We know median is insensitive to outlier. So, posterior median is insensitive to initial values.

Answer to the Question Number 2 (Bonus problem)

```
set.seed(7)
# Initial values

a0 = 2.0
b0 = 6.4
s = 16
n = 20
lambda = 64

M = 10000
# storing simulated samples
s_store = matrix(0,M)
```

```
theta_store = matrix(0,M)
n_store = matrix(0,M)

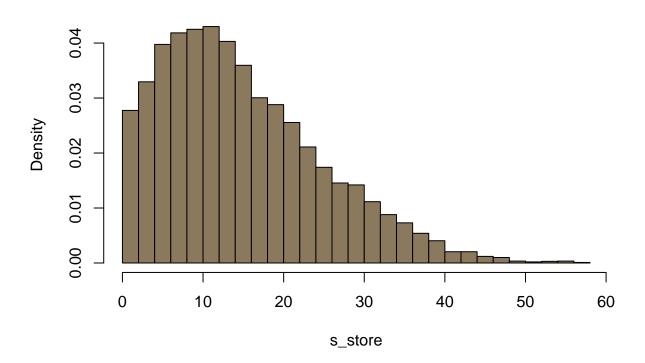
# for loop start

for (iter in 1:M) {
    theta = rbeta(1, a0+s, b0+n-s)
    n = s + rpois(1,(1-theta)*lambda)
    s = rbinom(1, n, theta)

    theta_store[iter, ] = theta
    n_store[iter, ] = n
    s_store[iter, ] = s
}

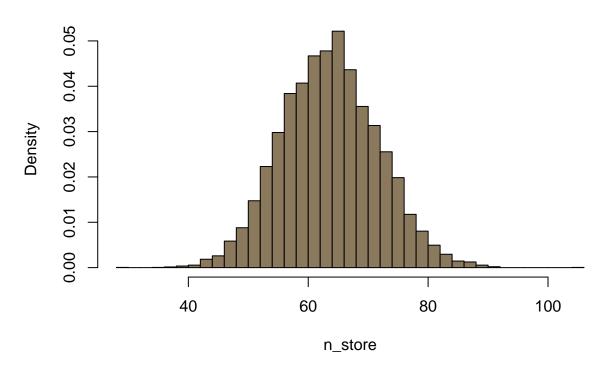
hist(s_store, breaks = 30, freq = F, col = "navajowhite4", main = "Histogram for s")
```

Histogram for s



```
hist(n_store, breaks = 30, freq = F, col = "navajowhite4", main = "Histogram for n")
```

Histogram for n



```
posterior_median_theta <- median(theta_store)
posterior_median_theta</pre>
```

[1] 0.216351

Yes, this posterior median of theta is similar to the posterior median of the problem 1, because theta is independent of n but s depends on n.