

## Example: Attribute Selection with Information Gain

□ Class P: buys\_computer = "yes"

□ Class N: buys\_computer = "no"

$$Info(D) = I(9,5) = -\frac{9}{14} \log_2\left(\frac{9}{14}\right) - \frac{5}{14} \log_2\left(\frac{5}{14}\right) = 0.940$$

age	$p_i$	$n_i$	$I(p_i, n_i)$
<=30	2	3	0.971
31...40	4	0	0
>40	3	2	0.971

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no

$$Info_{age}(D) = \frac{5}{14} I(2,3) + \frac{4}{14} I(4,0) + \frac{5}{14} I(3,2) = 0.694$$

$\frac{5}{14} I(2,3)$  means "age <=30" has 5 out of 14 samples, with 2 yes'es and 3 no's.

Hence

$$Gain(age) = Info(D) - Info_{age}(D) = 0.246$$

Similarly, we can get

$$Gain(income) = 0.029$$

$$Gain(student) = 0.151$$

$$Gain(credit\_rating) = 0.048$$

### 1. คำนวณ Info(D)

$$\begin{aligned} Info(D) &= I(8,4) \\ &= -8/12 \log_2(8/12) - 4/12 \log_2(4/12) \\ &= 0.9183 \end{aligned}$$

### 2. คำนวณ Info<sub>age, income, student, credit</sub>(D)

$$\begin{aligned} 2.1. \quad Info_{age}(D) &= 4/12 I(2,2) + 3/12 I(3,0) + 5/12 I(3,2) \\ &= 4/12 (1) + 3/12 (0) + 5/12 (0.9710) \\ Info_{age}(D) &= 0.5761 \end{aligned}$$

$$\begin{aligned} 2.2. \quad Info_{income}(D) &= 4/12 I(2,2) + 5/12 I(4,1) + 3/12 I(2,1) \\ &= 4/12 I(1) + 5/12 I(0.7219) + 3/12 I(0.9183) \\ &= 0.8637 \end{aligned}$$

$$\begin{aligned} 2.3. \quad Info_{student}(D) &= 6/12 I(5,1) + 6/12 I(3,3) \\ &= 6/12 I(0.6500) + 6/12 I(1) \\ &= 0.8250 \end{aligned}$$

$$\begin{aligned} 2.4. \quad Info_{credit}(D) &= 7/12 I(6,1) + 5/12 I(2,3) \\ &= 7/12 I(0.6906) + 5/12 I(0.9710) \\ &= 0.8074 \end{aligned}$$

### 3. คำนวณหา Gain

$$\begin{aligned} 3.1 \quad \text{Gain}(\text{age}) &= 0.9183 - 0.5761 \\ &= 0.3422 \end{aligned}$$

$$\begin{aligned} 3.2 \quad \text{Gain}(\text{income}) &= 0.9183 - 0.8637 \\ &= 0.0546 \end{aligned}$$

$$\begin{aligned} 3.3 \quad \text{Gain}(\text{student}) &= 0.9183 - 0.8250 \\ &= 0.0933 \end{aligned}$$

$$\begin{aligned} 3.4 \quad \text{Gain}(\text{credit}) &= 0.9183 - 0.8074 \\ &= 0.1109 \end{aligned}$$

**สรุป** ได้ค่า  $\text{Gain}(\text{age}) = 0.3422$  เป็นค่าที่มากที่สุดจึงให้ age เป็น root node