

* A car company believes that the percentage of residents in city ABC that owns a vehicle is 60% or less. A sales manager disagrees with this. He conducts a hypothesis testing surveying 250 residents and found that 170 responded Yes to owning a vehicle.

- State the null & Alternate hypothesis
- At 10% significance level is there enough evidence to support the idea that vehicle ownership in city ABC is 60% or less?

Ans:- Given $H_0 : P \leq 0.60 \rightarrow$ null hypothesis
 $H_a : P > 0.60 \rightarrow$ alternate hypothesis

$$n = 250, \bar{x} = 170$$

$$\hat{p} = \frac{\bar{x}}{n} = \frac{170}{250} = 0.68 \Rightarrow \hat{p} = 0.68$$

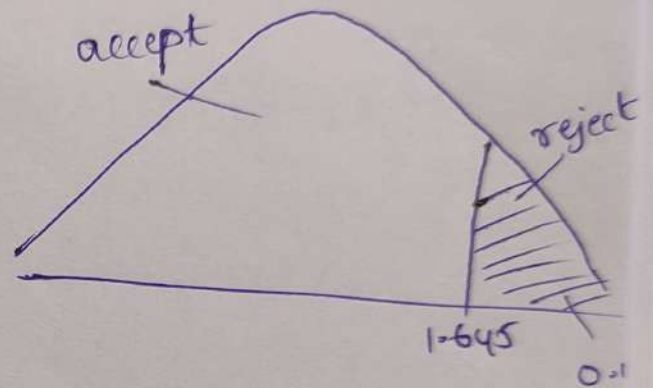
$$P_0 = 0.60, q_0 = 1 - 0.60 \Rightarrow 0.40$$

Significance level $\alpha = 10\% \Rightarrow 0.10$, Confidence level = $1 - 0.10 \Rightarrow 0.90$

\Rightarrow Decision boundary

2022.7.10 18:17

$$Z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0 q_0}{n}}} = \frac{0.68 - 0.60}{\sqrt{\frac{0.60(0.40)}{250}}} = \frac{0.08}{0.030984} = 2.58$$

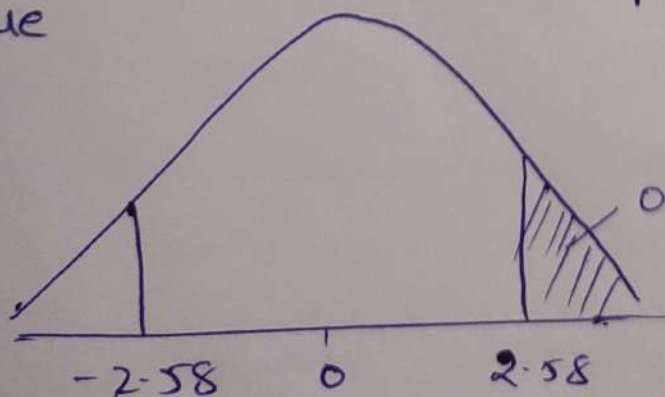


$1.645 < 2.58$ reject hypothesis

At 10% significance there is enough evidence to reject the idea that the vehicle ownership city ABC is 60%.

P-value

$$p\text{-value} = P(Z \geq 2.58)$$



$$0.009506$$

$$p\text{value} = 0.009506 + 0.009506 = 0.019$$

2022.7.10 18:18