
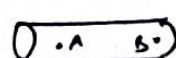


## M.P.F

①  $P = \frac{F_{\perp}}{A}$

②   $P = P_0 + \rho gh$

③ 


Horizontally pressure remains same

$$P_A = P_B$$

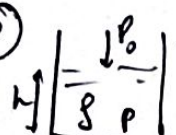
④ 

$$\rho_{mix} = \frac{m_1 + m_2}{(m_1/\rho_1) + (m_2/\rho_2)}$$

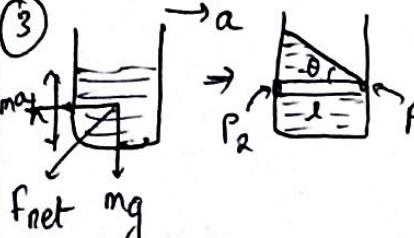
Variation in P in a fluid.

① 

$$P = P_0 + \rho(g+a)h$$

② 

$$P = P_0 + \rho(g-a)h$$

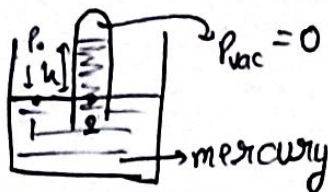
③ 

$$P_2 - P_1 = \rho la$$

$$\tan \theta = \frac{h}{l} = \frac{a}{g}$$

## Barometer

↳ measure atm. P



$$P_0 = \rho gh$$

## Manometer

↳ measure P of an enclosed gas



$$P_{gas} = P_0 + \rho gh$$

$$P_{gas} - P_0 = \rho gh$$

gauge pressure


## Upthrust / Buoyancy

$$U = V \rho g$$

V → Volume of solid immersed  
 $\rho$  → density of fluid  
 $g$  →

$$\text{Apparent weight} = \text{Weight} - \text{Upthrust}$$

## Law of flotation

  $f_{net} = 0$

$$\text{Wt of body} = \text{Upthrust}$$

$$\rho_s V_s = \rho_f V_f \quad h_s \rho_s = h_f \rho_f$$

## Eqn of continuity

$$AV = \text{constant}$$

$$A \propto \frac{1}{V} \quad \text{or} \quad A_1 V_1 = A_2 V_2$$

↳ Conservation of mass

## Bernoulli's Theorem



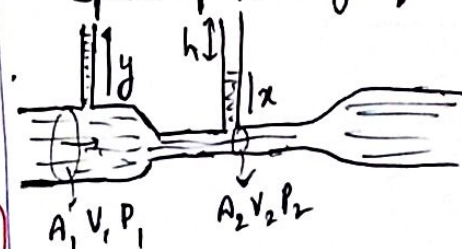
$$P + \rho gh + \frac{1}{2} \rho V^2 = \text{constant}$$

↳ Conservation of energy

$$P_1 + \rho gh_1 + \frac{1}{2} \rho V_1^2 = P_2 + \rho gh_2 + \frac{1}{2} \rho V_2^2$$

$$P_1 - P_2 = \frac{1}{2} \rho (V_2^2 - V_1^2) + \rho g(h_2 - h_1)$$

## Venturimeter: 2 measure speed of flowing liquid



$$V_2^2 - V_1^2 = 2gh$$

$$V_1 = A_2 \sqrt{\frac{2gh}{A_1^2 - A_2^2}}$$

$$V_2 = A_1 \sqrt{\frac{2gh}{A_1^2 - A_2^2}}$$

$$\text{Rate of flow} = A_1 A_2 \sqrt{\frac{2gh}{A_1^2 - A_2^2}}$$



## Critical Velocity

$$V_c = \frac{N_R \eta}{8D}$$

$N_R \rightarrow$  Reynold's No.

$\eta \rightarrow$  Coefficient of viscosity.

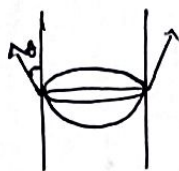
$\rho \rightarrow$  density of liquid.

$D \Rightarrow$  diameter of tube.

## Work done in soap BUBBLE

$$W = 8\pi R^2 T$$

# On mixing highly soluble impurity in water  
 $\Rightarrow T \uparrow$  &  $\theta \uparrow$



Upward force = (Surface T)  $\times$  (length in contact)

$$F_u = T 2\pi R$$

## Applications of Pascal law:

- ① Hydraulic lift
- ② Hydraulic brakes.
- ③ Hydraulic jack.

