

* Wave Optics (Basic) *

● Newton's corpuscular theory :- (2 or 4 marks)

1. Newton proposed that a light source emits tiny particle. These particle (rigid, elastic & massless) known as **corpuscular**. (Ansforst)
2. These particle travel through a transparent medium at very high speed (3×10^8 m/sec) in all directions along a straight line.
3. When these particle enter in our eyes produce a sensation or vision.
4. Due to different size of the particle they produce different types of colours.
5. These light particles repelled by reflective surfaces and attracted by transparent surface.

● Advantage of Newton's corpuscular Theory :-

1. Newton's theory explains reflection & refraction phenomena separately.
2. It explain the Rectilinear propagation of light.

● Disadvantage of Newton's theory :-

1. Newton's theory fails to explain the phenomena of Interference, Diffraction and polarisation of light.
2. He couldn't explain the concept of partial reflection & partial refraction.
3. According to this theory velocity of light particle is larger in denser medium comparative to rarer medium. (This is practically wrong.)

• Wave optics :- Wave optics is a disturbance of light which have wavelength, frequencies, optm amplitude, phase and phase-difference.

• Wave Front :-

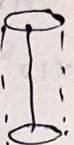
(तरंगांश) wave front is locus of all the points which are vibrating in same phase.

• (i) Point Source



spherical

(ii) Line-Source



Cylindrical

(iii) At infinite



Plane
wave front

* Coherent Sources :- (कलासम्बद्ध)

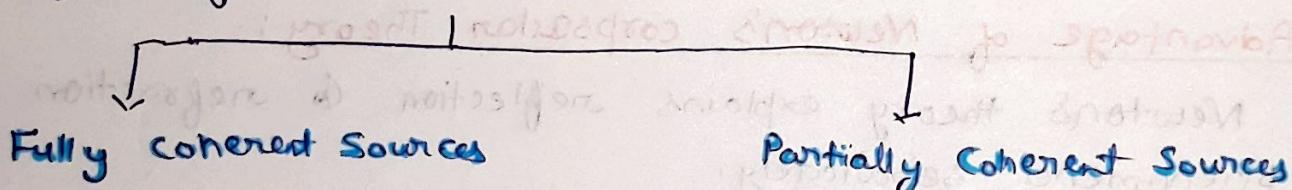
(i) Same wavelength

(ii) Same frequency

(iii) Same phase or same phase diff.

(iv) Same amplitude

Types of coherent sources



Ex. Laser

Ex. Sunlight and all natural sources.

Wave

Mechanical
wave
(in medium)

Electro-magnetic wave
(without medium)

Longitudinal wave
(water wave,

Transverse

Transverse wave

(Sound wave,

* Interference:-

(light waves)

When two coherent sources propagating in same direction superimpose each other then re-distribution of light intensity is called "interference".

There are two types of interference -

(i) **Constructive Interference
(Maxima)**

(ii) **Destructive Interference
(Minima)**

After interference of two light source we get maximum intensity then it is called constructive interference.

After interference of two light source we get minimum intensity then it is called destructive interference.

Q 1 While two independent sources can not be coherent source? (Mark - 2)

Ans Because they do not emit same wave. and not have same phase or constant phase difference between them.

* Production method of interference :-

(i) By devision of wave front.

Ex. ✓ Young's double slit experiment

(ii) Lloyd's mirror method

(iii) Fresnel's prism method

(ii) By devision of amplitude.

Ex.

(i) Thin film interference

✓ (ii) Newton's Rings

(iii) Wedge shape interference

**

Q 2 What are the condition for sustained interference?

(i) The Amplitude of both waves should be same.

(ii) frequencies should be same, wavelength, phase/phase difference should be same.

(iii) Point sources should be narrow. (Right)

(iv) The distance between both sources should be minimum

(Marks - 4, 2)

Thomas Young's Double Slit experiment

- Mathematical Analysis of Young's double slit exp.

Displacement equation for any general wave:-

$$y = a \sin(\omega t + \delta)$$

whereas

y = displacement ω = angular frequency

a = amplitude δ = Phase diff.

Let us assume

$$y_1 = A_1 \sin \omega t \quad \text{— is 1st wave}$$

$$y_2 = A_2 \sin(\omega t + \delta) \quad \text{2nd wave}$$

from the superimposition principle-

$$y = y_1 + y_2$$

$$y = A_1 \sin \omega t + A_2 \sin(\omega t + \delta)$$

$$y = A_1 \sin \omega t + A_2 \sin \omega t \cos \delta + A_2 \sin \delta \cos \omega t$$

$$y = (A_1 + A_2 \cos \delta) \sin \omega t + A_2 \sin \delta \cos \omega t$$

$$\text{let } A_1 + A_2 \cos \delta = A \cos \theta \quad \text{— iiii}$$

$$A_2 \sin \delta = A \sin \theta \quad \text{— iv} \quad \text{where as}$$

$$y = A \cos \theta \sin \omega t + A \sin \theta \cos \omega t$$

A = new amplitude

$$y = A \sin(\omega t + \theta) \quad \text{— v}$$

By squaring eq. iv & v and adding

$$A_1^2 + A_2^2 \cos^2 \delta + 2A_1 A_2 \cos \delta + A_2^2 \sin^2 \delta = A^2 \cos^2 \theta + A^2 \sin^2 \theta$$

$$A_1^2 + A_2^2 + 2A_1 A_2 \cos \delta = A^2$$

$$A = \sqrt{A_1^2 + A_2^2 + 2A_1 A_2 \cos \delta}$$

\rightarrow v

Redistributing Resultant Intensity

$$I \propto A^2$$

$$A^2 = a_1^2 + a_2^2 + 2a_1 a_2 \cos \delta$$

$$I_1 \propto a_1^2$$

$$I_2 \propto a_2^2$$

$$\boxed{I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \delta}$$

where as I_1, I_2 are the intensities.

If $a_1 = a_2 = a$

$$I_1 = I_2 = I$$

then eq (v)

$$A = \sqrt{a^2 + a^2 + 2a^2 \cos \delta}$$

$$A = 2a \sqrt{\cos \delta}$$

$$A = \sqrt{2a^2 + 2a^2 \cos \delta}$$

$$A = 2a \cos \frac{\delta}{2}$$

By eq (v)

$$I = I + I + 2I \cos \delta$$

$$I = 2I \cos \delta + 2I$$

$$I = 2I (\cos \delta + 1)$$

$$I = 2I (2 \cos^2 \frac{\delta}{2})$$

$$I = 4I \cos^2 \frac{\delta}{2}$$

Relation between path difference and phase difference

$$\boxed{\Delta \alpha = \frac{\lambda}{2\pi} \Delta \phi}$$

where as

$\Delta \alpha$ = Path diff.

$\Delta \phi$ = Phase diff.

$$\boxed{\Delta \phi = \frac{2\pi}{\lambda} \Delta \alpha}$$

$$I = I_1^2 + a$$

$$I = I_1 + I_2 + 2\sqrt{I_1 I_2} \cos \delta$$

for max intensity

$$\Delta \phi = 2n\pi$$

$$\Delta \alpha = \frac{\lambda}{2\pi} \times 2n\pi$$

$\Delta \alpha = n\lambda/2$ (even mult. of half of wavelength)

for min intensity

$$\Delta \phi = (2n+1)\pi \text{ or } (2n-1)\pi$$

$$\Delta \alpha = \frac{\lambda}{2\pi} (2n-1)\pi$$

$$\Delta \alpha = \frac{\lambda}{2} (2n-1)$$

(odd mult. of half of λ)

Comparison of Intensities at maxima & minima

$$I \propto a^2$$

$$I_1 = k a_1^2$$

$$I_2 = k a_2^2$$

Then

$$\frac{I_1}{I_2} = \frac{a_1^2}{a_2^2}$$

$$\boxed{\frac{a_1}{a_2} = \sqrt{\frac{I_1}{I_2}}}$$

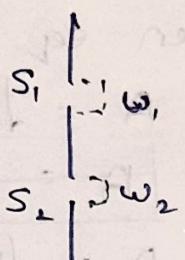
$$\frac{I_{\max}}{I_{\min}} = \frac{(a_1 + a_2)^2}{(a_1 - a_2)^2}$$

$$\frac{I_{\max}}{I_{\min}} = \frac{\left(\frac{a_1}{a_2} + 1\right)^2}{\left(\frac{a_1}{a_2} - 1\right)^2}$$

$$\text{if } \gamma = \frac{a_1}{a_2}$$

$$\boxed{\frac{I_{\max}}{I_{\min}} = \frac{(\gamma + 1)^2}{(\gamma - 1)^2}}$$

$$\boxed{\frac{w_1}{w_2} = \frac{a_1^2}{a_2^2} = \frac{I_1}{I_2}}$$



where w_1 = width of Slit of 1

w_2 = width of Slit 2

Numerical

Q Two coherent sources have intensities in the ratio of $\frac{25}{16}$, find the ratio of maxima to minima intensities after interference of light

$$\frac{I_1}{I_2} = \frac{25}{16}$$

$$\frac{a_1}{a_2} = \frac{5}{4}$$

$$\frac{I_{\max}}{I_{\min}} = \frac{\left(\frac{5}{4} + 1\right)^2}{\left(\frac{5}{4} - 1\right)^2}$$

$$\boxed{\frac{I_{\max}}{I_{\min}} = \frac{81}{1}}$$

Ans

Q The ratio of the intensities minima to maxima in the Young's double slit experiment is 9:25. find the ratio of the width of the two slits.

