

## Data Link Layer

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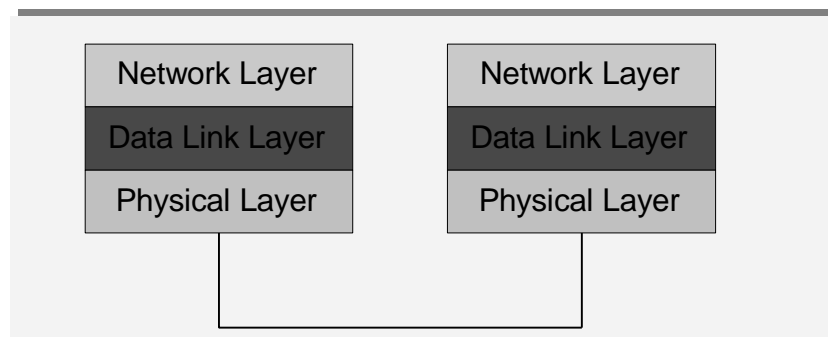
Introduction  
Synchronization  
Error Detection  
Flow Control  
Error Control (via Retransmission)

## Introduction

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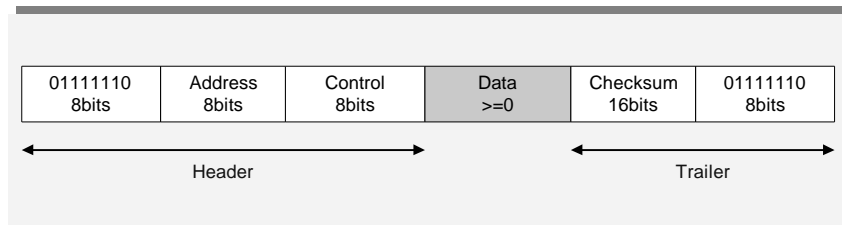
Main Task of the data link layer:

- Provide error-free transmission over a link



## Introduction

- The PDU at the Data Link Layer (DL-PDU) is typically called a Frame. A Frame has a header, a data field, and a trailer
- Example

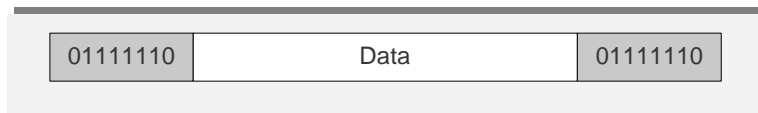


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## Framing

- Problem: Identify the beginning and the end of a frame in a bit stream
- Solution (bit-oriented Framing): A special bit pattern (flag) signals the beginning and the end of a frame (e.g., "01111110")



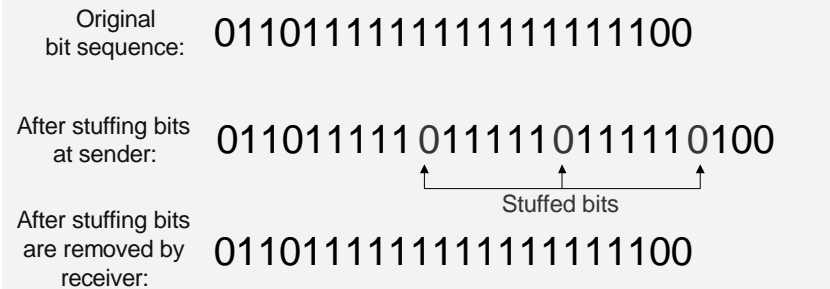
- Problem:
  - The sequence '01111110' must not appear in the data of the frame

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## Bit-Oriented Framing and Bit Stuffing

- 'Bit stuffing': If the sender detects five consecutive '1' it adds a '0' bit into the bit stream. The receiver removes the '0' from each occurrence of the sequence '111110'



- Note: The flags itself are not bit-stuffed.

## Error Control

Two basic approaches to handle bit errors:

- Error-correcting codes
  - Used if retransmission of the data is not possible
  - Data are encoded with sufficient redundancy to correct bit errors
  - **Examples:** Hamming Codes, Reed Solomon Codes, etc.
- Error-detecting codes plus retransmission
  - Used if retransmission of corrupted data is feasible
  - Receiver detects error and requests retransmission of a frame.

## Error Detection Techniques

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- Error Detection Techniques:
  - Parity Checks
  - Cyclic Redundancy Check

## Parity Checks

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General Method:

- Append a parity bit to the end of each character in a frame such that the total number of '1' in a character is:
  - even (even parity) or
  - odd (odd parity)
- **Example:** With ASCII code, a parity bit can be attached to an 7-bit character
  - ASCII "G" = **1 1 1 0 0 0 1**
  - with even parity =
  - with odd parity =

## Cyclic-Redundancy Codes (CRC)

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General Method:

- The transmitter generates an **n-bit check sequence number** from a given **k-bit frame** such that the resulting (k+n)-bit frame is divisible by some number
- The receiver divides the incoming frame by the same number
- If the result of the division does not leave a remainder, the receiver assumes that there was no error

## Cyclic-Redundancy Codes (CRC)

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- CRC is used by all advanced data link protocols, for the following reasons:
  - Powerful error detection capability
  - CRC can be efficiently implemented in hardware
- We discuss the CRC method in five easy steps:
  1. Prerequisites
  2. CRC Encoding Method
  3. Example
  4. Error Detection with CRC
  5. Capabilities of CRC

