

11.15

EE23BTECH11029 - Kanishk

Question:

A SONAR system fixed in a submarine operates at a frequency 40.0 kHz. An enemy submarine moves towards the SONAR with a speed of 360 km/hr. What is the frequency of sound reflected by the submarine? Take the speed of sound in water to be 1450 m/s.

Solution:

Operating frequency of the SONAR system, $f = 40\text{kHz}$

Speed of the enemy submarine, $V_e = 360\text{km/h} = 100\text{m/s}$

Speed of sound in water, $V = 1450\text{m/s}$

The source(SONAR system) is at rest and the observer (enemy submarine) is moving toward it.

Enemy submarine(observer) is approaching the SONAR(source), So

$$V_{rel} = V + V_e \quad (1)$$

As we know,

$$\lambda = \frac{V}{f} \quad (2)$$

Frequency observed by the enemy submarine would be

$$f' = V_{rel}/\lambda \quad (3)$$

Now by putting equation 1 and equation 2 in equation 3 we got

$$f' = \left(\frac{V + V_e}{V}\right)f \quad (4)$$

$$= \left(\frac{1450 + 100}{1450}\right)40 = 42.76\text{kHz}$$

This frequency (f') is reflected by the enemy ship and is observed by the SONAR (which now acts as observer). Now the the enemy submarine has become source,

In time period T the wave reflected by source(enemy submarine) will travel distance VT and source will travel by distance $V_e T$

So the change in displacement by the wave and source would be the wavelength of the wave

$$\lambda_2 = T(V - V_e) \quad (5)$$

$$T = 1/f' \quad (6)$$

Putting equaion 6 in equation 5 we get,

$$\lambda_2 = \left(\frac{V - V_e}{f'}\right) \quad (7)$$

As we know,

$$f'' = V/\lambda_2 \quad (8)$$

By putting equation 7 in equation 8 we got,

$$f'' = \left(\frac{V}{V - V_e}\right)f' \quad (9)$$

$$f'' = \left(\frac{1450}{1450 - 100}\right)42.76$$

$$= 45.93\text{kHz}$$

The equation of reflected wave is given as:

$$y = A \sin(2\pi * f''t + -\frac{2\pi}{\lambda}x) \quad (10)$$

where A is amplitude of wave generated.

Input Table:

f	f''
30kHz	34.44kHz
20kHz	22.96kHz
55kHz	63.14kHz
29kHz	33.29kHz
60kHz	68.88kHz
65kHz	74.62kHz