$$\therefore \frac{I_{\max}}{I_{\min}} = \frac{25}{9} = \frac{(r+1)^2}{(r-1)^2}$$

$$\boxed{r=4}$$

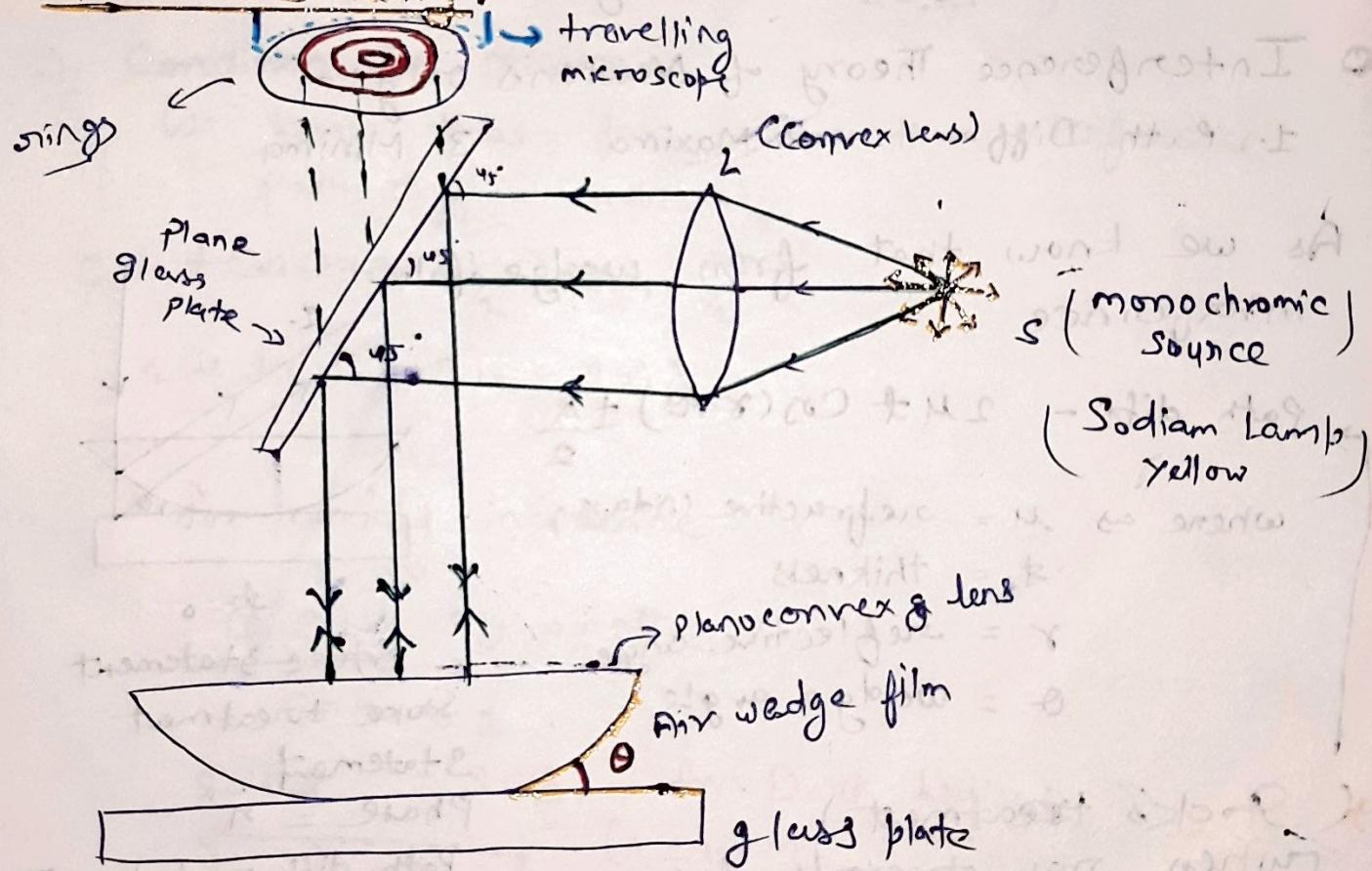
$$r = \frac{a_1}{a_2} = \frac{4}{1}$$

$$\frac{I_1}{I_2} = \frac{a_1^2}{a_2^2} = \frac{16}{1}$$

then width

$$\frac{w_1}{w_2} = \frac{I_2}{I_1} = \frac{1}{16}$$

* Newton's Ring :-



- When a planoconvex lens of Large Focal Length is placed on a plane glass plate with its convex surface in contact with Glass plate.

2. An air film of very small thickness is enclosed between the lower surface of planoconvex lens and upper surface of the glass plate, that is called "Air wedge Film."
3. When a beam of light from a monochromatic source is made to fall normally on the combination of plano convex lens at plane glass-plate.
4. Concentric rings are observed of alternating dark & bright with the center at the point where the lens and plate meet. these rings observed by a travelling microscope.

○ Interference Theory of Newton's ring:-

1. Path Diff. 2. Maxima 3. Minima

As we know that from wedge film interference.

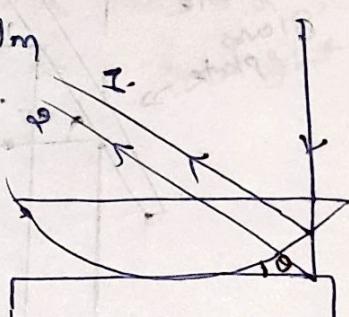
$$\text{path diff} = 2t \cos(\gamma + \theta) + \frac{\lambda}{2}$$

where ω μ = refractive index

t = thickness

γ = reflective angle

θ = wedge angle,



~~Stock's statement~~

~~Stock's treatment~~

~~Statement~~

~~Phase = π~~

~~Path diff = $\pm \lambda/2$~~

(Stock's treatment)

[when ray travels from

rarer to denser medium]

1. Condition for maxima :-

We know that for constructive interference

$$\text{Path diff} = \text{even} \times \frac{\lambda}{2}$$

$$2\mu t \cos(\gamma + \theta) + \frac{\lambda}{2} = 2n \times \frac{\lambda}{2}$$

$$2\mu t \cos(\gamma + \theta) = (2n - 1)\frac{\lambda}{2}$$

for normal incidence -

$$\theta = \gamma = 0$$

$$\theta \approx \text{very small} (\theta \rightarrow 0)$$
$$\cos \theta \rightarrow 1$$

$$2\mu t = (2n - 1)\frac{\lambda}{2} \quad \text{for bright fringes}$$
$$(n = 1, 2, 3, \dots)$$

2. Condition for minima :-

We know that for Destructive interference

$$\text{Path diff} = \text{odd} \times \frac{\lambda}{2}$$

$$2\mu t \cos(\gamma + \theta) + \frac{\lambda}{2} = (2n + 1)\frac{\lambda}{2}$$

$$2\mu t \cos(\gamma + \theta) = 2n\frac{\lambda}{2}$$

for normal incidence

$$\gamma = 0$$

$$\theta \text{ is very small}$$

$$\theta \rightarrow 0$$

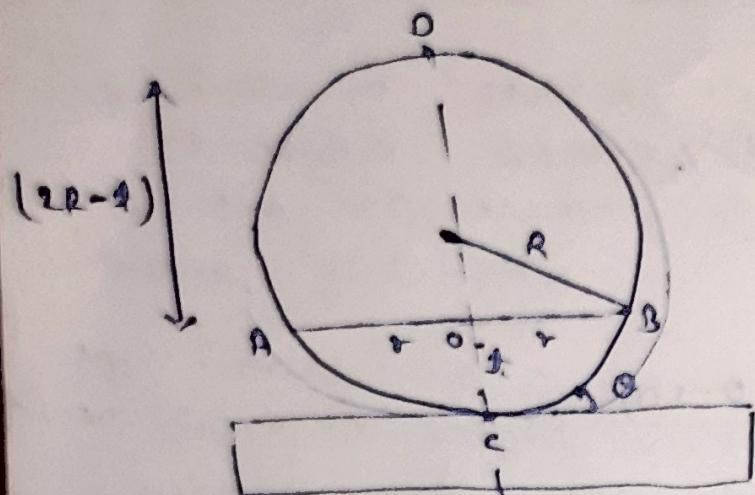
$$\cos \theta \rightarrow 1$$

$$2\mu t = 2n\left(\frac{\lambda}{2}\right) \quad \text{for Dark fringes}$$

$$\boxed{2\mu t = n\lambda} \quad (n = 1, 2, 3, \dots)$$

* Diameter of Newton's ring :-

Bright ring Dark ring



$t \rightarrow$ thickness C = Contact point.

R = Radius of curvature.

from the property of Circle (theorem)

$$OD \times OC = OA \times OB \quad (\text{diagonal of } \triangle OAB)$$

$$(2R-t) \times t = R \cdot R$$

$$t = \frac{R^2}{2R-t} \quad 2R \ggg t \quad t \rightarrow 0$$

$$t = \frac{R^2}{2R} \quad \text{--- (i)}$$

(i) Diameter of Bright ring -

we know that path diff. = even $\times \frac{\lambda}{2}$

$$2kt \cos(\theta + \phi) + \frac{\lambda}{2} = 2n \cdot \frac{\lambda}{2}$$

for normal incidence

$$2kt = (2n-1) \frac{\lambda}{2}$$

for air $n=1$

$$2st = (2n-1) \frac{\lambda}{2}$$

$$\text{value of } t = \frac{\gamma^2}{2R}$$

$$2 \cdot \frac{\gamma^2}{2R} = (2n-1) \frac{\lambda}{2}$$

$$\frac{\gamma^2}{R} = (2n-1) \frac{\lambda}{2}$$

$$\boxed{\gamma^2 = (2n-1) R \frac{\lambda}{2}}$$

$$\therefore \frac{D_n}{2} = \gamma$$

$$\left(\frac{D_n}{2}\right)^2 = (2n-1) \frac{R\lambda}{2}$$

$$D_n^2 = 4(2n-1) R \lambda$$

$$\boxed{D_n^2 = 2(2n-1) R \lambda}$$

(ii) Diameter of Dark rings

we know that Path diff = odd $\times \frac{\lambda}{2}$

$$\Delta n = (2n+1) \frac{\lambda}{2}$$

$$2Mt \cos(r+\theta) + \frac{\lambda}{2} = (2n+1) \frac{\lambda}{2}$$

$$2Mt \cos(r+\theta) = 2n\lambda$$

$$2Mt = 2n\lambda$$

for air $M=1$

$$t = n\lambda$$

$$\therefore t = \frac{\gamma^2}{2R}$$

$$2 \times \frac{\gamma^2}{2R} = n\lambda$$

$$\boxed{\gamma^2 = 2n R \lambda}$$

$$\therefore \frac{D_n}{2} = r$$

$$\left(\frac{D_n}{2}\right)^2 = 4\pi R\lambda$$

$$D_n^2 = 4\pi R\lambda$$

$$D_n = \sqrt{4\pi R\lambda}$$

for Dark ring. ($D_n \propto \sqrt{n}$)



Note

1. Diameter for bright rings are proportional to square root of odd natural number.

$$D_n \propto \sqrt{(2n-1)}$$

2. The separation between successive bright rings are in ratio.

3. In dark rings diameter if $n=0$

$$D_0 = \sqrt{4\pi R\lambda}$$

$$D_0 = 0$$

* So center rings of Newton's rings is dark.

4.

