

* Unit - 2 *

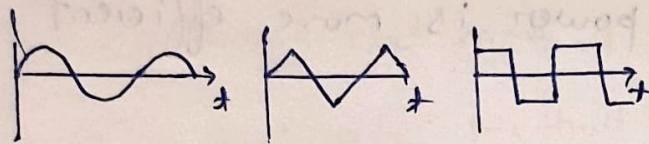
Singal Phase AC Current

- Difference b/w AC & DC.

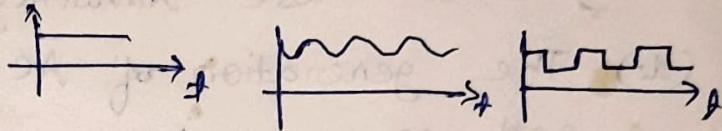
* Alternating Current

* Direct Current

- V & C change its polarity periodically.



- V & C polarity remains constant



- Energy loss is less

- Energy loss is more

- Less powerfull as it becomes max for few times.

- more powerful as it is always max & travel with full speed.

- transmitted upto a long distance

- can't be transmitted upto long distance

- AC can be converted into DC by using "Rectifier"

- DC can be converted by using "Inverter".

- Low cost.

- High cost.

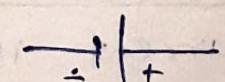
- Frequency is around 50Hz - 60Hz

- Frequency is zero

- AC motor & other AC applicances more durable & Robust.

- DC motor & other DC applicances less durable & robust.

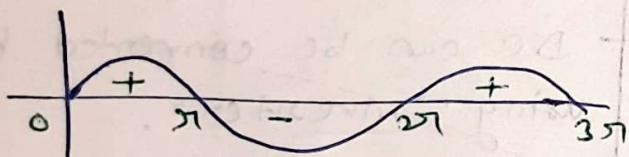
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So AC circuit are electrical circuits which are operated by AC energy sources such as alternate. → there circuits are more complicated than DC circuits. Due to there time varying factors, we mostly use AC systems.

AC systems offers many advantages over DC Systems. These Advantages are following.

- (1) The generation of AC power is more efficient and economical.
- (2) The AC voltage can easily step-up & step down.
- (3) The AC motors are less expensive & more efficient.
- (4) The AC System are used for generation, transmission & distribution of electrical power.



Positive \Rightarrow 0 to π

Negative \Rightarrow π to 2π

→ AC current may define as a current whose magnitude changes periodically with time.

AC Cycle consists two parts, first positive half and second negative half.

Instantaneous value Inst. value of an AC current is the magnitude of the AC current instant or particular time.

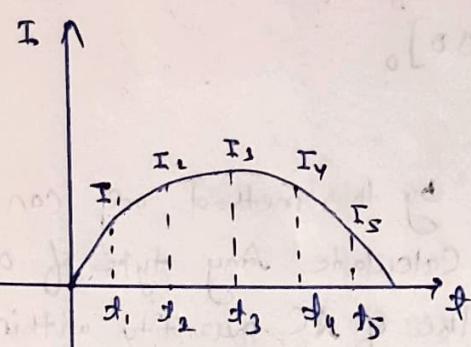
$$(I = \frac{dq}{dt} = \text{Inst})$$

• Average Value:- The avg value of an AC quantity is define as the avg of all instantaneous value of the AC quantity over one cycle.

For calculate avg value, following methods are used -

- (i) Mid Ordinate Method
- (ii) Analytical method

(i) Mid ordinate Method :-



$$I_{av} = \frac{\sum I_n}{n}$$

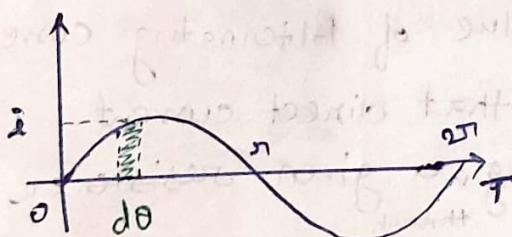
$$I_{av} = \frac{I_1 + I_2 + I_3 + \dots + I_n}{n}$$

Here n is total number of time interval.

$$I_{av} = \frac{\text{Area of Power}}{\text{Base}}$$

and $I_1, I_2, I_3, \dots, I_n$ are insto value of current of particular time interval.

(ii) Analytical Method:-



$$i = I_m \sin \theta$$

Area of the Strip

$$dA = i d\theta$$

A of half cycle can be find out by

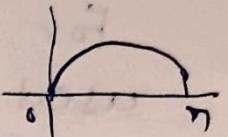
$$\therefore \int dA = \int i d\theta \rightarrow (i)$$

In this method, we consider a strip of thickness of $d\theta$ and the ordinate for the strip will be i .

$$A = \int_0^{\pi} i d\theta \quad (\because i = I_m \sin \theta)$$

$$\Rightarrow A = \int_0^{\pi} I_m \sin \theta d\theta \quad \text{---ii}$$

$$\Rightarrow A \leftarrow \therefore I_{av} = \frac{\text{Area of Half Wave}}{\text{Base of Half Wave}}$$



Base = $\pi - 0$
Area

$$I_{av} = \frac{\int_0^{\pi} I_m \sin \theta d\theta}{\pi - 0}$$

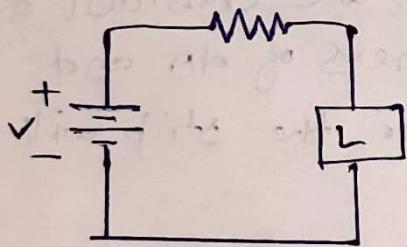
$$I_{av} = \frac{I_m}{\pi} [\cos \theta]_0^{\pi}$$

$$I_{av} = -\frac{2}{\pi} I_m$$

by this method we can calculate any type of any value of AC quantity within any time period.

RMS Value [Root mean Square]:-

→ The RMS value is effective value of an AC quantity.

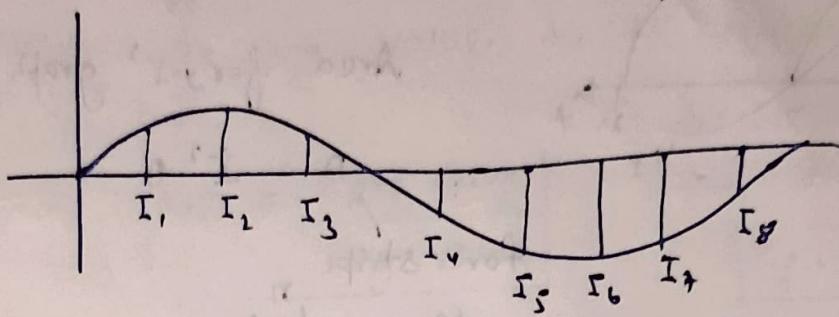


The RMS value of Alternating current is equal to that direct current which is flowing through a given resistance.