## Step 1: Prerequisites

### ■ Modulo-2 Arithmetic:

+	1	0
1	0	0
0	1	0

*	1	0
1	1	0
0	0	0

### ■ Examples of polynomials based on Modulo-2 operations:

1.  $(x+1)(x+1) =$
2.  $(x^2+1)(x^3+x+1) =$
3. If  $F(x)$  contains  $(x+1)$  as a factor, then  $F(1) = 0$

## Step 2: CRC Encoding Method

### ■ Let us view each block of data as a polynomial with binary coefficients:

1 0 1 1 0 1 is viewed as  $x^5 + x^3 + x^2 + 1$

Define:

- $M(x)$  Data block is a polynomial (= Message, Frame)
- $P(x)$  "Generator Polynomial" which is known to both sender and receiver (degree of  $P(x)$  is  $n$ )

## Step 2: CRC Encoding Method

- (I) Append  $n$  zeros to  $M(x)$ , i.e.,  $M(x) x^n$
- (II) Divide  $M(x) x^n$  by  $P(x)$  and obtain:  

$$M(x) x^n = Q(x) P(x) + R(x)$$
- (III) Set  $T(x) = M(x) x^n + R(x)$ .  $T(x)$  is the encoded message

Note:  $T(x)$  is divisible by  $P(x)$ . Therefore, if the received message does not contain an error then it can be divided by  $P(x)$ .

■ **Exercise:** Encode the frame **1 1 0 1 0 1 1 0 1 1**

## Step 3: Encoding

$$M(x) = x^9 + x^8 + x^6 + x^4 + x^3 + x + 1$$

- Generator polynomial is  $P(x) = x^4 + x + 1$
- Degree of  $P(x)$  is 4

- (I)  $M(x) x^4 = x^{13} + x^{12} + x^{10} + x^8 + x^7 + x^5 + x^4$
- (II)  $M(x) x^4 = Q(x) P(x) + R(x)$   

$$= (x^9 + x^8 + x^3 + x) P(x) + x^3 + x^2 + x$$
- (III)  $T(x) = M(x) x^4 + R(x)$   

$$= x^{13} + x^{12} + x^{10} + x^8 + x^7 + x^5 + x^4 + x^3 + x^2 + x$$

Transmitted Bit Sequence: **1 1 0 1 0 1 1 0 1 1 1 1 1 0**

## Step 4: Error Detection with CRC

- Errors can be expressed as Error Polynomials

- For example,

**Sent Message:**           1 0 1 1 1 0 1

**Received Message:**   1 1 1 1 0 0 1

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**Error:**                   0 1 0 0 1 0 0

- In the example, the Error Polynomial  $E(x)$  is given by:

$$E(x) = x^5 + x^2$$

## Step 5: Error Detection Capability of CRC

Note:

- Errors will not be detected by CRC if

$$E(x) / P(x) = B(x) + 0,$$

i.e.,  $E(x)$  contains  $P(x)$  as a factor

- Observe the following trade-off:
  - Large values of  $n$  introduce a lot of overhead, but improve the error detection capability.



## Step 5: Error Detection Capability of CRC

- All single-bit errors are detected, if  $P(x)$  has a factor with at least 2 terms:

$$E(x) = x^i$$

If  $P(x) = (x+1)P'(x)$ , then  $x^i$  cannot contain  $(x+1)$

- All double-bit errors are detected if  $P(x)$  has a factor with at least 3 terms

$$E(x) = x^i + x^j = x^j (x^{k+1} + 1) \quad (\text{for } k = i-j, j < i)$$

- If  $P(x)$  does not divide  $(x^k + 1)$  for any  $k$  up to the max. frame length then all double errors can be detected.

$P(x) = x^{15} + x^{14} + 1$  will not divide  $E(x) = x^k + 1$  for any  $k \leq 32,768$

## Step 5: Error Detection Capability of CRC

- If  $P(x)$  contains  $(x+1)$  as a factor then all errors with “odd” number of bits are detected.

- CRC detects 50% of all errors

- A CRC with  $n$  check bits will detect all burst errors of length  $\leq n$  bits.

Burst Error of Length  $k$ :  $E(x) = x^i (x^{k-1} + \dots + 1)$

## Additional Facts on CRC

- CRC can be efficiently implemented in hardware by a set of XOR gates and a shift register
- The following generator polynomials are widely used:

**CRC-12:**  $P(x) = x^{12} + x^{11} + x^3 + x^2 + x + 1$

**CRC-16:**  $P(x) = x^{16} + x^{15} + x^2 + 1$

**CRC-CCITT:**  $P(x) = x^{16} + x^{12} + x^5 + 1$

**CRC-32:**  $P(x) = x^{32} + x^{26} + x^{23} + x^{22} + x^{16} + x^{12} + x^{11} + x^{10} + x^8 + x^7 + x^5 + x^4 + x^2 + x + 1$