- Q Newton's rings are observed in Reflecting light of wavelength 5900 Å . Diameter of the 10th dark ring is 0.50 cm . Find the radius of curvature of the lens.

$$D_n = \sqrt{4\pi R\lambda}$$

$$(0.50) = \sqrt{4 \times 10 \times R \cdot 5900 \times 10^{-8}}$$

$$(0.50)^2 = 40 \times 5900 \times 10^{-8} \times R$$

$$25 \times 10^{-2} = 59 \times 4 \times 10^{-5} \times R$$

$$\frac{25 \times 10^{-2}}{59 \times 4} = R \Rightarrow R = 1.053 \text{ m}$$

$$R = 1053 \text{ cm}$$

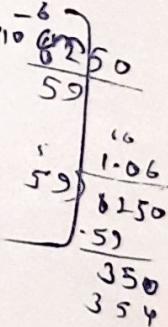
Given

$$\lambda = 5900 \text{ Å} = 59 \times 10^{-6} \text{ cm}$$

$$D_{10} = 0.50 \text{ cm}$$

$$n = 10$$

$$R = ?$$



Q In a newton's ring experiment, the diameter of the 10th dark ring changes from 1.4 cm to 1.27 cm when a liquid is introduced between the lens and the plate. calculate the Refractive index of the liquid.

Given

$$n = 1.0$$

$$\therefore D = \sqrt{\frac{4RN\lambda}{\mu}}$$

R $D_0 = 1.4$ cm

$D_{10} = 1.27$ cm

$$D_n \propto \frac{1}{(\mu)^{1/2}}$$

$$\begin{array}{r} 1.102 \\ 127 \sqrt{1.102} \\ \hline 130 \\ -127 \\ \hline 300 \end{array}$$

$$\frac{D_0}{D_{10}} = \frac{(\mu)^{1/2}}{1}$$

$$\frac{1.4}{1.27} = \frac{(\mu)^{1/2}}{1}$$

$$\sqrt{\mu} = 1.102$$

$$\boxed{\mu = 1.215} \text{ Ans}$$

Q In newton's ring experiment, Diameter of 5th ring (dark) was 0.336 cm. Find the radius of curvature of the planoconvex lens, if the wavelength of light used is 5800 Å also find out the Radius of 15th dark ring. ($\mu = 1$)

Given

$$D_5 = 0.336 \text{ cm.}$$

$$R = ?$$

$$\lambda = 5800 \text{ Å}$$

$$D_n = \sqrt{\frac{4RN\lambda}{\mu}}$$

$$(0.336)^2 = \frac{n=5}{4 \times R \times 5 \times 5800 \times 10^{-5}}$$

$$\mu = 1$$

$$0.113 = 116 \times 10^{-5} \times R$$

$$D_{15} \rightarrow ?$$

$$R = \frac{0.113 \times 10^5}{116}$$

$$R = 973 \text{ cm}$$

$$D_{15} = \sqrt{\frac{15 R \lambda \times 4}{M}}$$

$$\gamma_{15} = \sqrt{R \lambda \times 15}$$

$$\gamma_{15} = \sqrt{97.3 \times 5800 \times 10^{-8}} \times 15$$

$$\gamma_{15} = 0.29 \text{ cm}$$

05/09/24

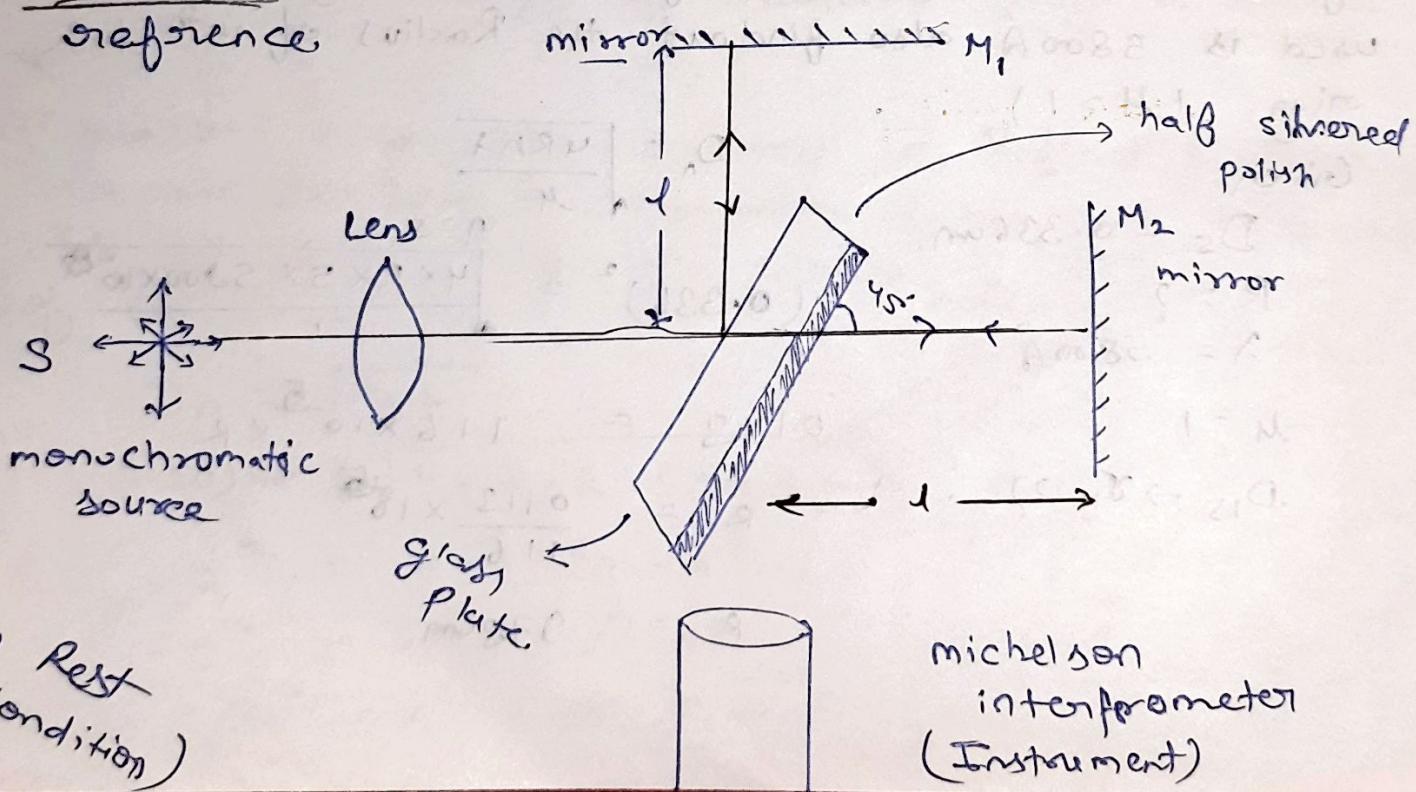
Michelson moreley experiment :-

Object to measure relative motion between earth & ether. to verify the presence of ether medium.

Q What is ether medium. (2)

A Ether is a hypothetical medium. It is used to explain how light waves reach us from the Sun, through the free space.

3. Ether is considered ^{as a} transparent medium, highly elastic which provides a fixed frame of reference



in Rest
(Condition)
michelson
interferometer
(Instrument)

Same - Same molecule
↳ cohesive force
(संरक्षण)

Diffr. molecule
Adhesive force
(असंगत)

Principle

(a)

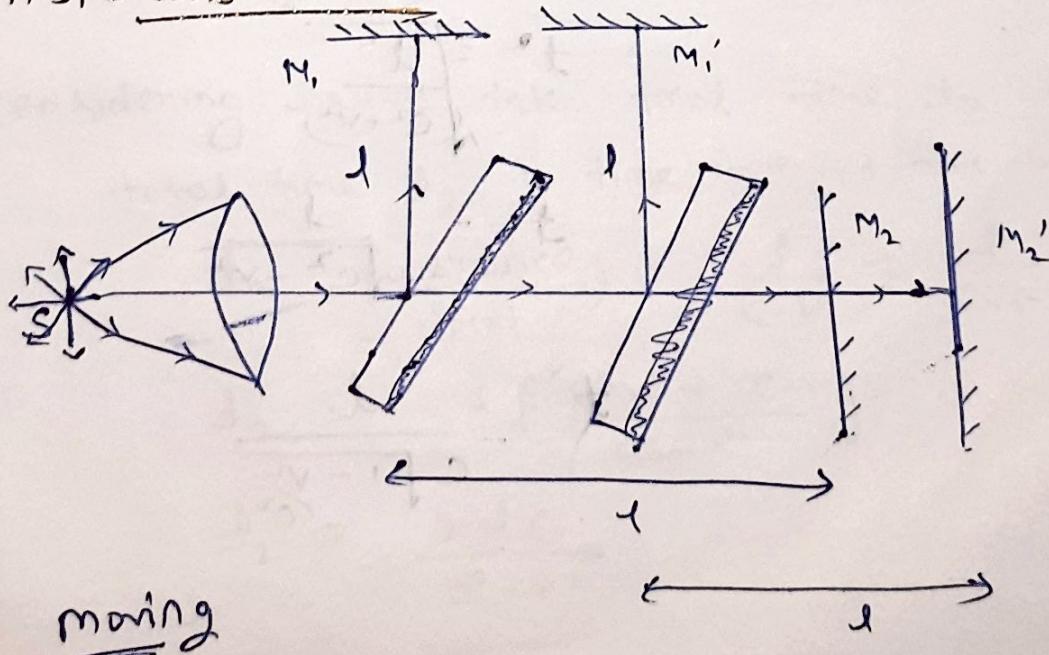
What is the principle of michelson interferometer?