(Circuit) resistive circuit for a given time interval, produces same heat as produced by the alternating current when flowing through the same circuit for the same duration of time.

We have two methods to find RMS value.

(i) Middle ordinate method :-



Q. When AC flows through a conductor with R resistor.

$$H_0 = \frac{I^2 R t}{Jn}$$

$$H_n = \frac{1}{Jn} [I_n^2 R \Delta t]$$

for all time period

$$H_{AC} = \frac{1}{J} \left[\frac{I_1^2 R \Delta t}{n} + \frac{I_2^2 R \Delta t}{n} + \frac{I_3^2 R \Delta t}{n} + \dots + \frac{I_n^2 R \Delta t}{n} \right] \\ (\Delta t_1 = \Delta t_2 = \dots = \Delta t_n)$$

$$H_{AC} = \frac{R \Delta t}{J} \left[\frac{I_1^2 + I_2^2 + \dots + I_n^2}{n} \right]$$

When DC flows through that same circuit

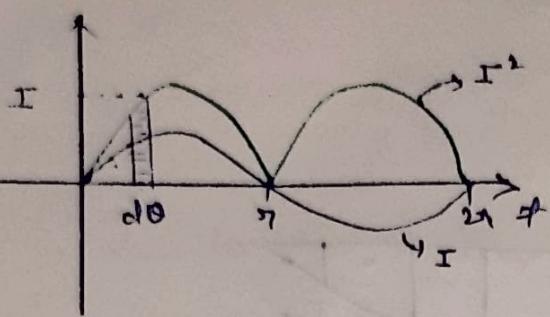
$$H_{DC} = \frac{I^2 R \Delta t}{J}$$

for rms value $H_{AC} = H_{DC}$

$$\frac{I_{rms}^2 R \Delta t}{J} = \frac{R \Delta t}{J} \left[\frac{I_1^2 + I_2^2 + \dots + I_n^2}{n} \right]$$

$$I_{rms} = \sqrt{\frac{I_1^2 + I_2^2 + \dots + I_n^2}{n}}$$

(ii) Analytical Method:-



$$\therefore I = I_m \sin \theta$$

$$I^2 = I_m^2 \sin^2 \theta$$

Area for I^2 graph

$$A = I^2 \cdot \theta$$

for strip

$$dA = \int_{0}^{\pi} I^2 d\theta \quad (\text{over the half cycle})$$

$$I_{rms}^2 = \frac{\int_0^{\pi} I^2 d\theta}{t_2 - t_1} \quad \left(\because \sin^2 \theta = \frac{1 - \cos 2\theta}{2} \right)$$

$$I_{rms}^2 = \int_0^{\pi} I_m^2 \sin^2 \theta d\theta$$

$$I_{rms}^2 = \frac{I_m^2}{\pi} \int_0^{\pi} \left[\frac{1 - \cos 2\theta}{2} \right] d\theta$$

$$I_{rms}^2 = \frac{I_m^2}{\pi} \left[\frac{\theta}{2} - \frac{\sin 2\theta}{4} \right]_0^{\pi}$$

$$I_{rms}^2 = \frac{I_m^2}{\pi} \left[\frac{\pi}{2} \right]$$

$$I_{rms}^2 = \frac{I_m^2}{2}$$

$$I_{rms} = \boxed{\frac{I_m}{\sqrt{2}}}$$

I_{avg} for half wave

$$\text{reactive} = \frac{1}{2} (\text{I}_{avg} \text{ of half cycle})$$

$$I_{avg} = 0.318 I_m$$

* Formula for
mean time Period

$$I_{avg} = \frac{\int_{t_1}^{t_2} I dt}{\int_{t_1}^{t_2} dt}$$

* for Full cycle

$$I_{avg} = 0 \quad (0 \text{ to } 2\pi)$$

* for half cycle \oplus

$$I_{avg} = \frac{2I_m}{\pi} \quad (0 \text{ to } \pi)$$

$$I_{avg} = -\frac{2I_m}{\pi} \quad (\pi \text{ to } 2\pi)$$

• Form Factor (K_F):-

Form factor represents the relation between Rms value & avg value. It is defined as the ratio of rms value to avg. value to AC quantity. It is denoted by K.F.

for sinusoidal varying current

$$K.F. = \frac{\text{Rms value}}{\text{Avg value}}$$

$$K_F = 1.11$$

• Peak Factor (K_P):-

It is defined as the ratio of max value to rms value of AC quantity. It is denoted by K_P

for sinusoidal varying current

$$K_P = \frac{\text{max value}}{\text{Rms value}}$$

$$K_P = 1.414$$

Terminology of AC Waves:-

$$I = I_m \sin(\omega t + \theta) \quad [\text{Sinusoidal wave form}]$$

Inst current
value of AC
quantity.

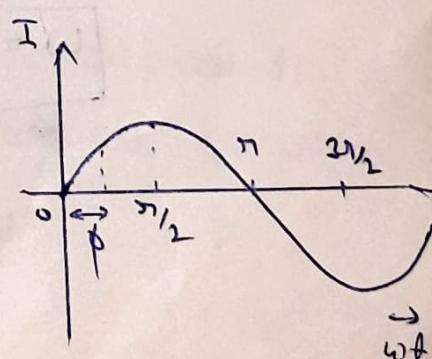
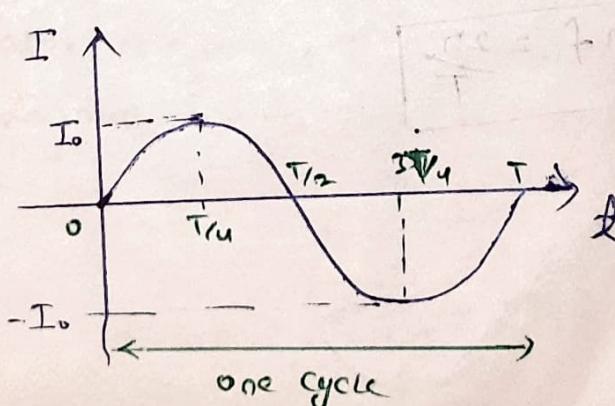
Angular representation.

max Current

$\omega \rightarrow$ Angular frequency

$t \rightarrow$ time

$\theta \rightarrow$ Phase angle.