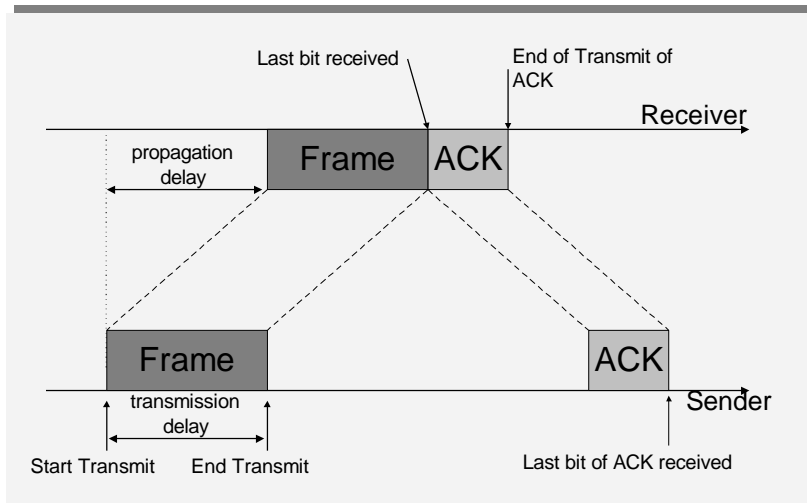
## Flow Control

- Flow Control is a technique for speed-matching of transmitter and receiver. Flow control ensures that a transmitting station does not overflow a receiving station with data
- We will discuss two protocols for flow control:
  - **Stop-and-Wait Protocol**
  - **Sliding Window Protocol**
- For the time being, we assume that we have a perfect channel between sender and receiver (**no errors**)

## Stop-and-Wait Flow Control

- Simplest form of flow control
- In Stop-and-Wait flow control, the receiver indicates its readiness to receive data for each frame
- **Operations:**
  1. **Sender:** Transmit a single frame
  2. **Receiver:** Transmit acknowledgment (ACK)
  3. Goto 1.

## Analysis of Stop-and-Wait



## Analysis of Stop-and-Wait

- **Transmission delay** is the time that the sender needs to transmit a frame
- Transmission delay is dependent on the size of a frame and the maximum data rate

### Example:

Frame Size = 1000 bit

Data rate of network = 1 Mbps

Transmission delay = 1000 bit / 1 Mbps = 1 msec

## Analysis of Stop-and-Wait

- **Propagation delay** is the time that a transmitted bit needs to travel from sender to the receiver
- Propagation delay is only dependent on the speed of the transmission medium and the distance between sender and receiver.

Speed of light: 300,000 km/sec,

Speed in guided media (approx.): 200,000 km/sec

### Example:

Distance = 1000 km

Propagation delay = 1000 km / (200,000 km/sec)

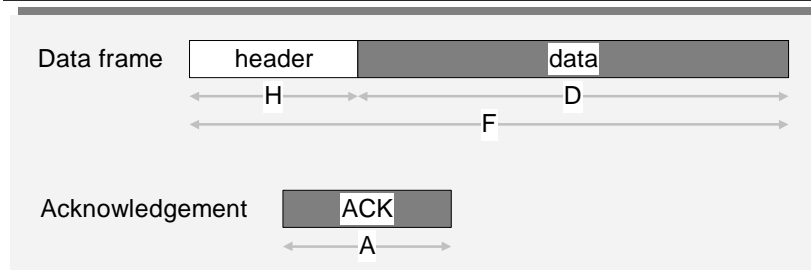
= 5 msec

## Analysis of Stop-and-Wait

### ■ Notation:

C	= Channel capacity in bps
I	= Propagation delay
H	= Number of bits in a frame header
D	= Number of data bits in a frame
F	= Total length of a frame (F= D+H)
A	= Total length of an ACK frame
F/C	= Transmission delay for a frame

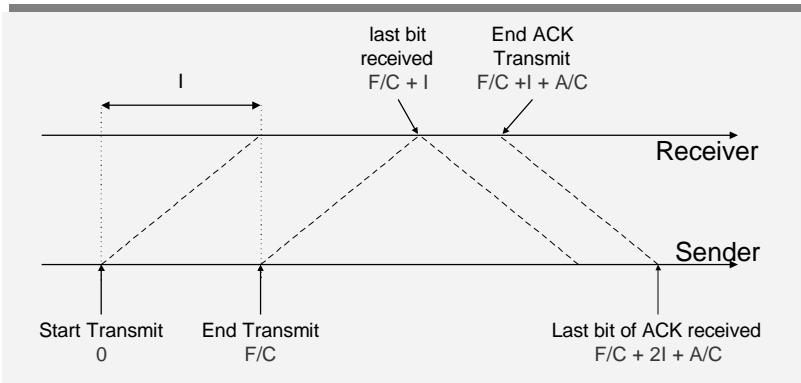
## Analysis of Stop-and-Wait



$$a = \frac{\text{propagation delay}}{\text{transmission delay}} = \frac{I}{F/C}$$

## Analysis of Stop-and-Wait

- Transmission of a frame (in Stop-and-Wait):



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## Analysis of Stop-and-Wait

- **Efficiency** of a protocol is the maximum fraction of time when the protocol is transmitting data
- Efficiency of Stop-and-Wait Flow Control:

$$\text{efficiency} = \frac{D/C}{F/C + A/C + 2I} = \frac{D}{F + A + 2IC}$$

- Assuming that  $H$  and  $A$  are negligible we obtain:

$$\text{normalized efficiency} = \frac{D}{D + 2IC} = \frac{1}{1 + 2a}$$

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## Exercise 1

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### Satellite Link

- Roundtrip propagation delay is 270 ms
  - Data rate is 56 kbps
  - Frame length is 4,000 bits (including header)
  - Lengths of ACK frames are negligible
- 
- What is the value of “a”?
  - What is the efficiency of the satellite link if Stop-and-Wait is used?

## Exercise 2

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### Local Area Network (LAN)

- Data rate is 10 (100) Mbps
  - Propagation rate is 200,000 km/sec
  - Length of the LAN is 10 km
  - Frame size is 500 bits (including header)
  - Length of ACK frames are negligible
- 
- What are the values of “a” for the 10 and 100 Mbps LANs?
  - How efficient are these LANs?
  - What is the minimum frame size in the LANs to reach an efficiency of at least 80%?