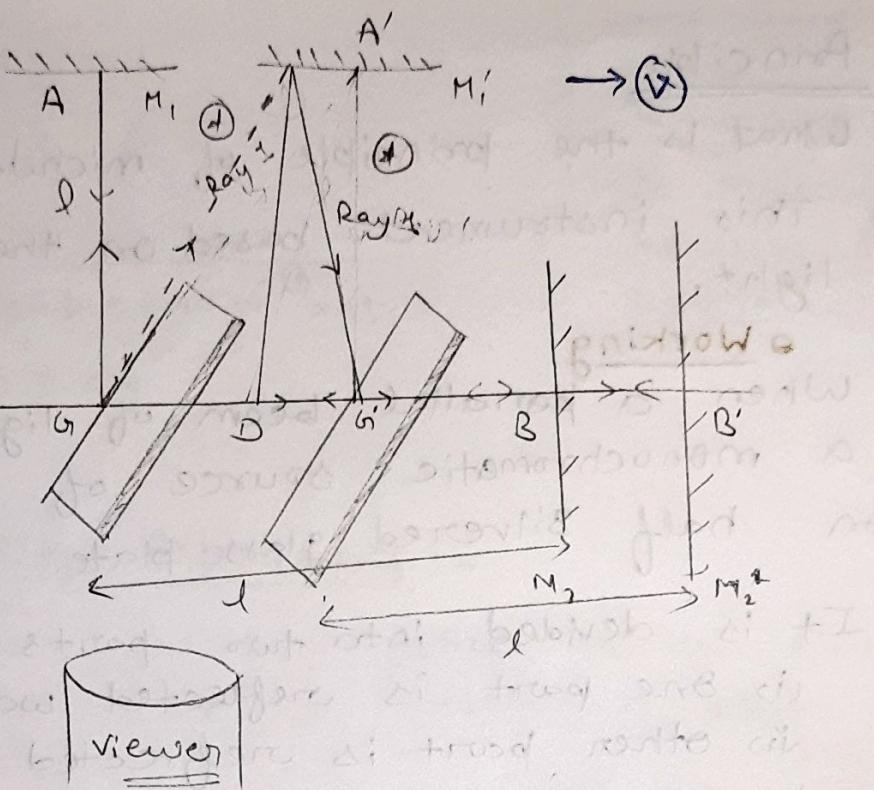
Ans This instrument based on the interference of light.

Working

- When a parallel beam of light coming from a monochromatic source of light is incident on half silvered glass plate.
- It is divided into two parts
 - one part is reflected wave and
 - other part is refracted wave.
 and both are coherent waves.
- In this, experiment interference produced by the method of division of amplitude.
- These waves ~~proceeds~~ proceeds in perpendicular direction and incidents normally on the mirror.
- After reflection on the mirror when they superimpose, produce an interference.

Const • Construction





Analysis for Ray 1

't' → let us time taken by Ray 1 to travel path $GA'G'$

$$\text{Total time} \Rightarrow t_1 = t + t'$$

$$t_1 = 2t$$

in right angled $\triangle GAD$

$$(ct)^2 = l^2 + v t^2$$

$$l^2 = (c^2 - v^2) t^2$$

$$t^2 = \frac{l^2}{c^2 - v^2}$$

$$t = \frac{l}{\sqrt{c^2 - v^2}}$$

$$t = \frac{l}{c \sqrt{1 - \frac{v^2}{c^2}}}$$

$$t = \frac{l}{c} \left(1 - \frac{v^2}{c^2}\right)^{-\frac{1}{2}}$$

$$(1+n)^n = 1+nv \dots$$

$$\left(1 - \frac{v^2}{c^2}\right)^{-\frac{1}{2}} = 1 - \frac{v^2}{c^2} \times \left(-\frac{1}{2}\right) = \left(1 + \frac{v^2}{2c^2}\right)$$

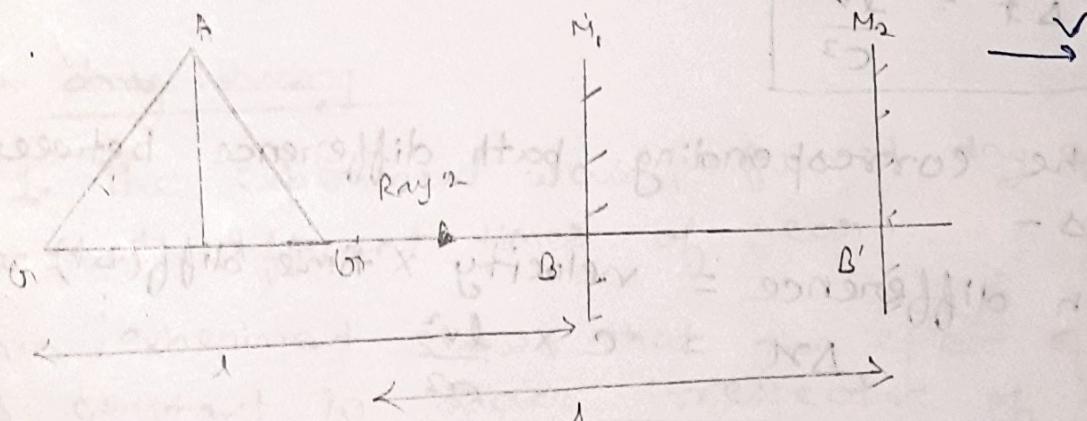
$$t = \frac{l}{c} \left(1 + \frac{v^2}{2c^2}\right)$$

So for Ray 1

$$t_1 = 2t$$

$$t_1 = \frac{2l}{c} \left(1 + \frac{v^2}{2c^2}\right)$$

Analysis for Ray 2



Considering Ray-2 take total time t_2 :

total time t_2 = time G to B + time B' to G'

$$t_2 = \frac{\text{(distance)}}{\text{Speed}} = \frac{l}{c+v} + \frac{l}{c-(-v)}$$

$$t_2 = l \left[\frac{c+v + c-v}{c^2 - v^2} \right]$$

$$t_2 = \frac{2lc}{c^2 - v^2}$$

$$t_1 = \frac{2l}{c} \frac{c}{(1 - v/c)}$$

$$t_2 = \frac{2l}{c} \left(1 - \frac{v^2}{c^2}\right)^{-1} \text{ By using binomial.}$$

$$t_2 = \frac{2l}{c} \left(1 + \frac{v^2}{c^2}\right)$$

→ time difference

$$\Delta t = t_2 - t_1$$

$$\Delta t = \frac{2l}{c} \left(1 + \frac{v^2}{c^2}\right) - \frac{2l}{c} \left(1 + \frac{v^2}{2c^2}\right)$$

$$\Rightarrow \Delta t = \cancel{\frac{2l}{c}} + \frac{2lv^2}{c^3} - \cancel{\frac{2l}{c}} - \frac{2lv^2}{2 \cdot c^3}$$

$$\Delta t = \frac{2lv^2 - lv^2}{c^3}$$

$$\boxed{\Delta t = \frac{lv^2}{c^3}}$$

* Now the corresponding path difference between two rays -

Path difference = velocity × time diff (Δt)

$$\Delta x = c \times \frac{lv^2}{c^3}$$

$$\boxed{\Delta x = \frac{lv^2}{c^2}}$$

After the michelson turn their approach apparatus by 90°

Path difference $\boxed{\Delta x' = -\frac{lv^2}{c^2}}$

Hence Resultant path difference

$$\Delta x'' = \frac{lv^2}{c^2} - \left(-\frac{lv^2}{c^2}\right)$$

$$\boxed{\Delta x'' = \frac{2lv^2}{c^2}}$$

If the wavelength of incident light is λ then
fringe shift (n)

$$n = \frac{\Delta x''}{\lambda} = \frac{2lv^2}{\lambda c^2}$$

Fringe shift [n or N]

$$N = \frac{2l}{\lambda} \left(\frac{v^2}{c^2}\right)$$

$$\left[\because l = 11m, \lambda = 5500\text{Å}, v = 10^{-4} \text{ m/s} \right]$$

$$\boxed{N = 0.4}$$

* Ether drag theory

Note 1. The experiment was performed day and night and at different times of year.

2. This experiment shows that the speed of light is constant in space irrespective of the direction and speed of the initial frame.
3. So, it was concluded by Michelson that there is no medium like ether.

Types of fringes

• Fringes observation in Michelson - Morley exp.

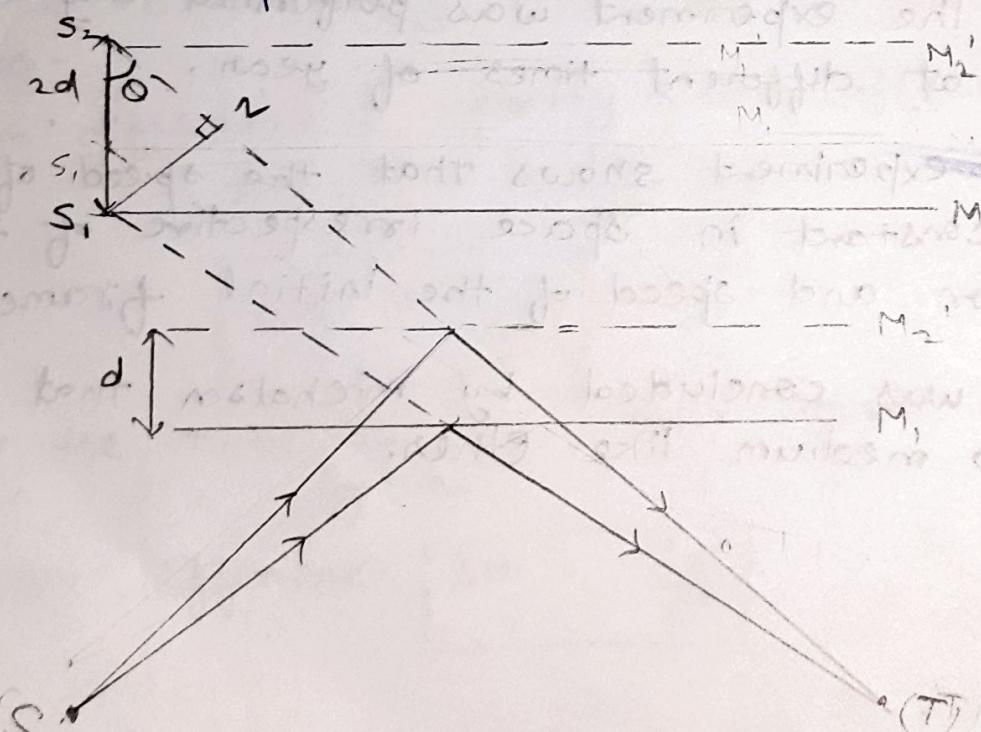
Types of observed frings

(i) Circular Frings

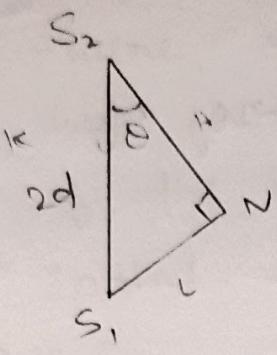
(ii) Localized frings.