(i) Wave form: A curve obtain by plotting its value against time is called wave form of AC Quantity.

(ii) Time Period: The time of completing one cycle of the AC wave is called its time period.

During the time 0 to 2π wave change its angle

$$\omega T = 2\pi$$

$$T = \frac{2\pi}{\omega}$$

(iii) Frequency: Frequency is the number of cycle that occurs in one second.

$$\text{Unit} \Rightarrow \text{Hz} \quad (\text{1/sec})$$

$$f = \frac{1}{T}$$

(iv) Amplitude: The maximum positive or negative value of an alternating quantity is called Amplitude.
[Max displacement from axis]

(v) Cycle: The value of Sine wave repeat after 2π radians. One complete set of positive & negative value of the function is called a cycle.

(vi) Angular Frequency:

Angular frequency (ω) is equal to the number of radian covered in one seconds.

$$\omega = 2\pi f = \frac{2\pi}{T}$$

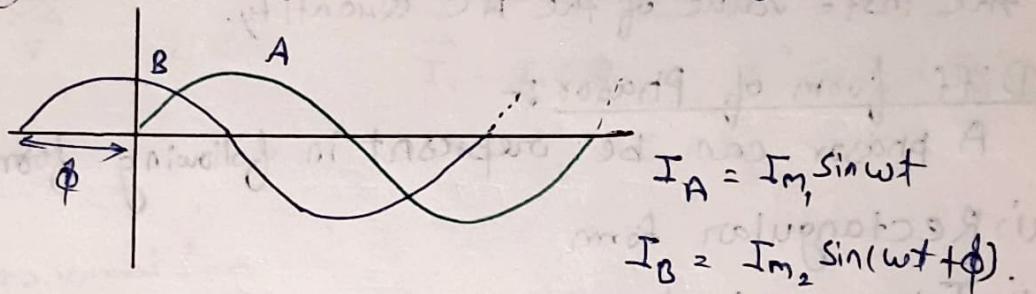
(vii) Phase: Phase is the fraction of the time period or cycle that has elapsed since it last passed from the chosen origin.

Phase angle is angular displacement from a reference point. (Angular component of periodic wave)

$$\boxed{\phi = \frac{2\pi t}{T}}$$

(viii) Phase Difference: This term is used to compare to phase of two alternating quantity.

It is a measurement in degrees of how much one wave lead another wave or lag behind that wave.



* Phase Representation of AC Quantity:

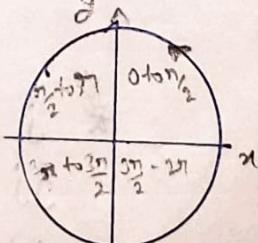
A phasor is a complex number used to represent the magnitude and phase of a sinusoidal function.

A phasor is a line of definite length rotating in an anticlockwise direction at a constant angular velocity ω .

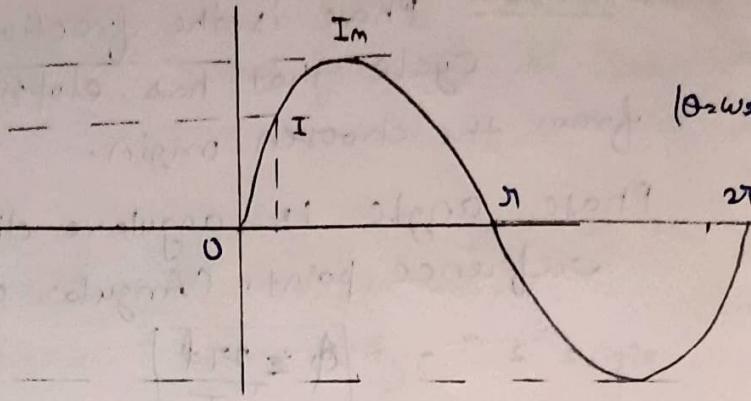
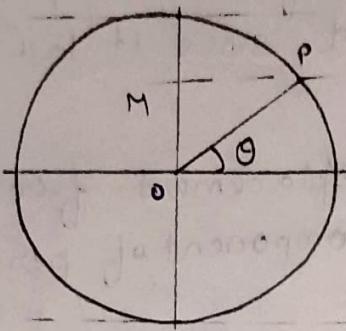
length of phasor line = max value of AC

That has both magnitude & direction.

In a phasor diagram, the phasors are represented by arrows which rotates with angular frequency of ω .



Anticlock



* Properties of Phasor

- (i) The length of a phasor is proportional to the max value of the AC Quantity.
- (ii) The projection of a phasor on the vertical axis gives the inst. value of the AC Quantity.

* Different forms of Phasor :-

A phasor can be represented in following forms:-

- (i) Rectangular form
- (ii) Trigonometrical form
- (iii) Polar form
- (iv) Exponential form.