## Sliding Window Flow Control

### ■ Major Drawback of Stop-and-Wait Flow Control:

- Only one frame can be in transmission at a time
- This leads to inefficiency if  $a > 1$

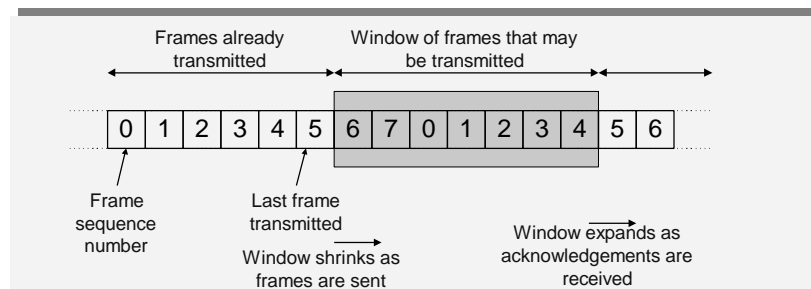
### ■ Sliding Window Flow Control

- Allows transmission of multiple frames
- Assigns each frame a k-bit sequence number
- Range of sequence number is  $[0..2^k-1]$ , i.e., frames are counted modulo  $2^k$

## Operation of Sliding Window

### ■ Sending Window:

- At any instant, the sender is permitted to send frames with sequence numbers in a certain range
- The range of sequence numbers is called the *sending window*

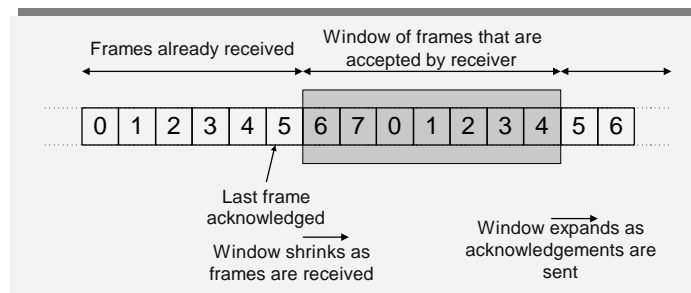




## Operation of Sliding Window

### ■ Receiving Window:

- The receiver maintains a *receiving window* corresponding to the sequence numbers of frames that are accepted

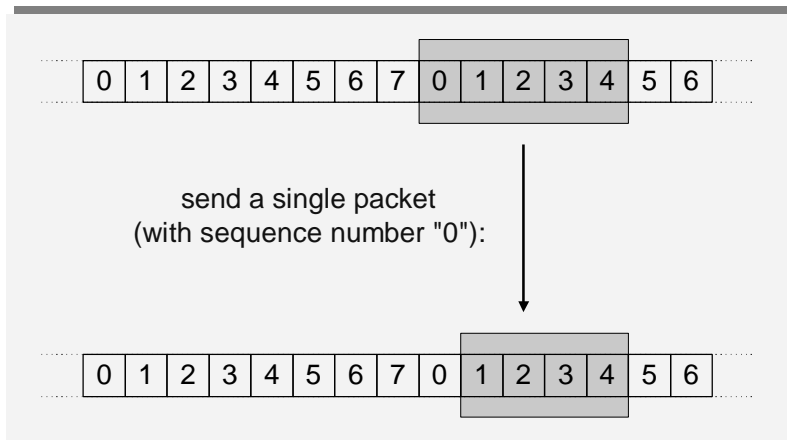


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## Operation of Sliding Window

### ■ Operations at the sender:

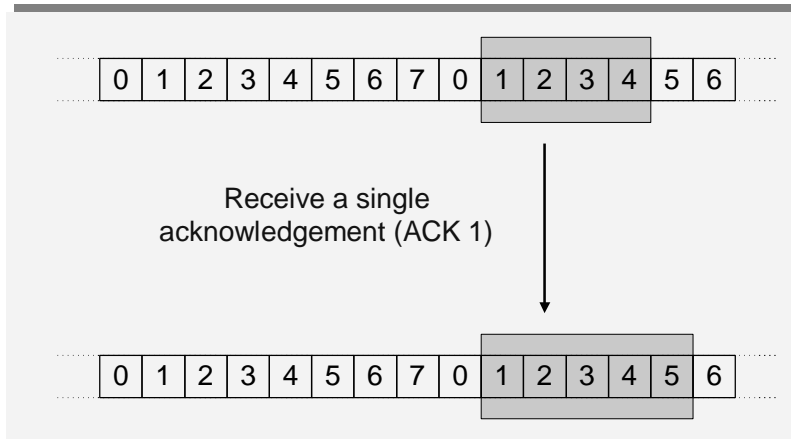


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## Operation of Sliding Window

### ■ Operations at the sender:

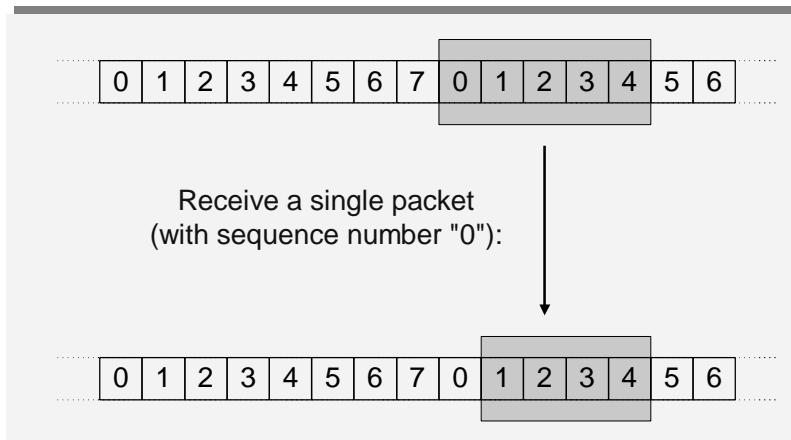


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## Operation of Sliding Window