(i) Circular Frings:-

- When mirror M_1 is seen directly through telescope (T) in addition to it virtual image of mirror M'_2 of mirror M_2 is formed by reflection in Plate G_1 , is also seen.
- This forms system equivalent to air film enclosed between two mirror between M_1 & M'_2 .
- These two intersecting beams appear to come from virtual source S_1 & S_2 directed from single source 'S'. Separation between them is 'd'.



* when m_1 & m_2 both are perpendicular to each other. (m_1 & m_2' Parallel.)



in $\Delta S_1 N S_2$

$S_2 N = 2d \cos \theta =$ Path difference between two intersecting beams.

effective Path diff = $2d \cos \theta - \frac{\lambda}{2}$

for Bright fringe

$$\Delta x = n\lambda$$

$$2d \cos \theta - \frac{\lambda}{2} = n\lambda$$

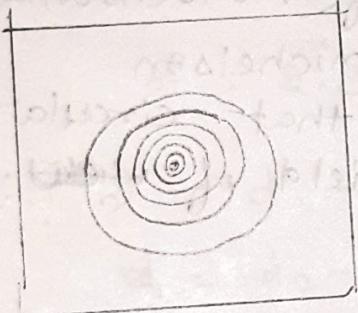
$$2d \cos \theta = (2n+1) \frac{\lambda}{2}$$

for dark fringe

$$\Delta x = (2n-1) \frac{\lambda}{2}$$

$$2d \cos \theta - \frac{\lambda}{2} = (2n-1) \frac{\lambda}{2}$$

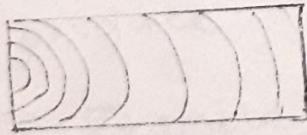
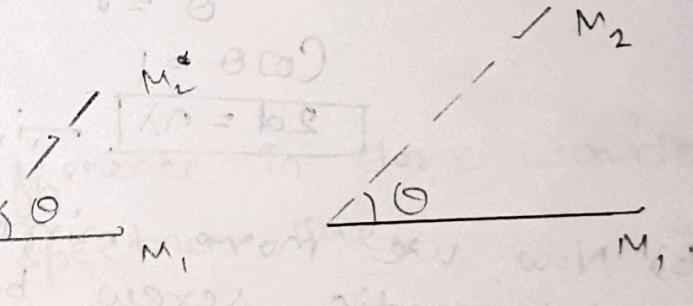
$$2d \cos \theta = n\lambda$$



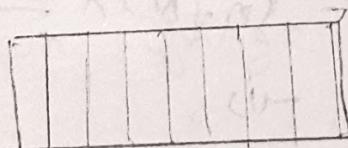
← Circular Fringes

Haidinger fringes

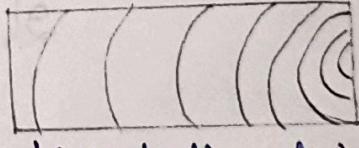
* Local fringe :-



Hyperbolic fringe



Linear fringe



Hypobolic fringe

* Interference pattern is circular, concentric and alternate bright & dark frings.

- * $2d \cos \theta$ is maximum if $\theta = 0$, so maximum order fringe lies at centre.
- * When we move away from centre of pattern $\theta \uparrow \therefore \cos \theta \downarrow$ so $2d \cos \theta \downarrow$
So n is also decreasing.

● Application of Michelson interferometer:-

~~App 1~~ To determine the wavelength of monochromatic source of light -

(a) To determine the wavelength of monochromatic source of light we adjust michelson interferometer in such a way that circular fringes are observed in the field of ~~view~~ view.
assume center is dark

at centre

$$\theta = 0$$

$$[2d \cos \theta = n\lambda]$$

$$\cos \theta = 1$$

$$2d = n\lambda \quad \text{--- i}$$

(b) Now we move mirror M, with the help of monochromatic screw by a small distance α , then N fringes across the field of view,

$$2(d+\alpha) = (n+N)\lambda \quad \text{--- ii}$$

$$\text{eq (ii) } \rightarrow \text{ i}$$

$$2(d+\alpha) - 2d = \alpha \lambda + N\lambda - n\lambda$$

$$2\alpha = N\lambda$$

$$\boxed{\lambda = \frac{2\alpha}{N}}$$

Q In a michelson interferometer when 100 fringe were shifted, the final reading of the screw was found to be 10.735 mm. If the wavelength of the light was 5.92×10^{-5} cm, what was the initial reading of the screw?

Soln

$$\lambda = \frac{2x}{N}$$

$$d_2 = 10.735 \text{ mm}$$

$$\lambda = 5.92 \times 10^{-5} \text{ cm}$$

$$N = 100$$

$$x = \frac{\lambda N}{2}$$

$$x = \frac{5.92 \times 10^{-5} \times 100}{2} \times 10$$

$$x = 2.96 \times 10^{-3} \text{ cm}$$

$$\therefore d_1 = d_2 - d_1 = \Delta d$$

$$d_1 = d_2 - x$$

$$d_1 = 10.735 - 2.96$$

$$d_1 = 7.775 \text{ mm}$$

App 2:

2. Determination of difference in close wavelength or resolution of spectrum line.

(a) When the source of light has two wavelength λ_1 & λ_2 very close to each other produce its own fringe pattern.

(b) Example - Sodium light

$$\lambda_1 = 5890 \text{ \AA}$$

$$\lambda_2 = 5896 \text{ \AA}$$

(c) The position of the mirror M_1 is adjusted at the circular fringes observed the bright & distinct.

(d) In this position bright fringes due to wavelength λ_1 coincide with the frings (bright) of the λ_2

Let in the case the thickness of virtual air film is 'd' and the order of the central fringes due to $\lambda_1 \neq \lambda_2$

$$\alpha = d_2 - d_1$$

$$\lambda_1 - \lambda_2 = \frac{\lambda^2}{2\alpha}$$

$$\left[\lambda = \frac{\lambda_1 + \lambda_2}{2} \right]$$

Q In michelson experiment, the distance moved by the movable mirror between two consecutive position of maximum distinctness is 0.0289 mm. If the mean wavelength of the two components of the sodium light is 5893 Å. Determine the diff. between the wavelength.

$$\lambda = 5893 \text{ \AA}, \quad \therefore \lambda_1 - \lambda_2 = \frac{\lambda^2}{2\alpha}$$

$$\alpha = 0.0289 \text{ mm}$$

$$\lambda_1 - \lambda_2 = \frac{(5893 \times 10^{-7})^2}{2 \times 0.0289}$$

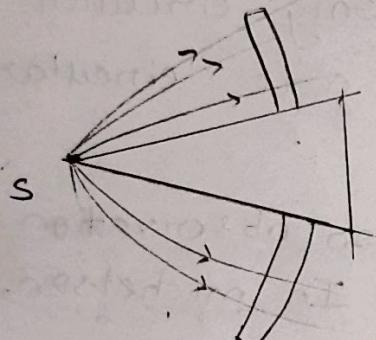
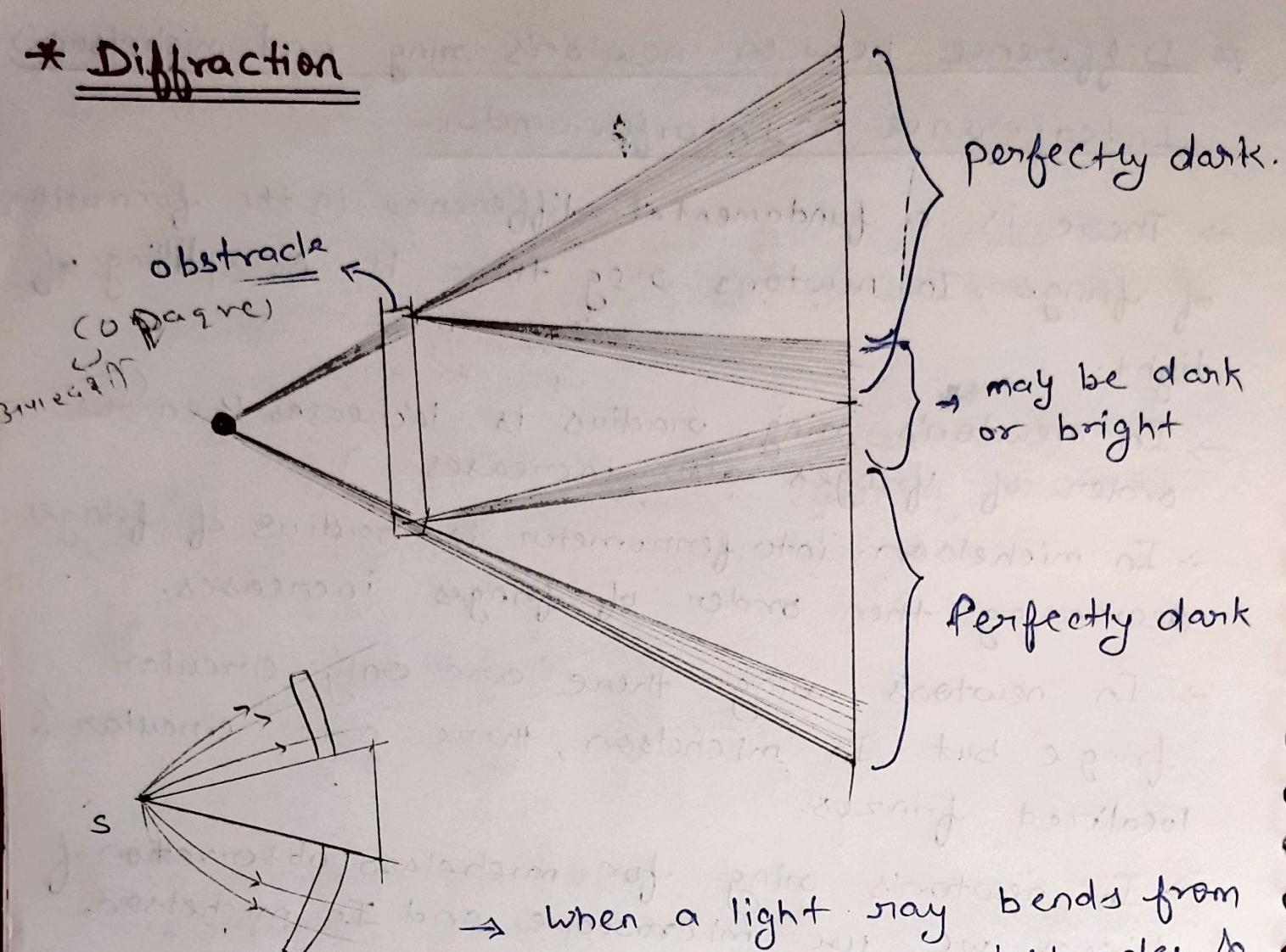
$$\lambda_1 - \lambda_2 = 60082 \times 10^{-10}$$

$$\boxed{\lambda_1 - \lambda_2 = 60082 \text{ \AA}}$$

Difference between newton's ring and michelson's Interference / Interferometer:-

- There is a fundamental difference in the formation of fringes, In newton's ring there is no splitting of light.
- In newton's ring radius is increases then the order of fringes also increases.
- In michelson interferometer is radius of fringes decreasing then order of fringes increases.
- In newton's ring there are only circular fringe but In michelson, there are circular & localized fringes.
- In newton's ring for michelson observation of fringes, we use microscope and In michelson, we use telescope.

