## Test tex!

#### NUAA

### Janurary 2021

## Introduction

1. Let's begin with a formula  $e^{i\pi}+1=0$ 

$$e = \lim_{n \to \infty} \left( 1 + \frac{1}{n} \right)^n = \lim_{n \to \infty} \frac{n}{\sqrt[n]{n!}}$$

2. we can do another:

$$e = \sum_{n=0}^{\infty} \frac{1}{n}.$$

3. we can also use continued fractions:

$$e = 2 + \frac{1}{1 + \frac{2}{2 + \frac{3}{3 + \frac{4}{4 + \frac{5}{5}}}}}$$
<sub>5+</sub> ...

## More formulas

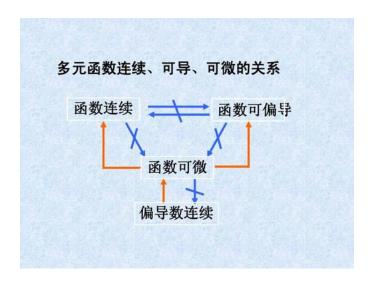
$$\int_{a}^{b} f(x)dx$$

$$\iiint f(x, y, z)dxdydz$$

$$\vec{v} = \langle v_{1}, v_{2}, v_{3} \rangle$$

$$\vec{v} \cdot \vec{w}$$

$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \end{bmatrix}$$



**1.1** A find the sum of 34 and 126 using a caculator.

$$34 + 126 = \boxed{160}$$

**B** Find the sum using long addition.

**1.2** Evaluate the following definite integral:

$$\int_{0}^{3} 2x \sqrt{x^{2} + 4} dx$$

$$u = x^{2} + 4 \quad du = 2x$$

$$\Rightarrow \int_{0^{2} + 4}^{3^{2} + 4} \sqrt{u} du = \frac{1}{2} u^{-\frac{1}{2}} \Big|_{4}^{13}$$

$$\frac{1}{2\sqrt{13}} - \frac{1}{2\sqrt{4}} \approx \boxed{-0.1113}$$

**2.1** A Find the root of the quadratic equation  $y = x^2 + 2x - 3$  using the quadratic formula.

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

# 1 Weighted Residual Methods

Fundamental equations Consider the problem governed by the differential equation:

$$\Gamma u = -\overline{f}$$
 in D

The above differential equation is solved by using the boundary conditions given as follows:

$$\boldsymbol{u} = -\overline{\boldsymbol{u}}$$
 on  $S_u$ 

$$t \equiv Bu = \overline{t}$$
 on  $S \setminus S_t$ 

where the boundary S consists of  $S_t$  and  $S_u$ . The boundary conditions given in eqs. (84) and (85) are called rigid and natural boundary conditions, or Dirichlet and Neumann boundary conditions, respectively. In most engineering problems,  $\Gamma$  and B are different operators in the forms of  $bm\Gamma = \Delta \cdot \Sigma$  and  $B = n \cdot \Sigma$ , where  $\varsigma$  is another differential operators and n is the normal vector on  $S_t$ .

$$\Delta^2 u = -\overline{f} \quad in \ D,$$