

Secant Method

Q1 $f(x) = x^3 + 2x^2 - 3x - 1$

In[7]:=

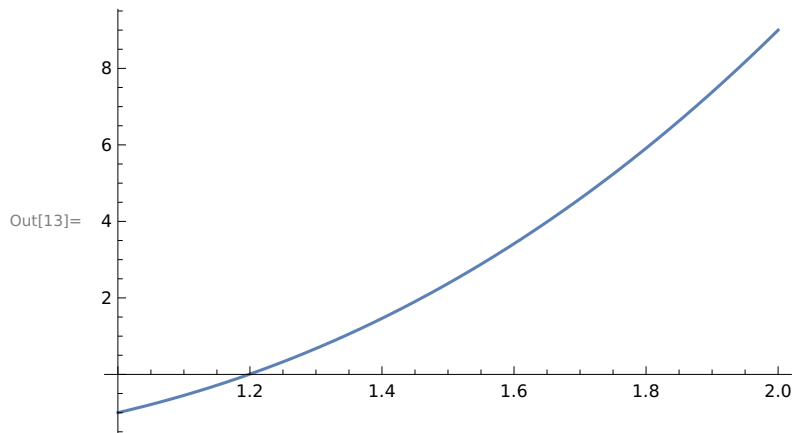
```
f[x_] := x^3 + 2 x^2 - 3 x - 1
```

In[8]:=

```
Subscript[P, 0] = 2;  
Subscript[P, 1] = 1;  
ϵ = 0.000005;  
Nmax = 10;  
For[n = 2, n ≤ Nmax, n++,  
Subscript[P, n] =  
  N[Subscript[P, n - 1] - (f[Subscript[P, n - 1]] * (Subscript[P, n - 1] - Subscript[P, n - 2]) /  
    (f[Subscript[P, n - 1]] - f[Subscript[P, n - 2]]))];  
If[Abs[Subscript[P, n] - Subscript[P, n - 1]] < ϵ, Return[Subscript[P, n]]];  
Print[n - 1, "th iteration value is ", Subscript[P, n]];  
Print["estimated error is :", Abs[Subscript[P, n] - Subscript[P, n - 1]]];  
Plot[f[x], {x, 1, 2}]
```

1th iteration value is 1.1
 estimated error is :0.1
 2th iteration value is 1.22173
 estimated error is :0.121729
 3th iteration value is 1.19649
 estimated error is :0.0252442
 4th iteration value is 1.19865
 estimated error is :0.00216004
 5th iteration value is 1.19869
 estimated error is :0.000045968

Out[12]= 1.19869



Q2 $f(x) = e^{-x} - x$

In[32]:= **f[x_] := Exp[-x] - x**

In[33]:= **Subscript[P, 0] = 2;**

Subscript[P, 1] = 1;

$\epsilon = 0.000005;$

Nmax = 10;

For[n = 2, n ≤ Nmax, n++,

Subscript[P, n] =

N[Subscript[P, n - 1] - (f[Subscript[P, n - 1]] * (Subscript[P, n - 1] - Subscript[P, n - 2]) /
(f[Subscript[P, n - 1]] - f[Subscript[P, n - 2]]))];

If[Abs[Subscript[P, n] - Subscript[P, n - 1]] < ϵ , Return[Subscript[P, n]]];

Print[n - 1, "th iteration value is ", Subscript[P, n]];

Print["estimated error is :", Abs[Subscript[P, n] - Subscript[P, n - 1]]];

1th iteration value is 0.487142

estimated error is :0.512858

2th iteration value is 0.573076

estimated error is :0.0859347

3th iteration value is 0.56723

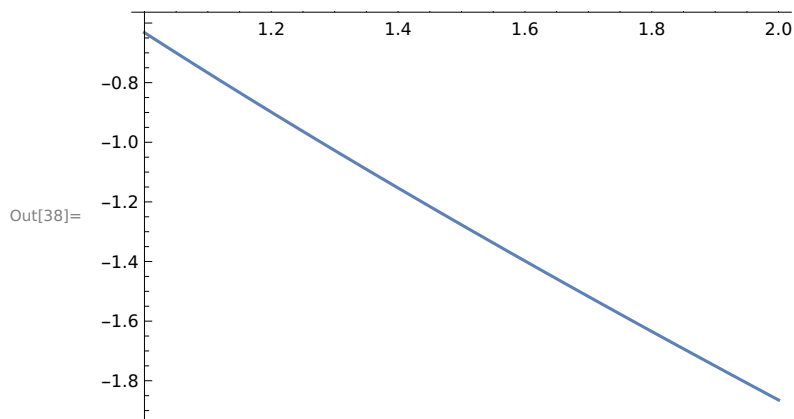
estimated error is :0.00584616

4th iteration value is 0.567143

estimated error is :0.0000869484

Out[37]= 0.567143

In[38]:= Plot[f[x], {x, 1, 2}]