* Diffraction

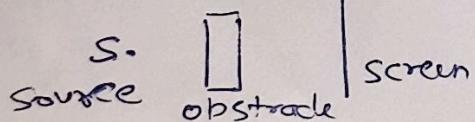


→ When a light ray bends from the sharp edges or corners of an obstacle & move towards the geometrical shadow of any obstacle then this phenomena is known as diffraction.

Diff between Fresnel and Fronhoffer diffraction

Augustine Fresnel

- (i) Source, screen and diffraction device (opaque obstacle) are at finite distance.



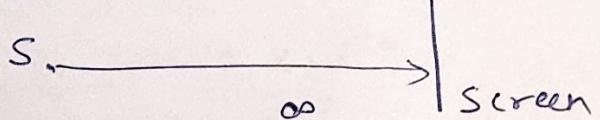
- (ii) No lens and mirror are used

- (iii) Centre may be bright or dark.

Joseph

Fronhoffer

- Source, screen & diffraction device are at infinite distance.



- Lens is used (Convex)

- Centre always bright.

4. wavefront may be spherical or cylindrical.

Wavefront always plane.

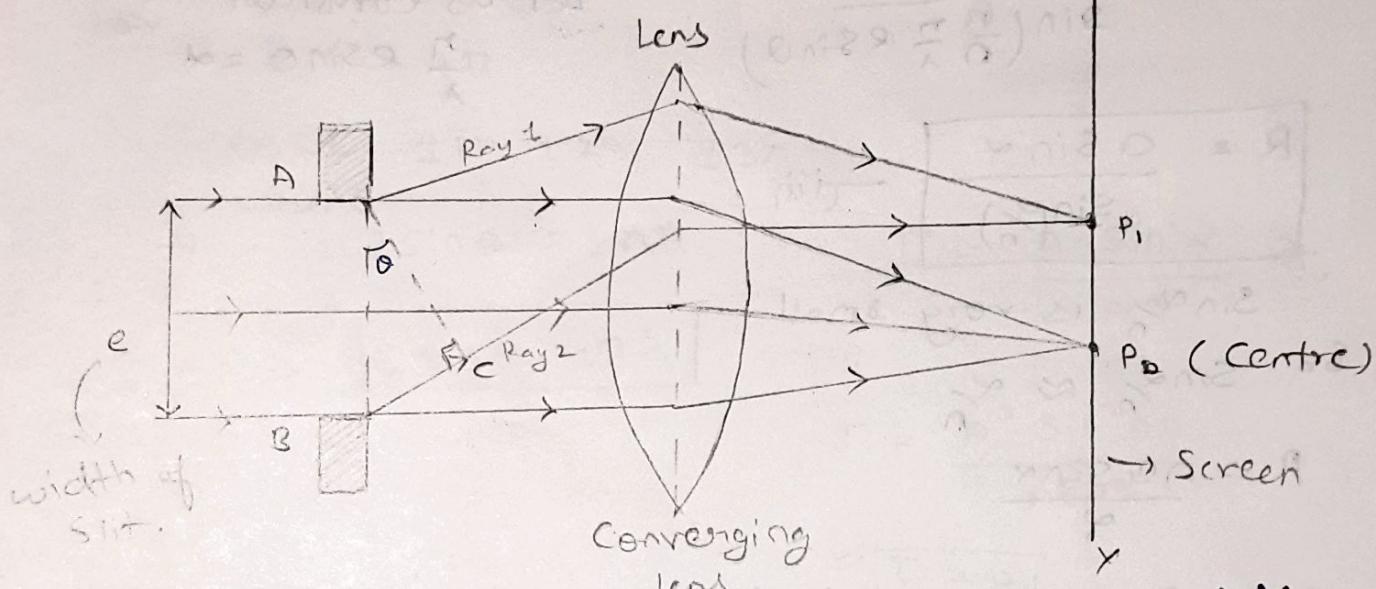
5. Diffraction devices used (obstacles)

Diffraction devices used

(zone plates, circular rings, Nots) (Nots)

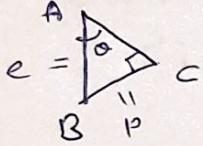
[Single slit, double slit ()]
N slit (Grating)

* Fraunhofer Diffraction due to Single slit :-



in $\triangle ABC$

(ii) Path difference



$$\frac{BC}{AB} = \sin\theta$$

$$\Rightarrow \sin\theta = \frac{BC}{e}$$

$$BC = e \sin\theta$$

$\downarrow \Delta n$ \rightarrow

(iii)

phase difference

$$\Delta\phi = \frac{2\pi}{\lambda} \times \Delta n$$

$$\Delta\phi = \frac{2\pi}{\lambda} \times e \sin\theta$$

Let's consider

there are n points between A & B

then Phase diff.

$$\Delta\phi = \frac{1}{n} \cdot \frac{2\pi}{\lambda} e \sin\theta$$

(iii) from the theory of n harmonic motions-

resultant amplitude is given by

$$R = \frac{\sin n \frac{\delta}{2}}{\sin \frac{\delta}{2}}$$

($\Delta\phi = \delta$)

$$R = \frac{a \sin \frac{n\theta}{2}}{\sin \frac{\theta}{2}} \quad \therefore \delta = \frac{1}{n} e \sin \theta \times \frac{2\pi}{\lambda}$$

$$R = \frac{a \sin \left(n \times \frac{1}{n} e \frac{\sin \theta \times \frac{2\pi}{\lambda}}{2} \right)}{\sin \left(\frac{1}{n} e \sin \theta \times \frac{2\pi}{\lambda} \right) \times \frac{1}{2}}$$

$$R = \frac{a \sin \left(\frac{n}{\lambda} e \sin \theta \right)}{\sin \left(\frac{1}{n} \frac{n}{\lambda} e \sin \theta \right)} \quad \text{Let us consider} \\ \frac{n}{\lambda} e \sin \theta = d$$

$$\boxed{R = \frac{a \sin \alpha}{\sin(\frac{\alpha}{n})}} \quad \text{(iii)}$$

$\sin \frac{\alpha}{n}$ is very small

$$\text{So } \sin \frac{\alpha}{n} \approx \frac{\alpha}{n}$$

$$R = \frac{n a \sin \alpha}{\alpha}$$

$$na = A \quad (\text{new amplitude})$$

$$\boxed{R = \frac{A \sin \alpha}{d} = \frac{\lambda A \sin \left(\frac{n}{\lambda} e \sin \theta \right)}{n e \sin \theta}}$$

(Resultant amplitude)

(iv) Resultant amplitude intensity -

$$\because I \propto R^2$$

$$= I = R^2$$

$$\boxed{I = \frac{A^2 \sin^2 \alpha}{\alpha^2}} \quad \text{(iv)}$$

(5.) Condition for minima :-

For I should be minimum.

$$I = 0$$

for $I = 0$,

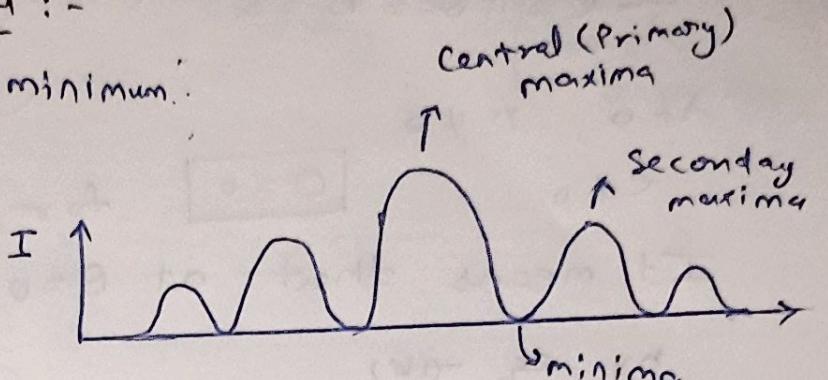
$$A \neq 0$$

for $I = 0$,

$$A \neq 0, \alpha \neq 0$$

$$\text{for } \sin \alpha = \sin n\pi$$

$$\alpha = n\pi$$



(I should not be zero due to A)

Henck $\pm n, \pm 2n, \pm 3n, \dots$

where

$$\alpha = \frac{n\pi \sin \theta}{\lambda} = \pm n\pi$$

$$\boxed{\sin \theta = \pm n\lambda} \rightarrow (V)$$

$$I = \frac{A^2 \sin^2 \alpha}{\alpha^2}$$

$$I = \frac{A^2 \sin^2 n\pi}{n^2 \pi^2}$$

$$\boxed{I = 0}$$

(6.) Condition for central or Primary maxima :-

For central maxima I should be maximum

$$\boxed{I \rightarrow \infty}$$

$$\therefore I = \frac{A^2 \sin^2 \alpha}{\alpha^2} = \infty$$

$$\boxed{\alpha = 0}$$

$$(A \neq 0) \& (\sin \alpha \neq 0)$$

$$\frac{d}{\lambda} r \sin \theta = 0 \quad \leftarrow (\theta = 0)$$

$\lambda \neq 0, r \neq 0$

$r \neq 0$

$$\boxed{\theta = 0}$$

for central maxima.

