Gauss Jordan

$$Q1 y+z=2, 2x+3z=5, x+y+z=3$$

In[161]:=
$$a = \{\{0, 1, 1, 2\}, \{2, 0, 3, 5\}, \{1, 1, 1, 3\}\};$$

 $a \parallel MatrixForm$

Out[162]//MatrixForm=

$$\begin{pmatrix} 0 & 1 & 1 & 2 \\ 2 & 0 & 3 & 5 \\ 1 & 1 & 1 & 3 \end{pmatrix}$$

In[163]:= RowReduce[a] // MatrixForm

Out[163]//MatrixForm=

$$\left(\begin{array}{cccc}
1 & 0 & 0 & 1 \\
0 & 1 & 0 & 1 \\
0 & 0 & 1 & 1
\end{array}\right)$$

Solve[
$$\{x == 1, y == 1, z == 1\}, \{x, y, z\}$$
]

Out[164]=

$$\{\{x\rightarrow 1,\;y\rightarrow 1,\;z\rightarrow 1\}\}$$

$$Q2 x+y+z=1, 4x+3y-z=6, 3x+5y+3z=4$$

Out[166]//MatrixForm=

$$\begin{pmatrix} 1 & 1 & 1 & 1 \\ 4 & 3 & -1 & 6 \\ 3 & 5 & 3 & 4 \end{pmatrix}$$

In[177]:= RowReduce[b] // MatrixForm

Out[177]//MatrixForm=

$$\begin{pmatrix} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & \frac{1}{2} \\ 0 & 0 & 1 & -\frac{1}{2} \end{pmatrix}$$

$$ln[178]:=$$
 Solve[{x == 1, y == 1/2, z == -1/2}, {x, y, z}]

Out[178]=

$$\left\{ \left\{ x \to 1, \ y \to \frac{1}{2}, \ z \to -\frac{1}{2} \right\} \right\}$$

 $In[169]:= c = \{\{2, 1, 1, -2, -10\}, \{4, 0, 2, 1, 8\}, \{3, 2, 2, 0, 7\}, \{1, 3, 2, -1, -5\}\};$ c // MatrixForm

Out[170]//MatrixForm=

$$\begin{pmatrix} 2 & 1 & 1 & -2 & -10 \\ 4 & 0 & 2 & 1 & 8 \\ 3 & 2 & 2 & 0 & 7 \\ 1 & 3 & 2 & -1 & -5 \end{pmatrix}$$

In[171]:= RowReduce[c] // MatrixForm

Out[171]//MatrixForm=

$$\begin{pmatrix}
1 & 0 & 0 & 0 & 5 \\
0 & 1 & 0 & 0 & 6 \\
0 & 0 & 1 & 0 & -10 \\
0 & 0 & 0 & 1 & 8
\end{pmatrix}$$

$$ln[172]:=$$
 Solve[{x == 5, y == 6, z == -10, w == 8}, {x, y, z, w}]

Out[172]=

$$\{\{x \to 5, y \to 6, z \to -10, w \to 8\}\}\$$

Q4
$$3x+3y+4z=20$$
, $2x+y+3z=13$, $x+y+3z=6$

$$In[173]:= d = \{\{3, 3, 4, 20\}, \{2, 1, 3, 13\}, \{1, 1, 3, 6\}\};$$

 $d \text{ // MatrixForm}$

Out[174]//MatrixForm=

$$\begin{pmatrix} 3 & 3 & 4 & 20 \\ 2 & 1 & 3 & 13 \\ 1 & 1 & 3 & 6 \end{pmatrix}$$

In[175]:= RowReduce[d] // MatrixForm

Out[175]//MatrixForm=

$$\begin{pmatrix} 1 & 0 & 0 & 7 \\ 0 & 1 & 0 & \frac{1}{5} \\ 0 & 0 & 1 & -\frac{2}{5} \end{pmatrix}$$

$$ln[176]:=$$
 Solve[{x == 7, y == 1/5, z == -2/5}, {x, y, z}]

Out[176]=

$$\left\{ \left\{ x \to 7, \ y \to \frac{1}{5}, \ z \to -\frac{2}{5} \right\} \right\}$$