

The Notorious 15 Box Puzzle

Mik Zlatin

September 8, 2024

Intro

In all my years of puzzling I have not seen such a simple question spark so much controversy. This lovely intuition-bending puzzle involves 15 boxes and 2 contestants. Who is more likely to win? Or is it a fair game?

Since this question only has 3 possible answers, it can be considered an intuition puzzle. My favorite! You, the puzzler, are encouraged to register a concrete guess before thinking too rigorously about the problem. Then try to justify, or disprove yourself for the best fun.¹

Riddle

The situation is simple. There are 15 boxes arranged in a 3×5 format as follows.

1	2	3	4	5
6	7	8	9	10
11	12	13	14	15

The contest organizers have laid out these 15 boxes, and have selected two of them (uniformly at random without replacement) to contain goats.

The two contestants, Alice and Bob, will open boxes in parallel to try and find a goat first! Both players begin at the top-left box, and open it together in the first round. Then, both players proceed by opening 1 box per round in a predetermined order as follows.

¹I saw this riddle on Gil Kalai's wonderful blog: [Combinatorics and More](#).

Alice opens boxes in “row-major” order, so her box-opening sequence is simply $1, 2, 3, \dots, 14, 15$. Bob goes by columns, from top to bottom, and then left to right. So his box-opening sequence is $1, 6, 11, 2, 7, 12, 3, \dots, 10, 15$.

If Alice and Bob open a box at the same time and it contains a goat, then the game is a tie! If Alice and Bob open two different boxes in the same round, and they both contain a goat, then it is also a tie! In any other case, whoever opens a box with a goat first wins the grand prize: another goat.

Riddle Question: Who is more likely to win the game? Or are Alice and Bob equally likely to win?