It means that at $\theta = 0$ we get central maxima.

by eq - (iv)

$$I = \frac{A^2 \sin^2 \alpha}{\alpha^2} \quad \left(\because \lim_{x \rightarrow 0} \frac{\sin x}{x} = 1 \right)$$

$\lambda = 0$ put in this eqn

$$\boxed{I_{\max} = I_0 = A^2} \quad \text{--- (vi)}$$

(*) Condition for secondary maxima:-

$$I = \frac{A^2 \sin^2 \alpha}{\alpha^2}$$

$$\left[\because \frac{d(N/D)}{d\alpha} = \frac{D \cdot \frac{dN}{d\alpha} - N \cdot \frac{dD}{d\alpha}}{D^2} \right]$$

therefore, for maxima

$$\boxed{\frac{dI}{d\alpha} = 0}$$

$$\frac{d}{d\alpha} \left(\frac{A^2 \sin^2 \alpha}{\alpha^2} \right) = \frac{\alpha^2 \cdot A^2 2 \sin \alpha \cos \alpha - A^2 \sin^2 \alpha \cdot 2\alpha}{(\alpha)^4}$$

$$\frac{dI}{d\alpha} = \frac{2\alpha A^2 \sin \alpha (\alpha \cos \alpha - \sin \alpha)}{\alpha^4}$$

$$\frac{dI}{d\alpha} = 0$$

$$\frac{2\alpha A^2 \sin \alpha (\alpha \cos \alpha - \sin \alpha)}{\alpha^4} = 0$$

$\alpha = 0$
central
(maxima)

$$\left. \begin{array}{l} \sin \alpha = 0 \\ (\text{minima}) \end{array} \right\}$$

$$\left. \begin{array}{l} \alpha \cos \alpha - \sin \alpha = 0 \\ \alpha = \tan \alpha \end{array} \right\}$$

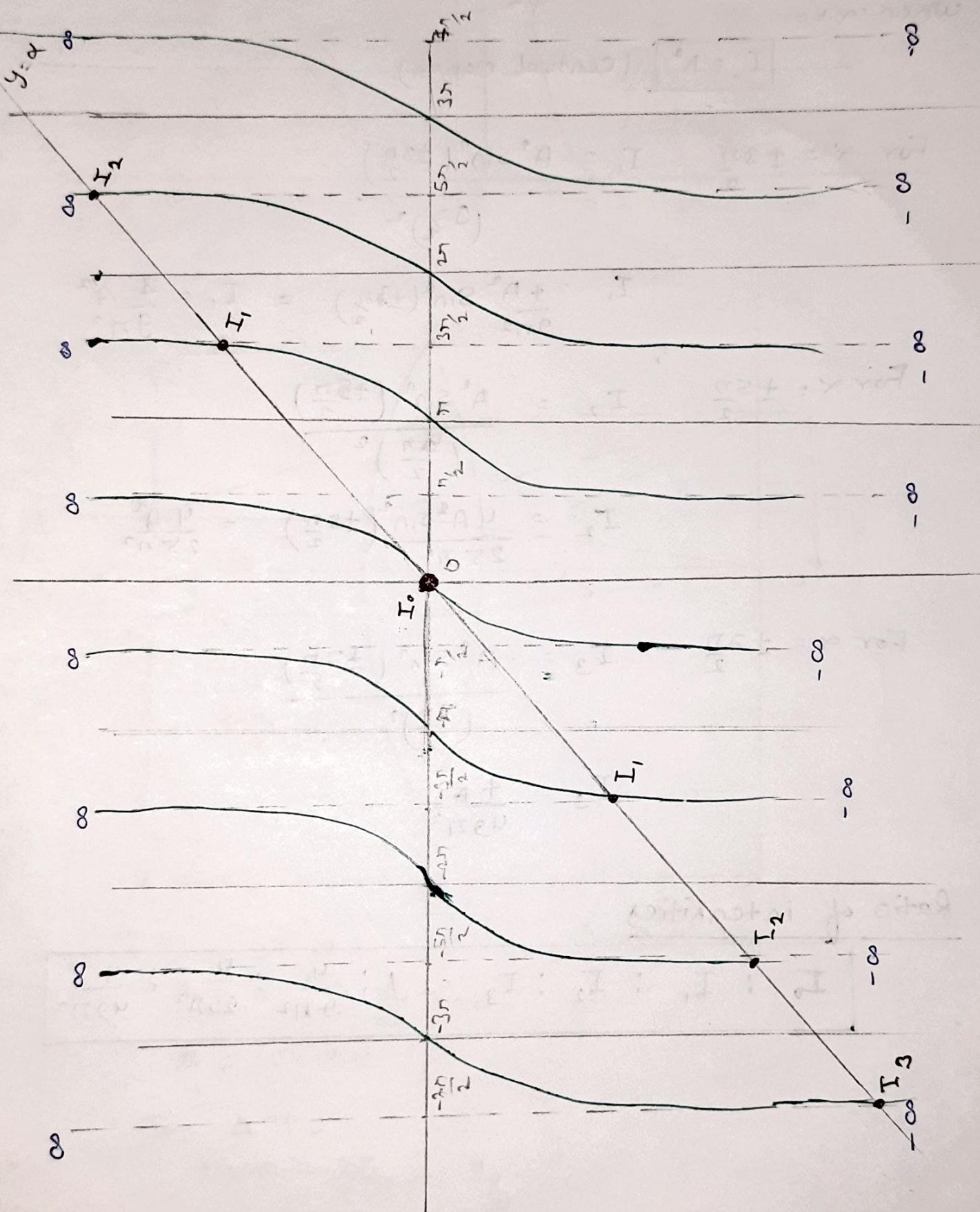
--- (vii)

$y = \alpha$ & $y = \tan \alpha$
will give the position of secondary
maxima.

$$y = m\alpha + c +$$

$$y = 1\alpha + 0$$

$$\begin{aligned} m &= 1 \\ \tan \alpha &= 1 \\ \alpha &= 45^\circ \text{ Slope} \end{aligned}$$



$$\alpha = \pm \frac{3\pi}{2}, \pm \frac{5\pi}{2}, \pm \frac{7\pi}{2}, \pm \frac{9\pi}{2}, \pm \frac{11\pi}{2}, \dots$$

From eq(i) $I = \frac{A^2 \sin^2 \alpha}{\varphi^2}$

when $\alpha = 0$

$$[I_0 = A^2] \text{ (central maxima)}$$

For $\alpha = \pm \frac{3\pi}{2}$ $I_1 = \frac{A^2 \sin^2 \left(\pm \frac{3\pi}{2} \right)}{\left(\frac{3\pi}{2} \right)^2}$

$$I_1 = \frac{4A^2 \sin^2 \left(\pm \frac{3\pi}{2} \right)}{9\pi^2} = I_1 = \frac{4}{9\pi^2} A^2$$

For $\alpha = \pm \frac{5\pi}{2}$ $I_2 = \frac{A^2 \sin^2 \left(\pm \frac{5\pi}{2} \right)}{\left(\frac{5\pi}{2} \right)^2}$

$$I_2 = \frac{4A^2 \sin^2 \left(\pm \frac{5\pi}{2} \right)}{25\pi^2} = \frac{4A^2}{25\pi^2}$$

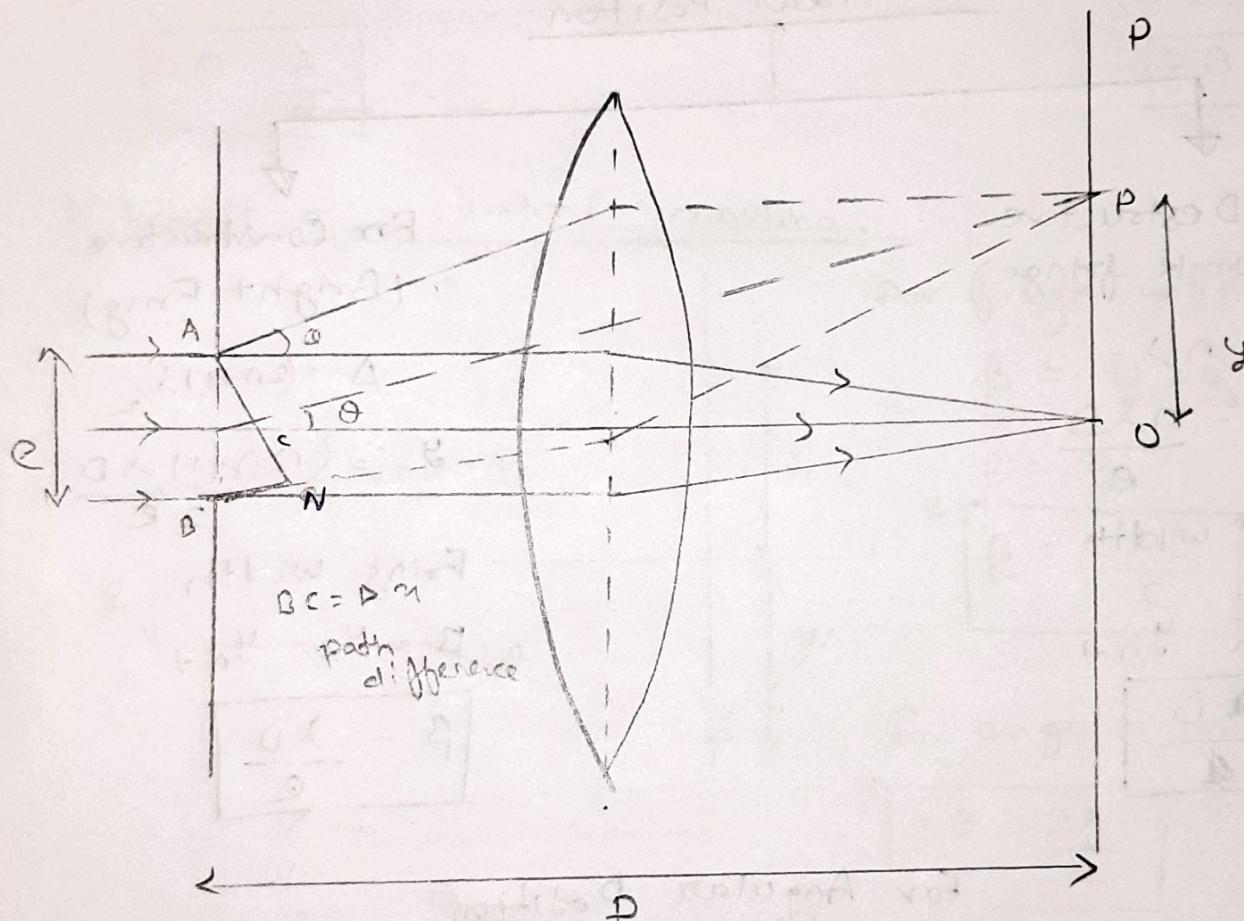
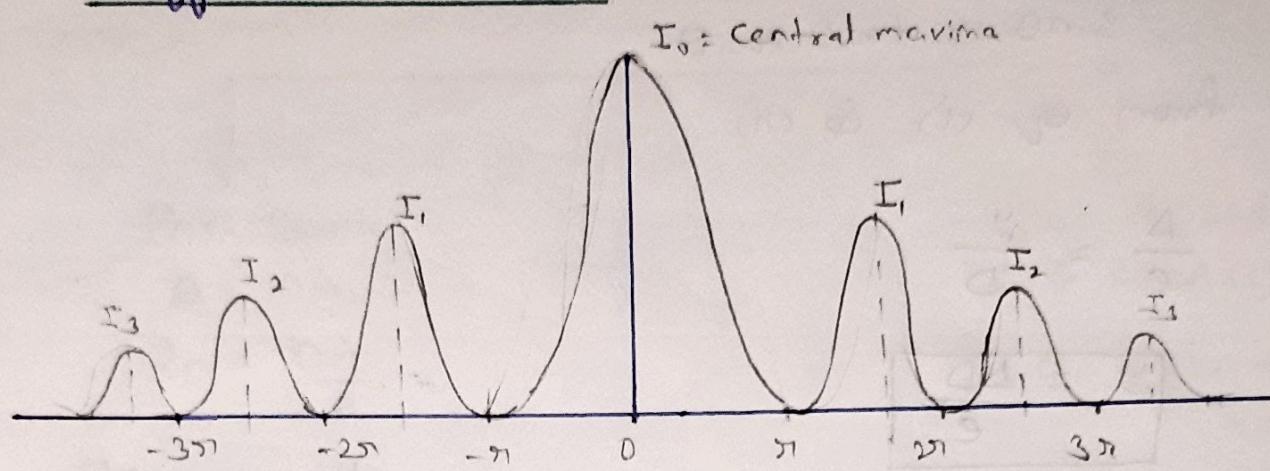
For $\alpha = \pm \frac{7\pi}{2}$ $I_3 = \frac{A^2 \sin^2 \left(\pm \frac{7\pi}{2} \right)}{\left(\frac{7\pi}{2} \right)^2}$