### ■ Operations at the receiver:

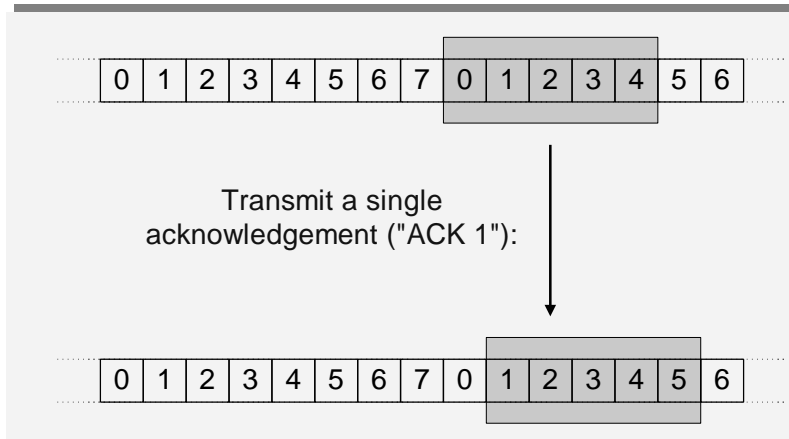


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## Operation of Sliding Window

### ■ Operations at the receiver:



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## Operation of Sliding Window

### ■ How is "flow control" achieved?

- Receiver can control the size of the sending window
- By limiting the size of the sending window data flow from sender to receiver can be limited

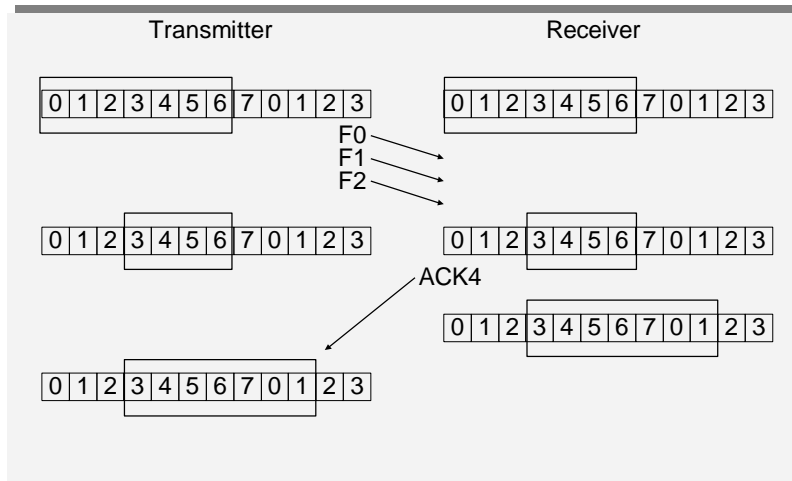
### ■ Interpretation of **ACK N** message:

- Receiver acknowledges all packets until (but not including) sequence number N

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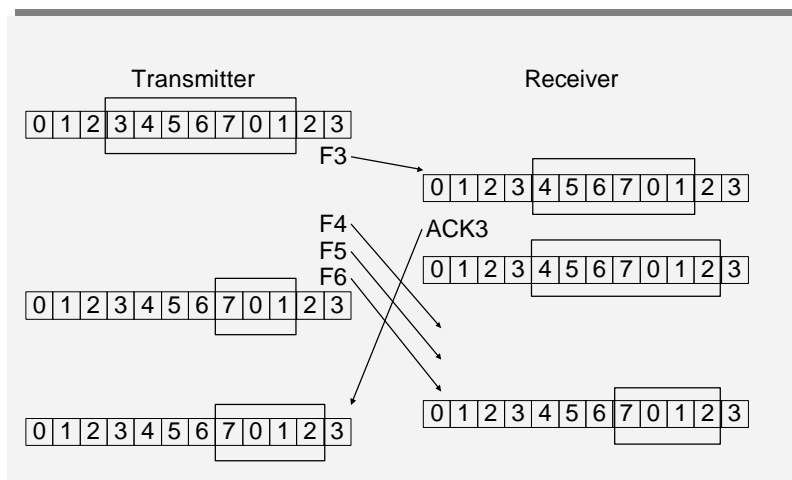
## Example



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## Example Continued



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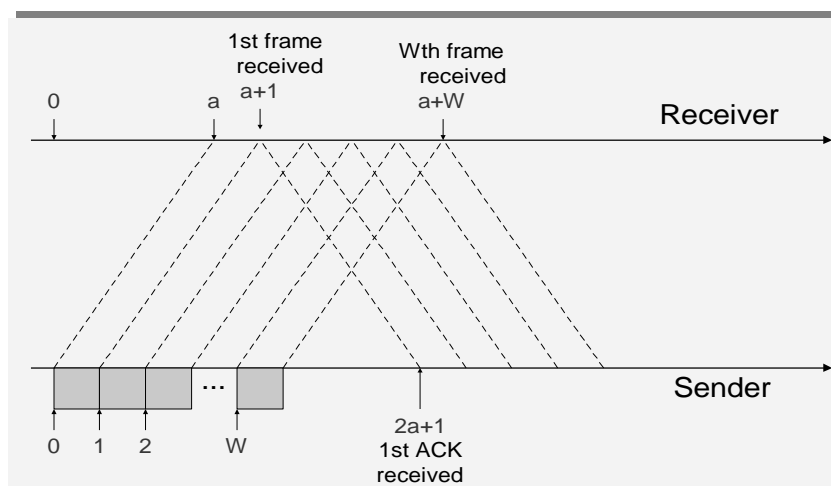
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## Analysis of Sliding Windows