(1) Rectangular form

$$\vec{V} = a + jb$$

magnitude of phase

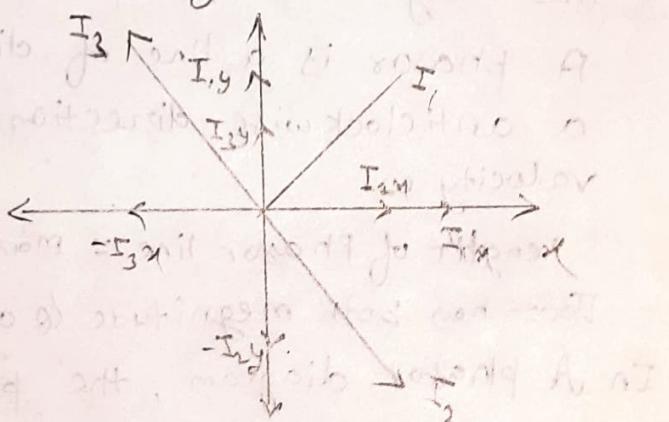
$$|V| = \sqrt{a^2 + b^2}$$

$$\phi = \tan^{-1}(b/a)$$

For $I_1 = I_{1x} + j I_{1y}$

$$I_2 = I_{2x} - j I_{2y}$$

$$I_3 = -I_{3x} + j I_{3y}$$



j = phase shift b/w

x & y axis

* $j = x + iy$

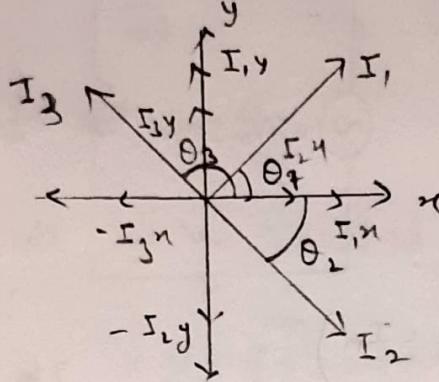
$$jj = x + iy$$

$$jj' \Rightarrow x + iy$$

* Trigonometric form

$$a = v \cos \phi, b = v \sin \phi$$

$$\vec{v} = v(\cos \phi + j \sin \phi)$$



Eg

$$I_1 = I_1 \cos \theta_1 + j I_1 \sin \theta_1$$

$$I_2 = I_2 \cos \theta_2 - j I_2 \sin \theta_2$$

$$I_3 = -I_3 \cos \theta_3 + j I_3 \sin \theta_3$$

* Polar form

$$\vec{v} = |v| \angle \phi$$

by previous ex

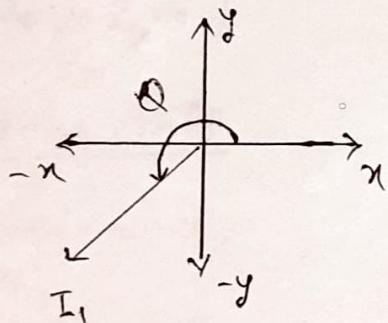
$$\vec{I}_1 = I_1 \angle \theta_1, \quad \vec{I}_2 = I_2 \angle \theta_2$$

$$\vec{I}_3 = I_3 \angle \theta_3$$

Note Exponential form

$$\vec{I}_1 = I_1 e^{j\theta_1}, \quad \vec{I}_2 = I_2 e^{j\theta_2}, \quad \vec{I}_3 = I_3 e^{j\theta_3}$$

O



$$I_1 = -I_1 \cos 240^\circ - I_1 \sin 240^\circ j$$

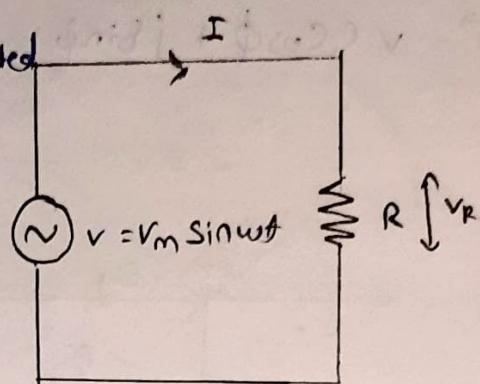
$$I_1 = +0.5 I_1 + 0.86 j I_1$$

$$\theta = 240^\circ$$

● AC Circuits

(i) AC circuit with Pure Resistance (R):

Consider a pure resistor R connected across an alternating voltage source.



$$(i) I = \frac{v}{R} = \frac{V_m \sin \omega t}{R}$$

$$I = I_m \sin \omega t \quad (\text{where } \frac{V_m}{R} = I_m)$$

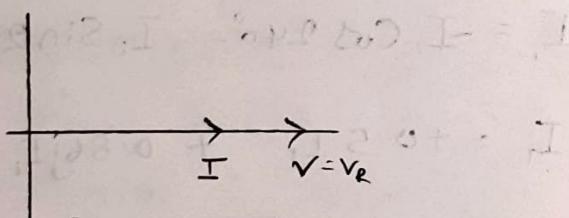
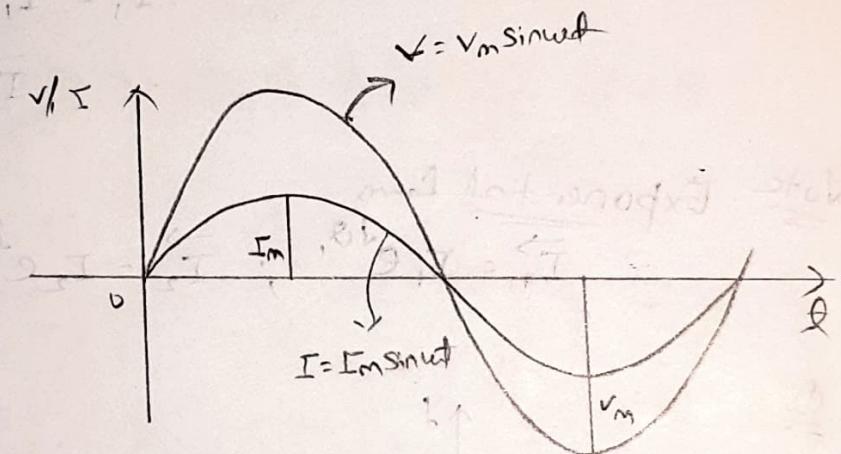
$$\text{viii) } Z = \frac{v}{I} = \frac{V_m / I_m}{I_m / I_m} = \frac{V_m}{I_m} \quad (\text{Impedance})$$

$$Z = \frac{V_m}{V_m / R}$$

$$\boxed{Z = R}$$

(ii) Phase Diff

$$\boxed{\phi = 0^\circ}$$



(in same phase)

(iv) Power Consumed $P = VI$

$$P = V_m \sin \omega t \cdot (I_m \sin \omega t)$$

$$P = V_m I_m \sin^2 \omega t$$

$$P = \frac{V_m I_m}{2} (1 - \cos 2\omega t)$$

Average Power

$$\boxed{P_{av} = \frac{V_m}{T/2} \cdot \frac{I_m}{T/2} = VI}$$

(ii) AC Circuit with Pure Inductor L

Consider a pure inductor L connected with an alternating voltage source.

