Homework 4 Question 2: Voltage Smoothing

We would like to send a sequence of voltage inputs to the manipulator arm of a robot. The desired signal is shown in the plot below (also available in voltages.csv)

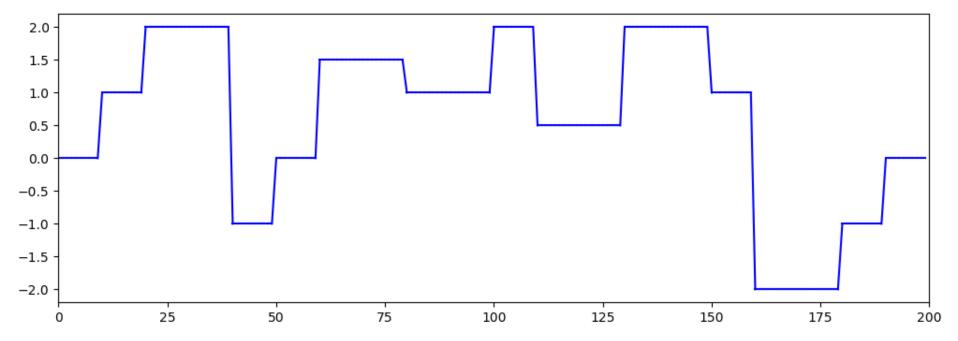
Unfortunately, abrupt changes in voltage cause undue wear and tear on the motors over time, so we would like to modify the signal so that the transitions are smoother. If the voltages above are given by $v_1, v_2, \ldots, v_{200}$, one way to characterize smoothness is via the sum of squared differences:

$$R(v) = (v_2 - v_1)^2 + (v_3 - v_2)^2 + \dots + (v_{200} - v_{199})^2$$

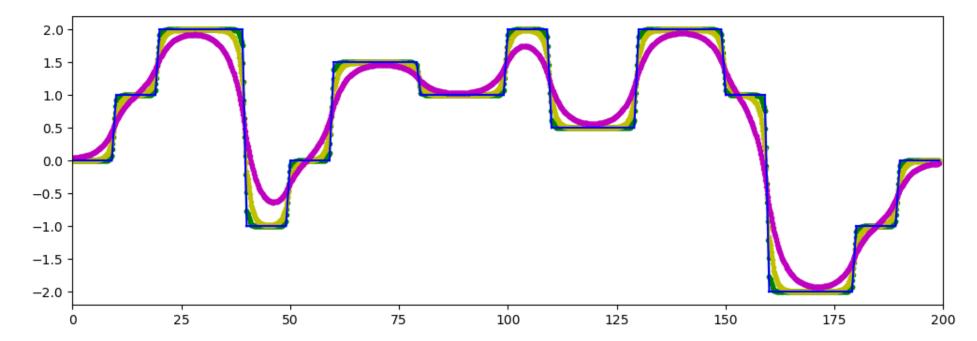
When R(v) is smaller, the voltage is smoother. Solve a regularized least squares problem that explores the tradeoff between matching the desired signal above and making the signal smooth. Explain your reasoning, and include a plot comparing the desired voltages with your smoothed voltages.

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In [7]: # Load the data file
    raw = readcsv("voltages.csv")

using PyPlot
    figure(figsize=(12,4))
    xlim(0,200)
    [plot(linspace(i-1,i,10),linspace(raw[i],raw[i+1],10),"b") for i in 1:length(raw)-1];
```



```
Objective Value:2.7044936151369257, for lambda: 0.1 Objective Value:14.310953247228213, for lambda: 1.0 Objective Value:50.14612903783541, for lambda: 10.0
```



The λ gives relative importance to minimize infidelity vs sharpness. Since smoothness is the desired property for our signal, λ is associated with sharpness. More the weight given to sharpness, more smooth the resulting voltage turns out to be and vice-versa.

The above graph has the legend is as follows (wasn't able to code it):

- Magenta line: $\lambda = 10$, This is the most smooth curve but deviates significantly from the original voltage signal because of large λ , as the objective to minimize the sharpness is more important than fidelity.
- **Yellow line**: $\lambda = 1$, This gives equal importance to both smoothness and fidelity.
- Green line: $\lambda = 0.1$, This gives more importance to fidelity than smoothness so the voltage curve looks more like the original voltage signal.
- Blue line: Is the original signal.