### ■ Define:

- We use the same parameters for as in Stop-and-Wait
- To simplify notation we set:
 
$$\begin{aligned} F/C &= 1 \\ l &= a \end{aligned} \quad (\text{Normalization})$$
- $W$  = Maximum window size (identical for sender and receiver)

## Analysis of Sliding Windows



## Analysis of Sliding Windows

- If the window size is sufficiently large the sender can continuously transmit packets:

- $W \geq 2a+1$ : Sender can transmit continuously

$$\text{normalized efficiency} = 1$$

- $W < 2a+1$ : Sender can transmit  $W$  frames every  $2a+1$  time units

$$\text{normalized efficiency} = \frac{W}{1 + 2a}$$

## ARQ Error Control

- Two types of errors:
  - Lost frames
  - Damaged Frames
- Most Error Control techniques are based on (1) Error Detection Scheme (e.g., Parity checks, CRC), and (2) Retransmission Scheme
- Error control schemes that involve error detection and retransmission of lost or corrupted frames are referred to as **Automatic Repeat Request (ARQ)** error control

## ARQ Error Control

- All retransmission schemes use all or a subset of the following procedures:
  - Receiver sends an **acknowledgment (ACK)** if a frame is correctly received
  - Receiver sends a **negative acknowledgment (NAK)** if a frame is not correctly received
  - The sender retransmits a packet if an ACK is not received within a **timeout** interval
  - All retransmission schemes (using ACK, NAK or both) rely on the use of timers

## ARQ Error Control

- **Note:** Once retransmission is used, a sequence number is required for every data packet to prevent duplication of packets
- Both **ACKs** and **NAKs** can be sent as special frames, or be attached to data frames going in the opposite direction (**Piggybacking**)

01111110	Address	Control	Data	Checksum	01111110
----------	---------	---------	------	----------	----------

0	Send Seq.-No.	P/F	Recv Seq.-No.
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For piggybacking

## ARQ Schemes

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- The most common ARQ retransmission schemes:
  - Stop-and-Wait ARQ
  - Go-Back-N ARQ
  - Selective Repeat ARQ
- The protocol for sending ACKs in all ARQ protocols are based on the sliding window flow control scheme

## Stop-and-Wait ARQ

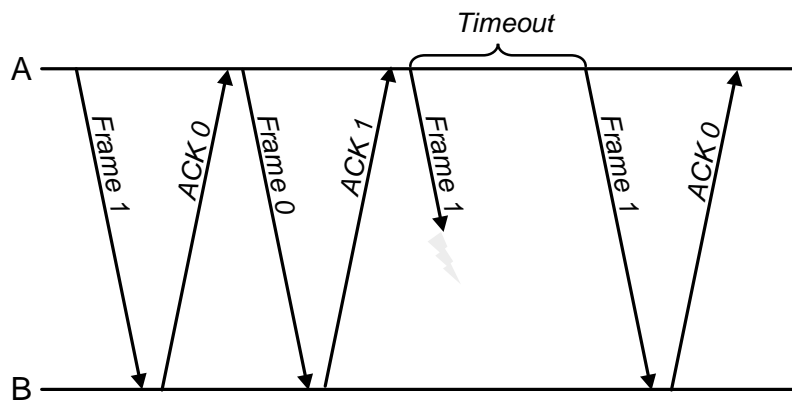
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- **Stop-and-Wait ARQ** is an addition to the Stop-and-Wait flow control protocol:
  - Frames have 1-bit sequence numbers ( $SN = 0$  or  $1$ )
  - Receiver sends an *ACK* ( $1-SN$ ) if frame  $SN$  is correctly received
  - Sender waits for an *ACK* ( $1-SN$ ) before transmitting the next frame with sequence number  $1-SN$
  - If sender does not receive anything before a timeout value expires, it retransmits frame  $SN$