$$V = L \frac{dI}{dt}$$

$$\therefore V = V_m \sin \omega t$$

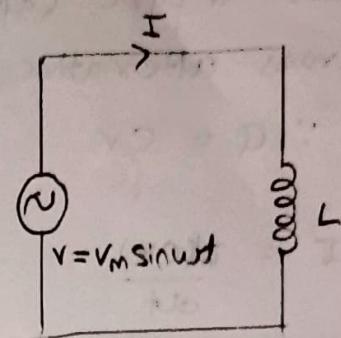
$$V_m \sin \omega t = L \frac{dI}{dt}$$

$$dI = \frac{V_m}{L} \sin \omega t dt$$

$$dI = \frac{V_m}{L} \int \sin \omega t dt$$

$$I = \frac{V_m}{\omega L} \cos \omega t$$

$$I = I_m \sin(\omega t - \frac{\pi}{2})$$



$$(Let \cancel{V_m} \omega L = X_L)$$

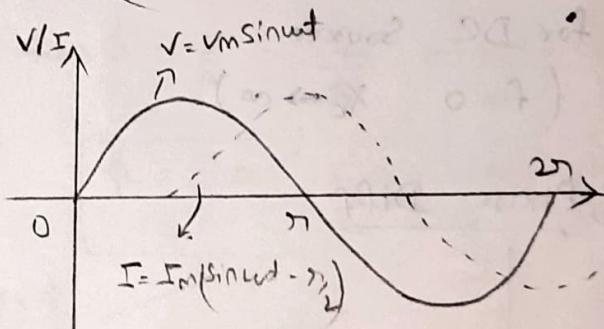
$$(I_{max} = \frac{V_m}{\omega L} = \frac{V_m}{X_L})$$

(ii) Impedance

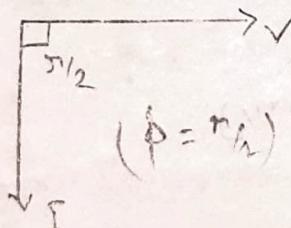
$$Z = X_L = \omega L$$

Unit = ohm

$$(for DC \\ I=0 \Rightarrow X_L=0)$$



(iii) Phase Diff



(iv) Power Consumed

$$P = VI = V_m \sin \omega t \cdot I_m \sin(\omega t - \frac{\pi}{2})$$

$$P = V_m I_m \sin^2 \omega t$$

$$or P = \frac{V_m^2 \sin^2 \omega t}{2X_L}$$

(iii) AC Circuit with Pure Capacitance :-

Consider a pure capacitor C connected across alternative voltage source.

$$\therefore Q = CV$$

$$I = \frac{dq}{dt}$$

(i)

$$I = \frac{d(CV)}{dt}$$

$$I = C \frac{d(V_m \sin \omega t)}{dt}$$

$$I = \omega C V_m \cos \omega t$$

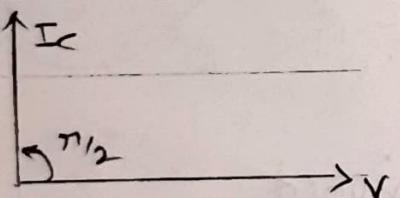
$$I = \frac{V_m}{X_C} \sin(\omega t + \pi/2)$$

$$\boxed{I_c = \frac{V_m}{X_C} \sin(\omega t + \pi/2)}$$

for DC Source

$$(f=0 \quad X_C \rightarrow \infty)$$

iii) Phase Diff

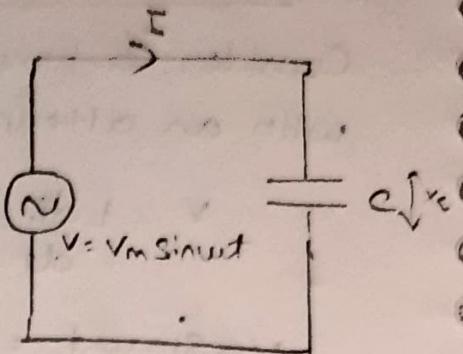


iv) Power Consumed

$$P = VI = V_m \sin \omega t \cdot I_m \sin(\omega t + \pi/2)$$

$$P = V_m I_m \sin \omega t \cos \omega t$$

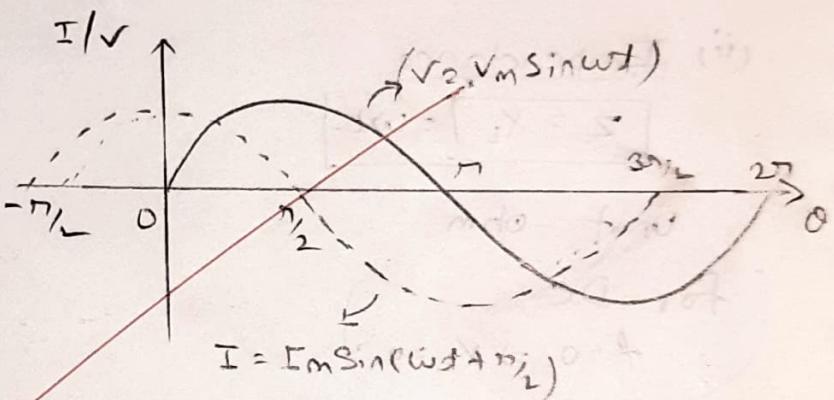
$$\boxed{P = \frac{V_m I_m}{2} \sin 2\omega t}$$



$$\text{Let } \frac{1}{\omega C} = X_C$$

(ii) (Capacitive impedance)

$$(I_{max} = \frac{V_m}{X_C} = V_m \times \omega C)$$



(iv) AC Circuit with R-L :-

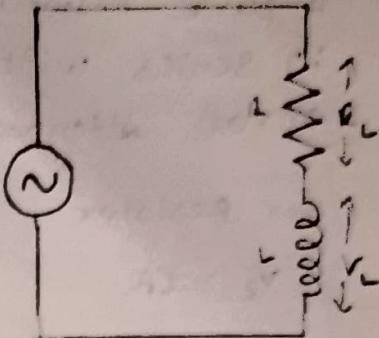
A pure resistor R connected with in series with a pure inductor L across an alternating voltage source (V)

