

## 1. (10 points) 9.23

When a CPU writes to the cache, both the item in the cache and the corresponding item in the memory must be updated. If data is not in the cache, it must be fetched from memory and loaded in the cache. If  $t_1$  is the time taken to reload the cache on a miss, show that the effective average access time of the memory system is given by

$$t_{ave} = ht_c + (1 - h)t_m + (1 - h)t_1$$

- Assuming the cache does not have to be reloaded, the average access time is equal to

$$t_{ave} = ht_c + (1 - h)t_m$$

In this case, the cache does take time to reload. For a single access, the time taken to reload the cache must be added to the no-miss access time. Since we are concerned about the average time, the cache reload time multiplied by the cache miss ratio must be added to the prior equation. This gives us

$$t_{ave} = ht_c + (1 - h)t_m + (1 - h)t_1$$

which is the hit ratio multiplied by the cache access time plus the miss ratio multiplied the memory access time plus the miss ratio multiplied by cache reload time.

## 2. (10 points) 9.26

A system has a level 1 cache and a level 2 cache. The hit rate of the level 1 cache is 90%, and the hit rate of the level 2 cache is 80%. An access to level 1 cache requires one cycle, an access to level 2 cache requires four cycles, and an access to main memory requires 50 cycles. What is the average access time?

- The average access time can be expressed as a sum of the various access times multiplied by their respective occurrence rates:

$$t_{avg} = h_1 t_{c1} + (1 - h_1) h_2 t_{c2} + (1 - h_1)(1 - h_2) t_m$$

where  $h_1$  is the l1 cache hit rate,  $h_2$  is the l2 cache hit rate,  $t_{c1}$  is the l1 cache access time,  $t_{c2}$  is the l2 cache access time, and  $t_m$  is the main memory access time. On average, the l1 cache access occurs as frequently as the l1 hit rate, the l2 cache access occurs as frequently as the l1 miss rate, and the main memory access occurs as frequently as the l2 miss rate and the l1 miss rate. Plugging in values gives:

$$t_{avg} = .9 \times 1 + .1 \times .8 \times 4 + .1 \times .2 \times 50 = \mathbf{2.22 \text{ cycles}}$$

## 3. (10 points) 9.35

A 64-bit processor has an 8-MB, four-way set-associative cache with 32-byte lines. How is the address arranged in terms of set, line, and offset bits?

- With a four way set associative 8MB cache, each set will be 2MB in size. 32 byte lines means the number of lines will be  $\frac{2^{30}}{2^6}$ , or  $2^{24}$ . This means that 24 of the 64 bits will be required for the line number. Since the line size is 32 bytes, or  $2^6$ , 6 bits will be required for the line offset. Since the cache has four, or  $2^2$ , sets, 2 bits will be required for the set number.
- 4. (10 points) Assume a 64-bit virtual address and a 64-bit physical address. The page size is 4KB. How many total entries are there in the page table? Express your answer in powers of 2.
- The table is given as  $4KB = 4 * 2^{10} = 2^2 * 2^{10} = 2^{12}$  bytes.
- Since the physical and virtual addresses are the same size, one address in ram and one address in the page table are the same size.

- A 64-bit address is equal to 8 bytes, or  $2^3$  bytes.
- Therefore, the table can fit  $\frac{2^{12}}{2^3}$ , or **512** entries.

5. (10 points) 7.16

Derive an expression for the speedup ratio (i.e., the ratio of the execution time without pipelining to the execution time with pipelining) of a pipelined processor in terms of the number of stages in the pipeline  $m$  and the number of instructions to be executed  $N$ .