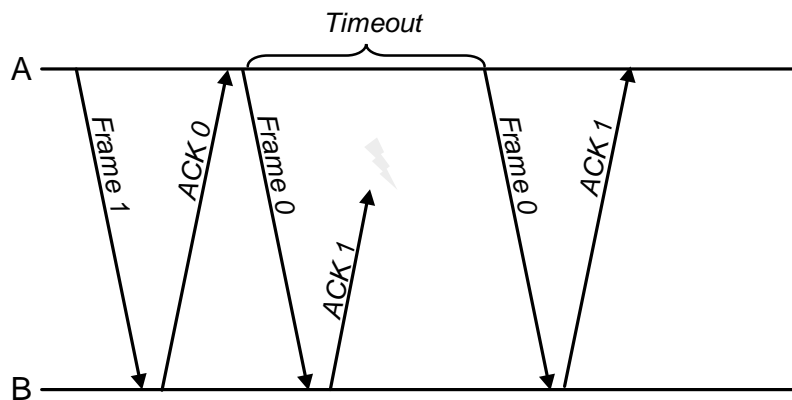
## Stop-and-Wait ARQ

### ■ Lost Frame



## Stop-and-Wait ARQ

### ■ Lost ACK



## Go-Back-N ARQ

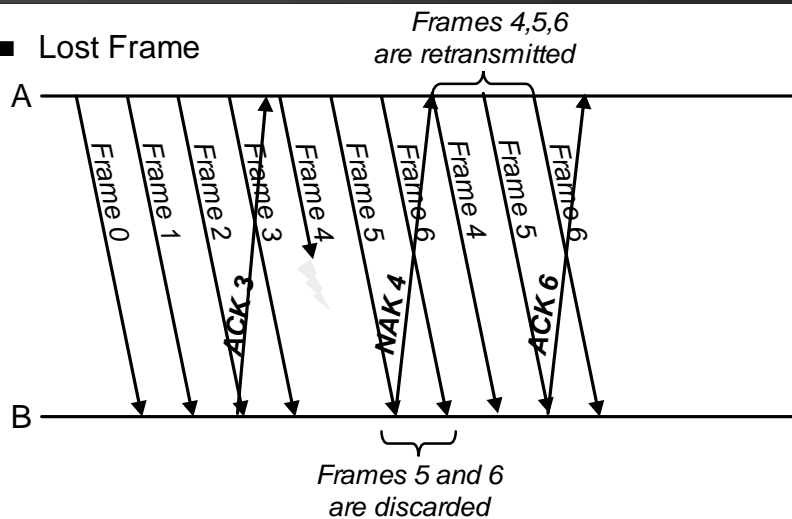
- Go-Back-N uses the sliding window flow control protocol. If no errors occur the operations are identical to Sliding Window
- Operations:
  - A station may send multiple frames as allowed by the window size
  - Receiver sends a **NAK  $i$**  if frame  $i$  is in error. *After that, the receiver discards all incoming frames until the frame in error was correctly retransmitted*
  - *If sender receives a **NAK  $i$**  it will retransmit frame  $i$  and all packets  $i+1, i+2, \dots$  which have been sent, but not been acknowledged*

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## Go-Back-N ARQ

### ■ Lost Frame

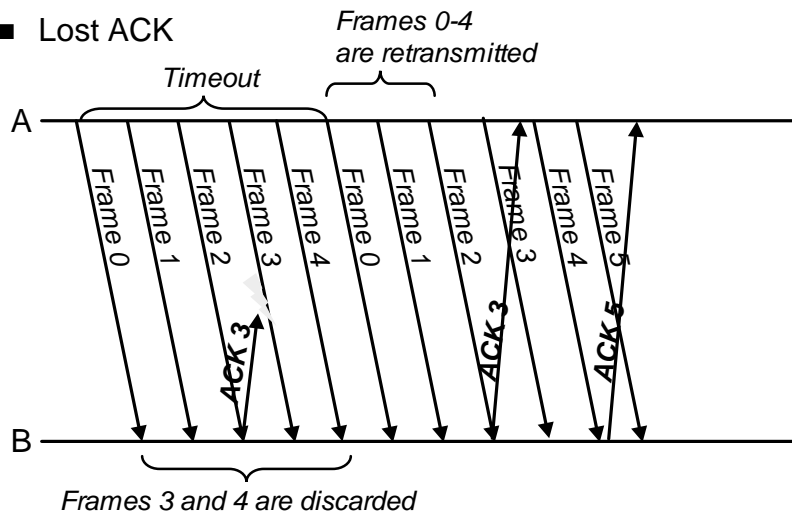


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## Go-Back-N ARQ

### ■ Lost ACK



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## Details Go-Back-N ARQ



### ■ Scenario 1:

A transmits *frame i*, and B detects error in *frame i*, but has received *frames i-1, i-2,...* correctly

→ B sends **NAK<sub>i</sub>**

### ■ Scenario 2:

*Frame i* is lost or B does not recognize *frame i*  
Assume that A sends *frame i+1* and B receives it

→ B sends **NAK<sub>i</sub>**, or A will timeout and retransmit *frame i* and all subsequent frames

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## Details Go-Back-N ARQ

Scenario 3: B receives *frame i* and sends **ACK(*i*+1)** which is lost

→ B may send an **ACK(*i*+*k*)** later which also acknowledges all frames <*i*+*k* (**ACKs** are “cumulative”)

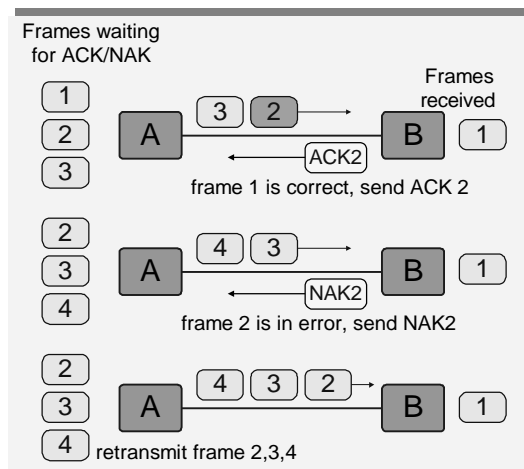
or

A retransmits *frame i* and all subsequent frames

Scenario 4: **NAK*i*** is lost

→ A will eventually time out

## Example of Go-Back-N ARQ



- In Go-back-N, if frames are correctly delivered, they are delivered in the correct sequence

- Therefore, the receiver does not need to keep track of 'holes' in the sequence of delivered frames