for Resistor

$$V_R = IR$$

for Inductor

$$V_L = IX_L$$



$$V_{\text{tot}} = \vec{V} = \vec{V}_R + \vec{V}_L$$

$$I(R + X_L)$$

$$|V| = \sqrt{V_R^2 + V_L^2}$$

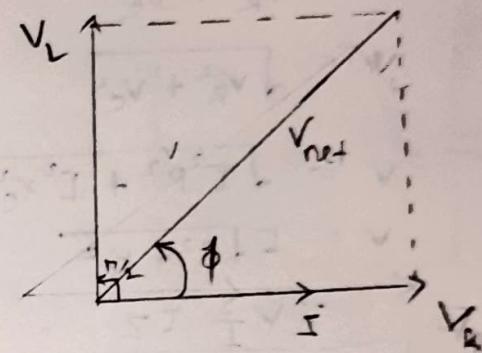
$$V = \sqrt{I^2 R^2 + I^2 X_L^2}$$

$$\therefore V = I \cdot Z$$

$$IZ = I \sqrt{R^2 + X_L^2}$$

$$Z = \sqrt{R^2 + X_L^2}$$

(ii) Impedance



$$(Z = R\hat{i} + X_L\hat{j})$$

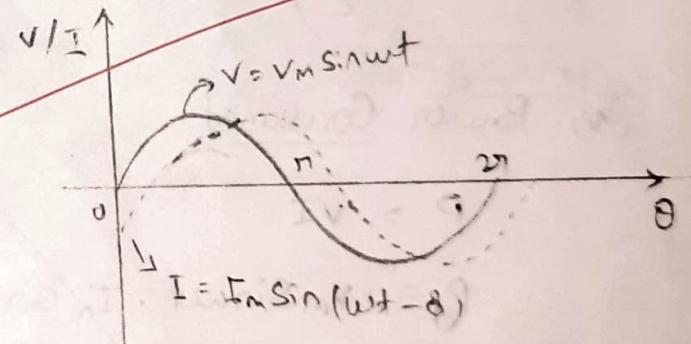
$$\tan \phi = \frac{L}{R} = \frac{X_L}{R} = \frac{\omega L}{R}$$

$$\phi = \tan^{-1}\left(\frac{X_L}{R}\right) = \tan^{-1}\left(\frac{\omega L}{R}\right)$$

(i) Current

$$I_m = \frac{V_m}{Z}$$

$$I = I_m \sin(\omega t - \phi)$$



(iii) Phase diff =

$$\phi = \tan^{-1}\left(\frac{X_L}{R}\right)$$

(iv) Power Consumed

$$P = VI = V_m \sin \omega t \cdot I_m \sin(\omega t - \phi)$$

$$P = V_m I_m [\sin \omega t (\sin \omega t \cos \phi - \cos \omega t \sin \phi)]$$

(v) AC circuit with R-C in series

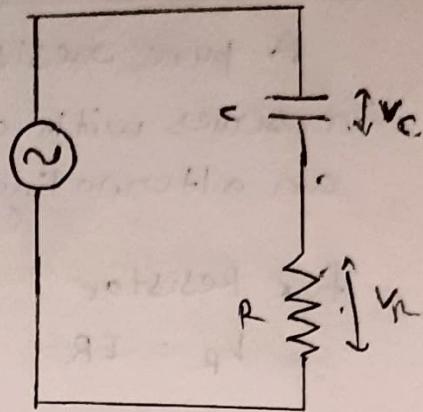
A pure resistance R connected with in series with a pure capacitor across Alternating source.

for Resistor

$$V_R = IR$$

for Capacitor

$$V_C = I X_C$$



$$(i) \quad \vec{V} = \vec{V}_R + \vec{V}_C$$

$$V = \sqrt{V_R^2 + V_C^2}$$

$$V = \sqrt{I^2 R^2 + I^2 X_C^2}$$

$$V = I \sqrt{R^2 + X_C^2}$$

$$\therefore V = IZ$$

$$Z = \sqrt{R^2 + X_C^2} \quad (\text{Impedance})$$

Current

$$I = I_m \sin(\omega t + \phi)$$

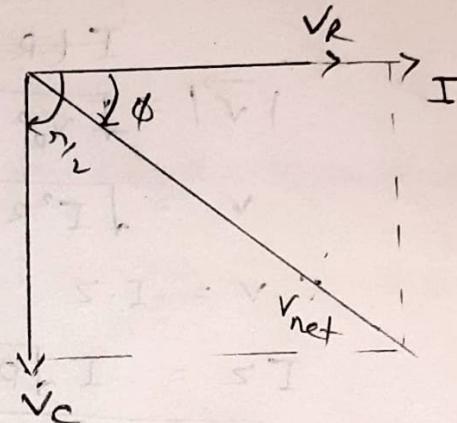
$$(I_m = \frac{V_m}{Z})$$

(ii) Power Consumed

$$P = VI$$

$$P = V_m \sin \omega t \cdot I_m \sin(\omega t + \phi)$$

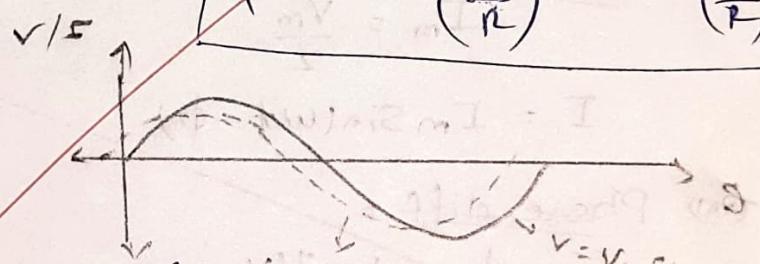
$$P = V_m I_m \sin \omega t \sin(\omega t + \phi)$$



(ii) Phase Diff

$$\tan \phi = \frac{V_C}{V_R} = \frac{X_C}{R}$$

$$\phi = \tan^{-1} \left(\frac{X_C}{R} \right) = \tan^{-1} \left(\frac{V_C}{V_R} \right)$$



$$V = V_m \sin \omega t \quad I = I_m \sin(\omega t + \phi)$$

M) AC Circuit with LCR :-

A pure Resistance, and a pure capacitor connected with in series with a pure inductor(L). across Alternating source.