## Pascal law:

1N =  $10^5$  dyne

$$\frac{F_1}{F_2} = \frac{A_1}{A_2}$$

Value of $N_R$	Type of flow
0 to 2,000	Streamline & stable
2000 to 3000	Streamline $\rightarrow$ Turbulent
Above 3000	Turbulent

$\theta$  is ~~not~~ constant for particular solid-liquid pair

When drops coalesce (combine)

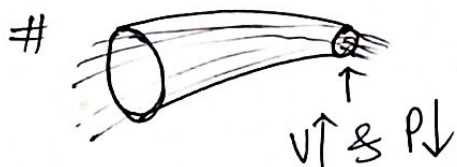
$\Rightarrow$  Volume conservation

When BUBBLE combine

$\Rightarrow$  Area conservation

Shortcut: where  $E =$  Energy

$$\frac{E_{\text{drop}}}{E_{\text{droplets}}} = \frac{1}{n^{2/3}}$$

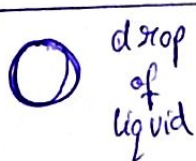


Soap solution is used for cleaning dirty clothes because surface tension of solution is decreased

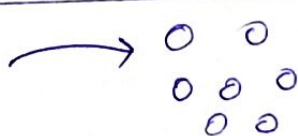
Shortcut: If there is a wire or ring lying on the surface of liquid, always replace 1 by 2L & replace  $2\pi R$  by  $4\pi R$  respectively.

As temperature of a liquid increases, then surface tension (T) (decreases) &

$\cos \theta \uparrow$  &  $\theta \downarrow$



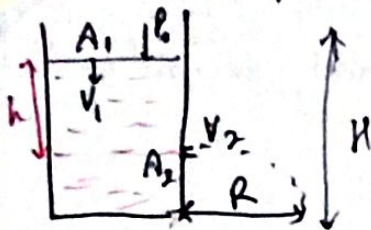
drop of liquid



then surface area increases.



## Speed of efflux:



$$v_2 = \sqrt{2gh} \rightarrow \text{open tank}$$

$$v_2 = \sqrt{2gh + \frac{(P - P_0)}{\rho}} \rightarrow \text{closed tank}$$

$$R = 2\sqrt{h(H-h)}$$

$$R_{\max} = H$$

## Velocity gradient

$$V_g = \frac{dv}{dx} = \frac{\text{change in velocity}}{\text{height}}$$

## Viscous force

$$F_v = -\eta A \frac{dv}{dx}$$

$\eta \rightarrow$  coefficient of viscosity

$$\eta \rightarrow \text{N-s/m}^2$$

$$\text{c.g.s} \rightarrow \frac{\text{dyne-s}}{\text{cm}^2}$$

poise

$$1 \text{ poise} = 10^{-1} \text{ N-s/m}^2$$

$$\eta = [M^1 L^{-1} T^{-1}]$$

## Stoke's Theorem

$$F_v = 6\pi\eta r v$$

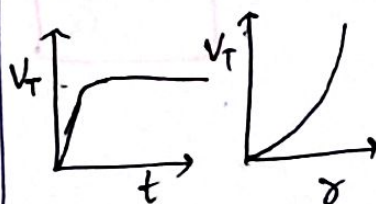
↑ spherical ho  
↑ fluid ka andar  
↑ motion mai ho

## Terminal Velocity



$$V_T = \frac{2}{9} \frac{r^2 (\sigma - \rho_f) g}{\eta}$$

↑ spherical ho  
↑ fluid mai ho



if  $V_T \rightarrow -ve$

↑ Rise upwards

## Surface Tension

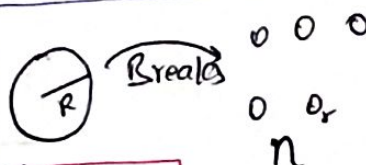
$$T = \frac{F_L}{l}$$



## Surface Energy

$$\Delta U = T \Delta A$$

Note: Soap film has two layers



$$R = n^{1/3} r$$

$$W = 4\pi R^2 T (n^{1/3} - 1)$$

## Capillary action

$$\cos \theta = \frac{r}{R}$$



## Excess P in liquid drop



$$\Delta P = \frac{2T}{R}$$

Excess P in soap Bubble

$$\Delta P = \frac{4T}{R}$$

## Contact angle 'theta'

$$\theta \rightarrow 0^\circ \text{ to } \pi^\circ$$

Note: for kerosen  $\rightarrow \theta = 0^\circ$



concave meniscus

$$\theta < 90^\circ$$

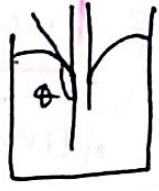
→ Rises

→ Liquid wets glass surface

→ Adhesive > Cohesive

eg methyl iodide, impure water

$$\theta = 29^\circ$$



convex meniscus

$$\theta > 90^\circ$$

→ Falls

→ Liquid do NOT wet glass surface

→ Ad < Coh

eg mercury

$$\theta = 135^\circ$$

#  $\theta = 90^\circ$   
eg water in silver capillary

→ Liquids wets the glass surface

→ Adhesive = Cohesive



$$h = \frac{2T \cos \theta}{r \rho g}$$