Q3 $f(x)=x^3-13$

In[39]:= f[x_] := x^3 - 13

In[40]:= Subscript[P, 0] = 0;

Subscript[P, 1] = 3;

$\epsilon = 0.000005$;

Nmax = 10;

For[n = 2, n ≤ Nmax, n++,

Subscript[P, n] =

$$\frac{N[\text{Subscript}[P, n-1] - (f[\text{Subscript}[P, n-1]] * (\text{Subscript}[P, n-1] - \text{Subscript}[P, n-2]) / (f[\text{Subscript}[P, n-1]] - f[\text{Subscript}[P, n-2]]))];$$

If[Abs[Subscript[P, n] - Subscript[P, n-1]] < ϵ , Return[Subscript[P, n]]];

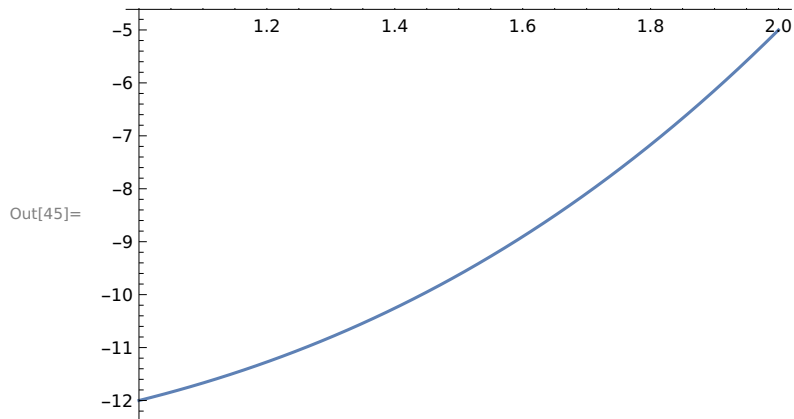
Print[n-1, "th iteration value is ", Subscript[P, n]];

Print["estimated error is :", Abs[Subscript[P, n] - Subscript[P, n-1]]];

1th iteration value is 1.44444
 estimated error is :1.55556
 2th iteration value is 2.09207
 estimated error is :0.647629
 3th iteration value is 2.49729
 estimated error is :0.405212
 4th iteration value is 2.33475
 estimated error is :0.162534
 5th iteration value is 2.35034
 estimated error is :0.0155903
 6th iteration value is 2.35134
 estimated error is :0.000999479
 7th iteration value is 2.35133
 estimated error is :7.03717 $\times 10^{-6}$

Out[44]= 2.35133

In[45]:= Plot[f[x], {x, 1, 2}]



Q 4 $f(x) = x^3 - 3x^2 + 2x + 5$

In[46]:= f[x_] := x^3 - 3 x^2 + 2 x + 5

```

In[47]:= Subscript[P, 0] = 0;
Subscript[P, 1] = -1;
 $\epsilon$  = 0.000005;
Nmax = 10;
For[n = 2, n ≤ Nmax, n++,
Subscript[P, n] =
  N[Subscript[P, n - 1] - (f[Subscript[P, n - 1]]*(Subscript[P, n - 1] - Subscript[P, n - 2]) /
    (f[Subscript[P, n - 1]] - f[Subscript[P, n - 2]]));
If[Abs[Subscript[P, n] - Subscript[P, n - 1]] <  $\epsilon$ , Return[Subscript[P, n]]];
Print[n - 1, "th iteration value is ", Subscript[P, n]];
Print["estimated error is :", Abs[Subscript[P, n] - Subscript[P, n - 1]]];

1th iteration value is -0.833333
estimated error is :0.166667
2th iteration value is -0.900277
estimated error is :0.0669437
3th iteration value is -0.904325
estimated error is :0.00404786
4th iteration value is -0.90416
estimated error is :0.000164377

```

Out[51]= -0.904161

```

In[52]:= Plot[f[x], {x, 1, 2}]

```