for Resistor

$$V_R = IR$$

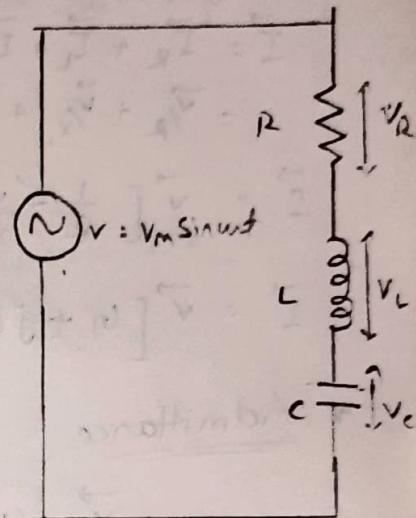
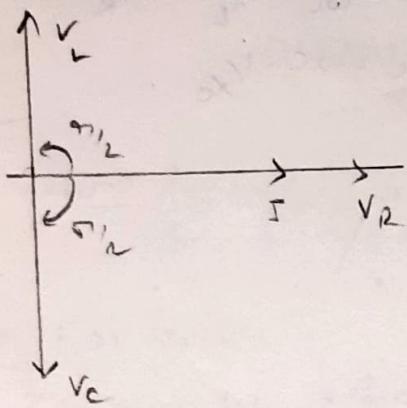
for Capacitor

$$V_C = IX_C$$

for Inductor

$$V_L = IX_L$$

$$(i) \vec{V} = \vec{V}_R + \vec{V}_L + \vec{V}_C$$



Phase Diff

$$\theta = |X_L - X_C|$$

(ii) Impedance

$$\vec{V} = \vec{V}_R + \vec{V}_L + \vec{V}_C$$

$$\tan \phi = \frac{\theta}{R} = \frac{X_L - X_C}{R}$$

$$V = \sqrt{V_R^2 + V_L^2}$$

$$\tan \phi = \frac{X_L - X_C}{R}$$

$$V = I [R + (X_L - X_C)j]$$

$$\phi = \tan^{-1} \left(\frac{X_L - X_C}{R} \right)$$

$$V = I \sqrt{R^2 + (X_L - X_C)^2}$$

$$V = I \cdot Z$$

$$Z = \sqrt{R^2 + (X_L - X_C)^2}$$

(iii) Current : $V_m = V_m \sin \omega t$ then $I = I_m \sin(\omega t \pm \phi)$

$\rightarrow +$ when $X_C > X_L \rightarrow$ Current leads

$\rightarrow -$ when $X_L > X_C \rightarrow$ Current lags

Note For Parallel Series Connection

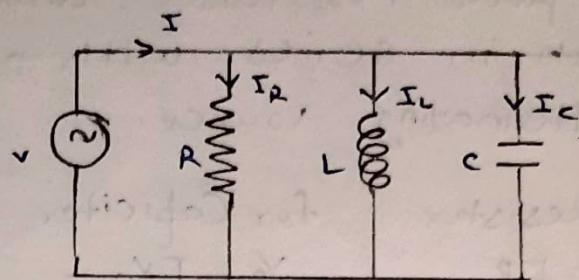
Apply KCL

$$\vec{I} = \vec{I}_R + \vec{I}_L + \vec{I}_C$$

$$= \frac{\vec{V}}{R} + \frac{\vec{V}}{X_L} + \frac{\vec{V}}{X_C}$$

$$\vec{I} = \vec{V} \left[\frac{1}{R} - \frac{j}{X_L} + \frac{j}{X_C} \right]$$

$$\vec{I} = \vec{V} [G + j(B_C - B_L)]$$



$$\begin{cases} B_L = \frac{1}{\omega L} = \frac{1}{X_L} & G = \frac{1}{R} \\ B_C = \omega C = \frac{1}{X_C} \end{cases}$$

* Admittance

$$\vec{Y} = (G + j(B_C - B_L))$$

* Phase Angle

$$\phi = \tan^{-1} \left(\frac{B_C - B_L}{G} \right)$$

• Real Power :-

In a simple ac circuit consisting of a source & load, both the current & voltage are sinusoidal. If the load is purely resistive, the product of voltage & current at every instant is positive.

$$P = V_{rms} I_{rms} \cos \phi$$

$$P = I_{rms}^2 R$$

Unit = watt

• Reactive Power :-

It is the power developed in the inductive reactance of the circuit -

$$Q = V_{rms} I_{rms} \sin \phi$$

$$Q = I_{rms}^2 X_L$$

Unit = Volt-ampere-reactive.

* Apparent Power

It is given by the product of rms value of applied voltage & circuit current -
unit \Rightarrow Volt Amp (VA)

$$S = V_{rms} I_{rms}$$

* Power triangle

$$\text{Real Power } P = I^2 R \quad \text{Reactive Power } Q = I^2 X_L$$

$$\text{Apparent Power } S = I^2 Z$$

$$\text{Here } [S = \sqrt{P^2 + Q^2}] \Rightarrow Z = \sqrt{R^2 + X_L^2}$$

* Power Factor

It may be defined as

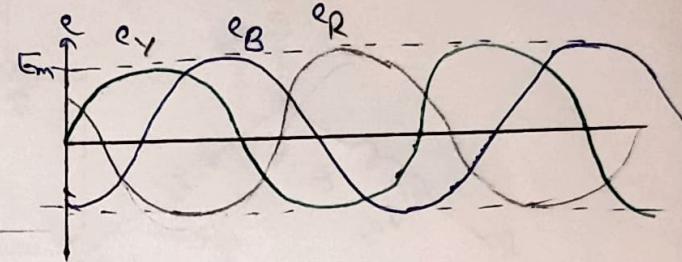
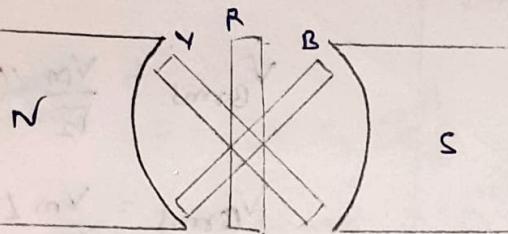
(i) Cosine of angle of lead or lag

(ii) ratio or $R/Z = \frac{\text{True Power}}{\text{Apparent Power}} = \frac{P}{S}$

$$\boxed{\cos \phi = R/Z = P/S}$$

Three Phase AC Circuit:-

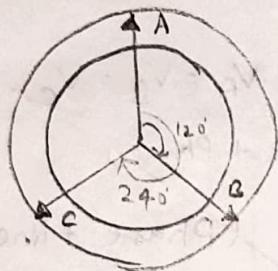
A three phase system consists of three separate but identical windings that are displaced by 120° electrical degrees from each other. When these three windings are rotated in an anticlockwise direction with constant angular velocity in a uniform magnetic field. The emf are induced in each winding which have the same magnitude and displaced 120° from one another.



$$e_R = E_m \sin \omega t$$

$$e_B = E_m \sin(\omega t - 120^\circ)$$

$$e_Y = E_m \sin(\omega t - 240^\circ)$$



* Phase Sequence The sequence in which the voltage in three phase reach maximum positive value is called the phase sequence or phase order.

