

Gradient Descent

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import numpy as np

def gradient_descent(X, y, learning_rate, num_iterations):
    num_samples, num_features = X.shape
    theta = np.zeros(num_features) # Initialize theta with zeros

    for _ in range(num_iterations):
        # Calculate predictions using current theta
        predictions = np.dot(X, theta)

        # Calculate the error between predictions and actual values
        error = predictions - y

        # Calculate the gradient
        gradient = np.dot(X.T, error) / num_samples

        # Update theta using gradient and learning rate
        theta -= learning_rate * gradient

    return theta

# Example usage
# Generate some random data for demonstration
np.random.seed(42)
num_samples = 100
num_features = 2
X = np.random.rand(num_samples, num_features)
true_theta = np.array([2, 3])
y = np.dot(X, true_theta) + np.random.normal(0, 0.1, num_samples)

learning_rate = 0.01
num_iterations = 1000
learned_theta = gradient_descent(X, y, learning_rate, num_iterations)

print("True theta:", true_theta)
print("Learned theta:", learned_theta)
```

```
True theta: [2 3] Learned theta: [2.21400966 2.79279662]
```

```

import numpy as np

def stochastic_gradient_descent(X, y, learning_rate, num_epochs):
    num_samples, num_features = X.shape
    theta = np.zeros(num_features) # Initialize theta with zeros

    for _ in range(num_epochs):
        for i in range(num_samples):
            # Choose a random sample
            random_index = np.random.randint(num_samples)
            xi = X[random_index]
            yi = y[random_index]

            # Calculate prediction for the current sample
            prediction = np.dot(xi, theta)

            # Calculate the error for the current sample
            error = prediction - yi

            # Calculate the gradient for the current sample
            gradient = xi * error

            # Update theta using gradient and learning rate
            theta -= learning_rate * gradient

    return theta

# Example usage
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np.random.seed(42)
num_samples = 100
num_features = 2
X = np.random.rand(num_samples, num_features)
true_theta = np.array([2, 3])
y = np.dot(X, true_theta) + np.random.normal(0, 0.1, num_samples)

learning_rate = 0.01
num_epochs = 100
learned_theta = stochastic_gradient_descent(X, y, learning_rate, num_epochs)

```

```
print("True theta:", true_theta)
print("Learned theta:", learned_theta)
```

```
True theta: [2 3] Learned theta: [2.02047617 3.01444191]
```