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6. (10 points) 9.12

How is data in main store mapped on to each of the following?

a) Direct-mapped Cache:

In a direct mapped cache, the main store is split into a number of equal sets, where each set is the size of the cache. From there, the sets are divided into lines, where the number of lines in the set is equal to the total number of lines in the cache.

b) Fully-Associative Cache:

In a fully associative cache, lines are taken from main memory and stored directly in cache. Each line's location is tagged with an address, and each line has an associated data validity bit.

c) Set-Associative Cache:

In a set associative cache, the cache is broken up into  $n$  sets for an  $n$ -way associative cache. A line has the same address across all  $n$  sets. When searching for an item, the sets are searched in parallel. When a match is found in any set, the search ends.

7. (10 points) 7.18

A processor executes an instruction in the following six stages. The time required by each stage in picoseconds is given for each stage.

IF	Instruction Fetch	300ps
ID	Instruction Decode	150ps
OF	Operand Fetch	250ps
OE	Execute	350ps
M	Memory Access	700ps
OS	Operand Store (writeback)	200ps

a. What is the time to execute an instruction if the processor is not pipelined?

If the processor is not pipelined, each instruction will have to go through the whole fetch/execute process before the next can start. This gives the time to execute an instruction as:

$$300ps + 150ps + 250ps + 350ps + 700ps + 200ps = \mathbf{1950ps}$$

b.

8. (10 points) 6.13

A computer has the following parameters:

Operation	Frequency	Cycles
Arithmetic/logic instructions	65%	1
Register load operations	10%	5
Register store operations	5%	2
All branch instructions	20%	8

If the average performance of the computer (in terms of its CPI) is to be increased by 20% while executing the same instruction mix, what target must be achieved for the cycles per conditional branch instruction?

- The CPI for branch instructions executed by machine A is as follows:  

$$CPI_A = \frac{freq_{ar}}{100} \times cyc_{ar} + \frac{freq_{ld}}{100} \times cyc_{ld} + \frac{freq_{st}}{100} \times cyc_{st} + \frac{freq_{br}}{100} \times cyc_{br}$$
When values are plugged in, we get:  

$$CPI_A = .65 + .5 + .1 + 1.6 = 2.85$$
- We know that a 20% performance increase is desired. This means our new CPI will be equal to our old CPI multiplied by 1.2, or  

$$CPI_B = \frac{CPI_A}{1.2} = 2.375$$
- If we reorder the equation from the first bullet for finding the branch instruction cycles using our new CPI, we get:  

$$cyc_{br} = \frac{CPI_B - \frac{freq_{ar}}{100} \times cyc_{ar} - \frac{freq_{ld}}{100} \times cyc_{ld} - \frac{freq_{st}}{100} \times cyc_{st}}{\frac{freq_{br}}{100}}$$
Plugging values in gives us:  

$$cycles_{branch} = \frac{2.375 - .65 - .5 - .1}{.2} = 5.625$$
We can only have integer multiples of clock cycles. Since 5.625 is our minimum target, 6 cycles will be too slow. This means that to see a 20% performance increase, we need to see branch instructions being executed in **5 cycles**

9. (15 points) 7.35

A RISC processor has an eight-stage pipeline: F D O E1 E2 MR MW WB (fetch, decode, register read operands, execute 1, execute 2, memory read, memory write, result writeback to register). Simple logical and arithmetic operations are complete by the end of E1. Multiplication is complete by the end of E2. How many cycles are required to execute the following code assuming that internal forwarding is not used?

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MUL    r0, r1, r2
ADD     r3, r1, r4
ADD     r5, r1, r6
ADD     r6, r5, r7
LDR     r1, [r2]
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- asdf

10. (15 points) 7.38

the following table gives a sequence of instructions that are performed on a four-stage pipelined computer. Detect all hazards. For example, in instruction m uses operand r2 generated by instruction m-1, the write m-1,r2 in the RAW column in line m.

Number	Instruction	RAW	WAR	WAW
1	ADD r1, r2, r3			
2	ADD r4, r1, r3			
3	ADD r5, r1, r2			
4	ADD r1, r2, r3			
5	ADD r5, r2, r3			
6	ADD r1, r6, r6			
7	ADD r8, r1, r5			