$$\text{Ex } RYB \Rightarrow YBR \Rightarrow BRY$$

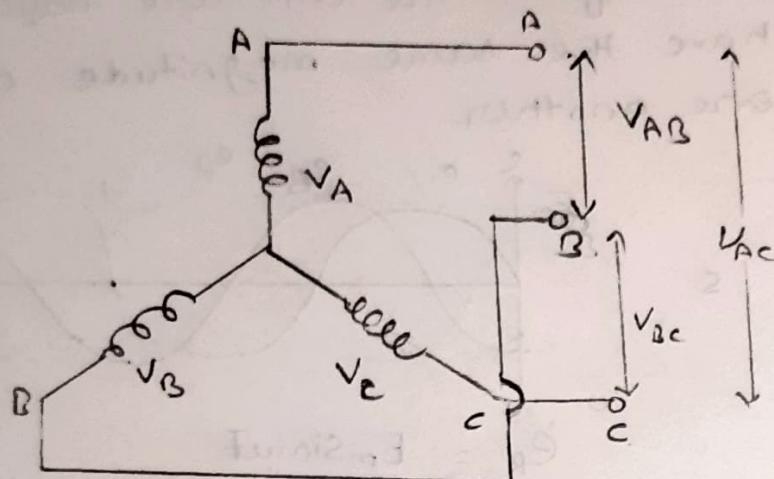
* Phase Voltage :- The voltage induced in each winding is called the phase voltage.

* Phase current :- The current flowing through each winding is called the phase current.

* Line Voltage :- The voltage available between any pair of terminal or lines is called the line voltage.

* Line current :- The current flowing through each line is called the line current.

Voltage Current Relation in Star Connection :-



$$V_{A\text{rms}} = \frac{V_m}{\sqrt{2}}$$

$$V_{B\text{rms}} = \frac{V_m \angle (-120^\circ)}{\sqrt{2}}$$

$$V_{C\text{rms}} = \frac{V_m \angle (-240^\circ)}{\sqrt{2}}$$

~~Phase Voltage are $V_A = V_B = V_C$
(Phase + Phase)~~

~~$V_{AB}, V_{BC}, V_{CA} \Rightarrow$ Line Voltage (Phase + line)~~

~~$(V_A - V_B), (V_B - V_C), (V_C - V_A)$~~

~~[$V \rightarrow (+)$]~~

$$V_{AB} = V_A - V_B$$

$$(V_{AB})^2 = (V_A - V_B)^2 = V_A^2 + V_B^2 + 2VAV_B \cos\phi$$

~~$V_{AB} = V_{BC} = V_{CA} = V_L$~~

~~$V_A = V_B = V_C = V_p$~~

~~$V_L^2 = V_p^2 + V_p^2 + 2V_p^2 \cos\phi$~~

~~$\phi = 60^\circ$~~

$$V_L^2 = 2V_p^2 (1 + \cos 60^\circ)$$

$$V_L = \sqrt{\frac{2V_p^2 \times \sqrt{3}}{2}}$$

$$\boxed{V_L = \sqrt{3} V_p}$$

Phase current...

$$I_{AB} = I_{BC} = I_{CA} = I_{Ph}$$

Line current

$$I_A = I_B = I_C = I_L$$

$$\boxed{I_L = I_{Ph}}$$

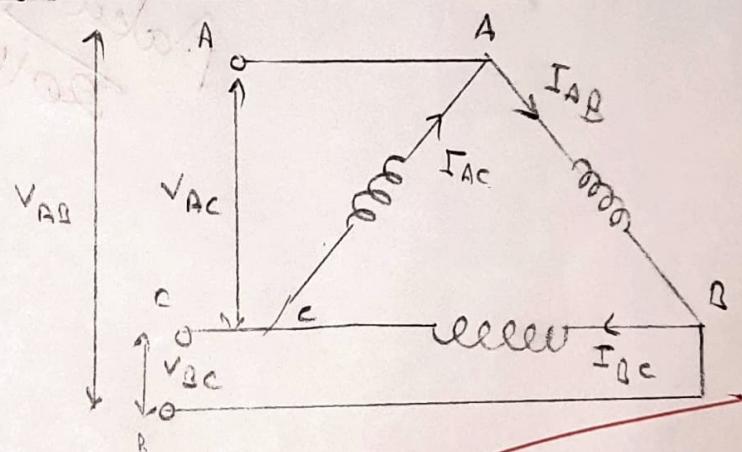
Power

$$P = \sqrt{3} V_L I_L \cos \phi$$

$$\text{Reactive power} \Rightarrow Q = \sqrt{3} V_L I_L \sin \phi$$

$$\text{Apparent power} \Rightarrow S = \sqrt{3} V_L I_L$$

Voltage Current Relation between in Delta Connection.



$$I_{AB} = I_{BC} = I_{CA} = I_{Ph} = \text{(Phase current RMS value)}$$

$$I_{AB} = I_{Ph}$$

line Current (KCL)

$$I_{BC} = I_{Ph} L - 120^\circ$$

$$I_A = I_{AB} - I_{AC}$$

$$I_{CA} = I_{Ph} L - 240^\circ$$

$$I_B = I_{AC} - I_{BC} < 120^\circ$$

$$I_C = I_{BC} - I_{Ph} (\cos 120^\circ + j \sin 120^\circ)$$

$$I_B = I_{Ph} (1 - (-\frac{1}{2}) + j \frac{\sqrt{3}}{2})$$

$$I_B = \frac{V_{ph}}{\sqrt{3}} = (\frac{3}{2} - j\frac{3}{2}) I_{ph}$$

$$I_B = V_{ph}(\sqrt{3}) (\frac{3}{2} - j\frac{3}{2})$$

$$I_B = \sqrt{3} I_{ph} < -30^\circ \quad \cos 30^\circ = \frac{\sqrt{3}}{2}$$

$\therefore I_A = \sqrt{3} I_{ph} < -150^\circ$

$$I_C = \sqrt{3} I_{ph} < -270^\circ$$

Power
Total Power

$$P = \sqrt{3} V_{ph} I_{ph} \cos \phi$$

~~Reactive Power~~

$$Q = \sqrt{3} V_{ph} I_{ph} \sin \phi$$

Apparent power

$$S = \sqrt{3} V_{ph} I_{ph}$$

