

Analyzing the Time Complexity of a Program

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```
1 void duplicatePrint(int[] a, int n) {  
2     for (int i = 0; i < n; i++) {  
3         for (int j = 0; j < i; j++) {  
4             for (int k = 0; k < 5; k++) {  
5                 System.out.println(a[k]);  
6             }  
7         }  
8     }  
9 }
```

Examples:

If n = 5:

- The outer loop runs n times, which is 5 times.
 - The middle loop runs i times, which is also 5 times.
 - The inner loop runs 5 times regardless of the value of n.
- Total of 125 times

If n = 6:

- The outer loop runs n times, which is 6 times.
 - The middle loop runs i times, which is also 6 times.
 - The inner loop runs 5 times regardless of the value of n.
- Total of 180 times

If n = 7:

- The outer loop runs n times, which is 7 times.
 - The middle loop runs i times, which is also 7 times.
 - The inner loop runs 5 times regardless of the value of n.
- Total of 245 times

If n = 8:

- The outer loop runs n times, which is 8 times.
 - The middle loop runs i times, which is also 8 times.
 - The inner loop runs 5 times regardless of the value of n.
- Total of 320 times

All the above examples run for $f(n) = 5 \times n^2$ time.

The inner most loop runs 5 times regardless of the value of n, so it runs a constant time.

The number of times the other two loops runs will be dependent on the value of n.

```
1 void duplicatePrint(int[] a, int n) {  
2     for (int i = 0; i < n; i++) {O (n)  
3         for (int j = 0; j < i; j++) {O (n)  
4             for (int k = 0; k < 5; k++) {O (5)  
5                 System.out.println(a[k]);Constant time  
6             }  
7         }  
8     }  
9 }
```

We have two loops that run n times, and one that runs 5 times. If we multiply all of them together, we get the expression $O(5n^2)$ which is the same as $O(n^2)$. Therefore, this program has an asymptotic upper bound of $O(n^2)$.