$$I_3 = \frac{4A^2}{49\pi^2}$$

Ratio of intensities

$$I_0 : I_1 : I_2 : I_3 = 1 : \frac{4}{9\pi^2} : \frac{4}{25\pi^2} : \frac{4}{49\pi^2}$$

* Diffraction Pattern :-



In $\triangle ABN$

$\Delta = \text{Path diff.}$

$$\theta = \sin \theta = \frac{\Delta}{e} \quad (\text{in})$$

$$\Delta = e \sin \theta$$

In $\triangle CPO$

$$\tan \alpha = \frac{OP}{CO} = \frac{y}{D}$$

$$\tan \alpha = \frac{y}{D} \quad (\text{in})$$

when angle is very small

$$\sin \theta \approx \tan \theta \approx \theta$$

from eq (i) & (ii)

$$\frac{\Delta}{e} = \frac{y}{D}$$

$$y = \frac{\Delta D}{e}$$

for linear Position

For Destructive
(Dark fringe)

$$\Delta = n\lambda$$

$$y_n = \frac{n\lambda D}{e}$$

Fringe width

$$\beta = y_n - y_{n-1}$$

$$\beta = \frac{\lambda D}{e}$$

For Constructive
(Bright Fring)

$$\Delta = (2n+1)\lambda/2$$

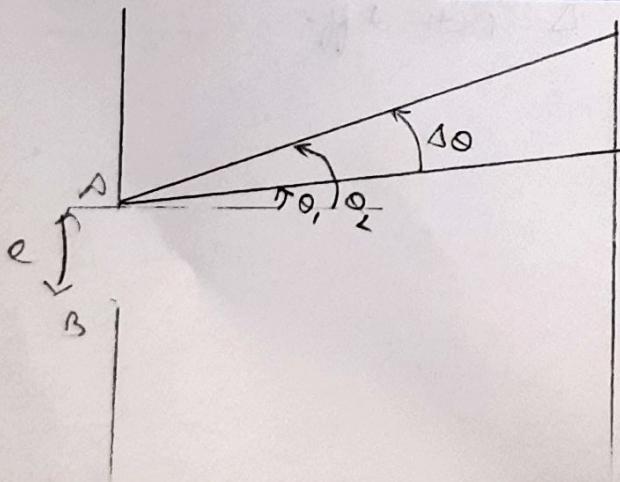
$$y_n = \frac{(2n+1)\lambda D}{2e}$$

Fring width

$$\beta = y_n - y_{n-1}$$

$$\beta = \frac{\lambda D}{e}$$

for Angular Position



From eq (i)

$$\Delta = e \sin \theta$$

$$\sin \theta = \frac{\Delta}{e}$$

When angle is very small

$$\theta = \frac{\Delta}{e}$$

Path diff

Angular Position

For Dark

$$\Delta = n\lambda$$

$$\theta_n = \frac{n\lambda}{e}$$

For Bright

$$\Delta = (2n+1)\frac{\lambda}{2e}$$

$$\theta_n = \frac{(2n+1)\lambda}{2e}$$

Angular width

$$\Delta\theta = \theta_n - \theta_{n-1}$$

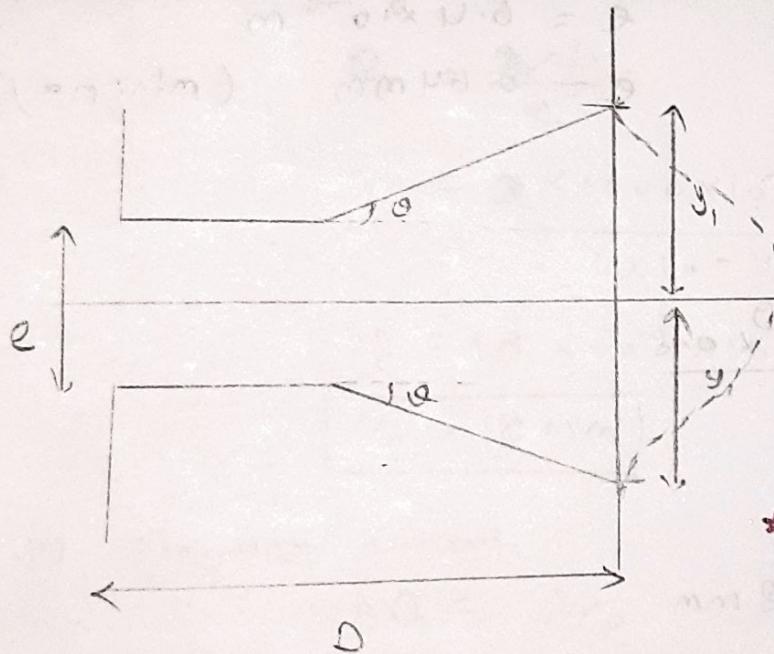
$$\boxed{\Delta\theta = \frac{\lambda}{e}}$$

Angular width

$$\Delta\theta = \theta_n - \theta_{n-1}$$

$$\boxed{\Delta\theta = \frac{\lambda}{e}}$$

* Width of central maxima:-



for fringe width

$$\beta = y_1 + y_2$$

$$\beta = 2y_1$$

$$\boxed{\beta_c = \frac{2\lambda D}{e}}$$

for angular width

$$\boxed{\Delta\theta = \frac{2\lambda}{e}}$$

Q A parallel beam of light of wavelength 6000nm is incident normally on a slit of width 'e'. If the distance between slit and screen is 0.8 m and the distance of second order maxima for the centre of the screen is which 15 mm, calculate the width of slit.

Sol

Given

$$D = 0.8 \text{ m}$$

$$\lambda = 6000 \text{ nm}$$

$$y_2 = 15 \text{ mm}$$

$$\therefore y = \frac{n \lambda D}{e}$$

$$15 \times 10^{-3} = \frac{2 \times 6000 \times 10^{-9} \times 0.8}{e}$$

$$e = \frac{9.6 \times 10^{-4}}{15}$$

$$e = 6.4 \times 10^{-4} \text{ m}$$

$$e = 0.64 \text{ mm. (minima)}$$

$$y_n = \frac{(2n+1) \lambda D}{2e}$$

$$15 \times 10^{-3} = \frac{5 \times 6000 \times 10^{-9} \times 0.8}{2e}$$

$$e = \frac{1.6 \times 10^{-3}}{2}$$

$$e = 0.8 \times 10^{-3} = 0.8 \text{ mm}$$

- Q Yellow light ($\lambda = 6000 \text{ \AA}$) illuminates a single slit of width $1 \times 10^{-4} \text{ m}$. Calculate -
- The distance between the two dark lines on either side of the central maxima, when the diffraction pattern is viewed on a screen kept 1.5 m away from the slit.
 - The angular spread of the first diffraction minima.

Sol" Given $D = 1.5 \text{ m}$
 $\lambda = 6000 \text{ \AA}$
 $a = 1 \times 10^{-4} \text{ m}$

(i) dark fringe width

$$R_c = \frac{2\lambda D}{a}$$

$$Y_c = \frac{2 \times 6000 \times 10^{-10} \times 1.5}{1 \times 10^{-4}}$$

$$Y_c = 18 \times 10^{-7} \times 10^4$$

$$\boxed{Y_c = 18 \text{ mm}}$$

(ii) Angular width

$$\Delta\theta = \frac{\lambda}{a}$$

$$\Delta\theta = \frac{6000 \times 10^{-10}}{1 \times 10^{-4}}$$

$$\Delta\theta = 6 \text{ mrad}$$

Q3 Monochromatic light of wavelength 5890 \AA is incident normally on a slit of width 0.003 mm . Find the ~~the~~ angular position of first and second minima in diffraction pattern of a slit.

Soln Given -

$$\lambda = 5890\text{ \AA} \quad \Delta\theta_1 = ? \quad \Delta\theta_2 = ?$$

$$e = 0.003\text{ mm}$$

$$\sin\theta_1 = \frac{n\lambda}{e}$$

$$\theta_2 = \frac{2\lambda}{e}$$

$$\sin\theta_1 = \frac{5890 \times 10^{-10}}{3 \times 10^{-6}}$$

$$\sin\theta_2 = 2 \times \theta_1$$

$$\sin\theta_1 = 19.63 \times 10^{-4}$$

$$\sin\theta_2 = 0.392 \cancel{\text{rad}}$$

$$\sin\theta_1 = 0.196 \cancel{\text{rad}}$$

~~sin\theta~~

$$\theta_2 = \sin^{-1}(0.392)$$

$$\theta_2 = 23.07 \cancel{\text{rad}}$$

$$\theta_1 = 11.303 \text{ rad}$$

