

CLASS: Induction

- Due Feb 15 at 11:59pm
- Points 8
- Questions 8
- Time Limit None
- Allowed Attempts Unlimited

Instructions

This CLASS assignment is a introduction to Induction.

You have multiple attempts in answering the question

Chapter 5 Note <https://www.youtube.com/watch?v=ZIlcMafP36E&list=PLiwEbczHeZcuf7VyebyKcVDqfViUkqfh&index=7&t=931s>

Take the Quiz Again

Attempt History

	Attempt	Time	Score
LATEST	<u>Attempt 1</u>	9 minutes	8 out of 8

⚠ Correct answers are hidden.

Score for this attempt: 8 out of 8

Submitted Feb 15 at 7:42pm

This attempt took 9 minutes.



Question 1

1 / 1 pts

Induction: The sum of first n natural numbers is $n(n+1)/2$ <https://www.youtube.com/watch?v=sVL6r4oCnSw&list=PLiwEbczHeZcuf7VyebyKcVDqfViUkqfh&index=136>

Mathematical Induction Note.pdf (<https://deanza.instructure.com/courses/33250/files/10862361?wrap=1>) https://deanza.instructure.com/courses/33250/files/10862361/download?download_frd=1

Now answer the following question:

What is the every first step in Mathematical Induction?

- ☐ Consider the formula be true for a given number k

- ☐ Consider the formula be true for $k=1$
- ☒ Check the domain, and plug in the smallest value



Question 2

1 / 1 pts

Induction: The sum of first n natural numbers is $n(n+1)/2$ [↗\(https://www.youtube.com/watch?v=sVL6r4oCnSw&list=PLiwEbczHeZcuf7VyebtyKcVDqfViUkqfh&index=136\)](https://www.youtube.com/watch?v=sVL6r4oCnSw&list=PLiwEbczHeZcuf7VyebtyKcVDqfViUkqfh&index=136)

What a closed form is? [↗\(https://www.youtube.com/watch?v=fgiAohoV6bU&list=PLiwEbczHeZcuf7VyebtyKcVDqfViUkqfh&index=137\)](https://www.youtube.com/watch?v=fgiAohoV6bU&list=PLiwEbczHeZcuf7VyebtyKcVDqfViUkqfh&index=137)

Now answer the following question:

In the first example in this lecture, what is the very first value that we select?

$$1 + 2 + \cdots + n = \frac{n(n+1)}{2}.$$

- ☐ 0
- ☒ 1
- ☐ 2



Question 3

1 / 1 pts

Sum of Geometric Sequence Using Induction [↗\(https://www.youtube.com/watch?v=5WqNU5oj4Mc&list=PLiwEbczHeZcuf7VyebtyKcVDqfViUkqfh&index=138\)](https://www.youtube.com/watch?v=5WqNU5oj4Mc&list=PLiwEbczHeZcuf7VyebtyKcVDqfViUkqfh&index=138)

Now answer the following question:

What is the name of the following Sum?

$$\sum_{i=0}^n r^i = \frac{r^{n+1} - 1}{r - 1}.$$

☐ Arithmetic Sum

☒ Geometric Sum

☐ Harmonic Sum



Question 4

1 / 1 pts

[2^2n -1 is divisible by 3 Using Induction](https://www.youtube.com/watch?v=eobK_k8cfIY&list=PLiwEbczHeZcuf7VyebyKcVDqfViUkqfh&index=140)  **(https://www.youtube.com/watch?v=eobK_k8cfIY&list=PLiwEbczHeZcuf7VyebyKcVDqfViUkqfh&index=140)**

Now answer the following question:

In the example in this lecture, what is the very first value that we select?

For all integers $n \geq 0$, $2^{2n} - 1$ is divisible by 3.

Make sure you feel comfortable about solving these types of problems.

☒ 0

☐ 1

☐ 2

☐ 3



Question 5

1 / 1 pts

[2^2n -1 is divisible by 3 Using Induction](https://www.youtube.com/watch?v=eobK_k8cfIY&list=PLiwEbczHeZcuf7VyebyKcVDqfViUkqfh&index=140)  https://www.youtube.com/watch?v=eobK_k8cfIY&list=PLiwEbczHeZcuf7VyebyKcVDqfViUkqfh&index=140

Now answer the following question:

Which law help to write the following?

$$\begin{aligned} 2^{2(k+1)} - 1 &= 2^{2k+2} - 1 \\ &= 2^{2k} \cdot 2^2 - 1 \end{aligned}$$

- ☐ Associative law
- ☒ Exponents Law
- ☐ Inductive Law
- ☐ Factoring Law



Question 6

1 / 1 pts

[2^2n -1 is divisible by 3 Using Induction](https://www.youtube.com/watch?v=eobK_k8cfIY&list=PLiwEbczHeZcuf7VyebyKcVDqfViUkqfh&index=140)  https://www.youtube.com/watch?v=eobK_k8cfIY&list=PLiwEbczHeZcuf7VyebyKcVDqfViUkqfh&index=140

Now answer the following question:

Which law help to write the last line?

$$\begin{aligned} 2^{2(k+1)} - 1 &= 2^{2k+2} - 1 \\ &= 2^{2k} \cdot 2^2 - 1 && \text{by the laws of exponents} \\ &= 2^{2k} \cdot 4 - 1 \\ &= 2^{2k}(3 + 1) - 1 \\ &= 2^{2k} \cdot 3 + (2^{2k} - 1) && \text{by} \end{aligned}$$

- ☐ Exponents Law
- ☐ Inductive Law
- ☒ Law of Algebra
- ☐ Idempotent Law



Question 7

1 / 1 pts

[2n+1 is less than 2^n Using Induction](https://www.youtube.com/watch?v=tDFDDH3BEzI&list=PLiwEbczHeZcuf7VyebtyKcVDqfViUkqfh&index=141)  **[_ \(https://www.youtube.com/watch?v=tDFDDH3BEzI&list=PLiwEbczHeZcuf7VyebtyKcVDqfViUkqfh&index=141\)](https://www.youtube.com/watch?v=tDFDDH3BEzI&list=PLiwEbczHeZcuf7VyebtyKcVDqfViUkqfh&index=141)**

Now answer the following question:

In proving the following inequality, what is the very first number to plug in, in the basis step?

$$2n + 1 < 2^n.$$

- ☐ 0
- ☐ 1
- ☐ 2
- ☒ 3



Question 8

1 / 1 pts

I certify that I took note of all definitions and formulas. They are neat and organized.

- ☒ True
- ☐ False

Quiz Score: 8 out of 8