## Selective-Repeat ARQ

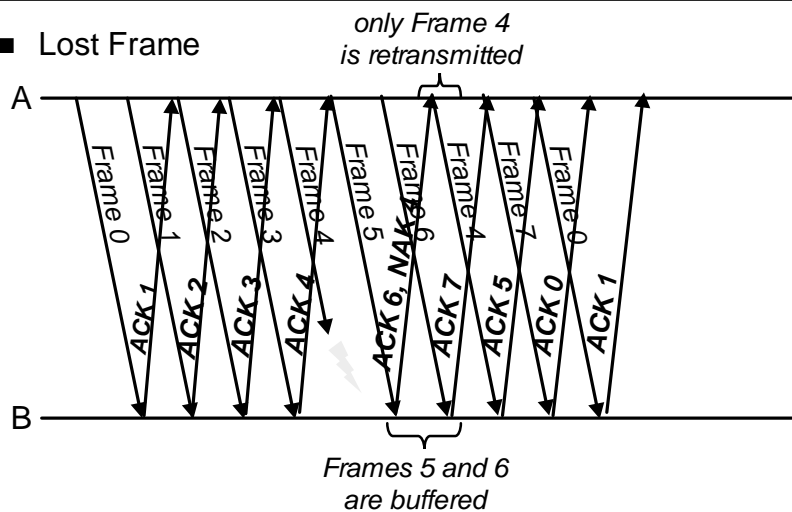
- Similar to Go-Back-N ARQ. However, the sender only retransmits frames for which a **NAK** is received
- **Advantage over Go-Back-N:**
  - Fewer Retransmissions.
- **Disadvantages:**
  - More complexity at sender and receiver
  - Each frame must be acknowledged individually (no cumulative acknowledgements)
  - Receiver may receive frames out of sequence

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## Selective-Repeat ARQ

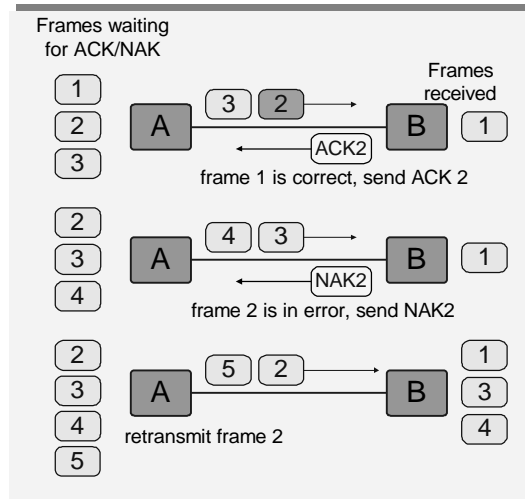
- Lost Frame



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## Example of Selective-Repeat ARQ



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- Receiver must keep track of 'holes' in the sequence of delivered frames
- Sender must maintain one timer per outstanding packet

## Analysis of ARQ Protocols

- What is the efficiency of the discussed ARQ protocols?
- A number of assumptions:
  - **ACKs** and **NAKs** are never lost, and frames are not dropped.
  - Sizes of **ACKs**, **NAKs**, and frame headers are negligible.

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## Analysis of Stop-and-Wait ARQ

### ■ Parameters:

$U$  = efficiency

$T_t = F/C$  transmission delay of a frame

$I$  = propagation delay

$a = I/T_t$

$P$  = Probability that a frame is in error

### ■ Without Errors ( $P=0$ ):

$$U = \frac{T_t}{T_t + 2I}$$

## Analysis of Stop-and-Wait ARQ

### ■ With Errors:

- Probability that  $k$  transmission attempts are needed to successfully transmit a frame

$$P[k \text{ attempts needed}] = P^{k-1} \cdot (1-P)$$

### ■ Expected number of attempts ( $=E[A]$ ):

$$E[A] = \sum_{i=1}^{\infty} i P^{i-1} \times (1-P) = \frac{1}{1-P}$$

### ■ Expected efficiency with errors

$$U = \frac{T_t}{E[A] \cdot (T_t + 2I)} = \frac{(1-P) \cdot T_t}{T_t + 2I} = \frac{1-P}{1+2a}$$

## Analysis of Go-Back-N ARQ

### Without Errors

- $W T_t > 2l + T_t$

$$U = 1$$

- $W T_t < 2l + T_t$

$$U = \frac{W}{1 + 2a}$$

### With Errors

- $W T_t > 2l + T_t$

$$U = 1 - P$$

- $W T_t < 2l + T_t$

$$U = \frac{W \cdot (1 - P)}{1 + 2a}$$

## Analysis of ARQ Protocols - Results

$$P = 10^{-3}$$



## Example DL Protocol: XModem

- **XModem** is a simple data link protocol which used to be popular for communications over modems
- **Xmodem** uses Stop-and-Wait ARQ

SOH	NUM	CNUM	Data	CKS
1byte	1	1	<=128	1

- **SOH:** frame delimiter (start of header, "00000001")
- **NUM:** 8-bit sequence number
- **CNUM:** bitwise complement of NUM
- **Data:** up to 128 bytes
- **CKS:** checksum = sum of the data field without overflow bit

## XModem

- **NAK:** "00010101" sent every 15 sec when data is not received
- **ACK:** "00000110" sent if CKS is correct
- **EOT:** "00000100" end of transmission
- **Variations of XModem:**
  - XModem-CRC : uses CRC
  - YModem: allows to send 1,024 bytes of data in a frame. Also: allows batch file transfers
  - ZModem