# Binary classifier using Support Vector Machine models

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This document provides an implementation of a binary classifier using Support Vector Machine (SVM) models. We used linear, Radial Basis Function (RBF) and Polynomial as type of kernels with a wide range of different parameters. This model is trained and tested with two out of 10 classes of the dataset of Cifar-10 which is consisted of 50.000 training samples and 10.000 testing samples all cassified in 10 groups. More details can be found on cifar website

## I. THE PREPERATION CODE

a) Firstly we are **loading** up all of the **libraries** that are required and also we are **loading** the **Cifar10** dataset in 4 arrays each corresponding to x,y training or testing data

```
import numpy as np
import time
import matplotlib.pyplot as plt
from sklearn.decomposition import PCA
from sklearn.svm import SVC
from sklearn.metrics import classification_report, accuracy_score
from sklearn.preprocessing import StandardScaler
from keras.datasets import cifar10

# Load CIFAR-10 into our programm
(x_train, y_train), (x_test, y_test) = cifar10.load_data()
```

b) After that, we are creating a "labels" numpy array to make our project more general in case the user wants to pick 2 other classes of his choice. Also we are picking correspondingly to "labels" array the desired 2 classes. For the purposes of this document we picked the worst case scenario that cifar10 can provide which is classification of "Dog" and "Cat". Finally we are filtering out the data that contains the two classes we need and combining them into x train, test and y train, test arrays

```
# Class labels in CIFAR-10 dataset to make the project more general
labels = ['airplane', 'automobile', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', 'ship', 'truck']
# Select the two desired classes
class_1, class_2 = 3, 5
mask_train = (v_train.flatten() == class_1) | (v_train.flatten() == class_2)
mask_test = (v_test.flatten() == class_1) | (v_test.flatten() == class_2)
x_train, y_train = x_train[mask_train], y_train[mask_train]
x_test, y_test = x_test[mask_test], y_test[mask_test]
```

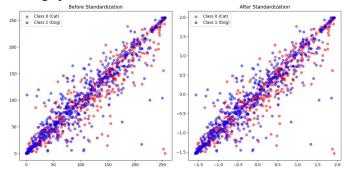
c) In this step we are **relabeling** y\_train and y\_test to 0 and 1 instead of 4 and 6 for simplicity reasons. Also we are **reshaping** our data to match the desired format that is set from Scikit learn library for SVM models.

```
# Relabel classes to 0 and 1
y_train = (y_train.flatten() == class_2).astype(int)
y_test = (y_test.flatten() == class_2).astype(int)

# Reshaping our data to fit sckit learn SVM requirments
x_train_flat = x_train.reshape(x_train.shape[0], -1)
x_test_flat = x_test.reshape(x_test.shape[0], -1)
```

## d) Standardizing dataset

In this step, we are rescaling our data to have a mean of zero and a variance of . To do that, for each element we are subtracting the mean and dividing the result by the variance. In that way our data get values between -1.5 and 2 as shown in the below graph



## e) Principal Component Analysis (PCA)

Lastly, we are applying principal component analysis (or known as PCA) where we are lowering our dataset dimensions from 3072 to 88 without loosing more than 10% of information in order to speed up training and reduce computational complexity .

```
Before PCA
X_train: (10000, 3072)
X_test: (2000, 3072)

After PCA
X_train: (10000, 88)
X_test: (2000, 88)
```

#### II. KERNELS

#### A) Linear kernel

#### Results

In that model, we chose to implement an SVM with a linear kernel while we used different values of C, which controls the trade-off between maximizing the margin and minimizing classification errors. As shown in the below pictures, the values of C we chose were 0.1 and 1. Even though C is getting bigger we are not having any significant increments on either training and testing accuracy as we expected, because our classes are not linearly separable. The best testing accuracy we achieved was 61.15% at 328.12 seconds

```
SVM Classification Report with C: 0.1:
Training accuracy: 61.339999999999996%
Test accuracy: 61.0%
Execution time: 59.21244 seconds

SVM Classification Report with C: 1:
Training accuracy: 61.3%
Test accuracy: 61.1500000000000006%
Execution time: 328.12970 seconds
```

#### Code

The code for linear kernel impmentation was pretty simple as scikit learn library provides all the required tools to declare a linear model using SVC() function, train it using the .fit() function and extracting the results using .predict() function. We also needed to run the model for various values of C, thats why we are declaring an array C in the beginning and using a for loop for each of its elements. Finallym the .perf\_counter() helped us to calculate the execution time for each model

```
for i in C:
    start_time = time.perf_counter()
    svm_model = SVC(kernel='linear', C=i)
    svm_model.fit(x_train_pca, y_train)
    y_pred_train = svm_model.predict(x_train_pca)
    y_pred = svm_model.predict(x_test_pca)
    end_time = time.perf_counter()
    execution_time = end_time - start_time

    print(f"\nsvM classification Report with C: {i}:")
    print(f"Training accuracy: {accuracy_score(y_train, y_pred_train)*100}%")
    print(f"Test_accuracy: {accuracy_score(y_test, y_pred)*100}%")
    print(f"Execution_time: {execution_time:.5f} seconds")
```

## B) Polynomial kernel

## Results

In that part of our project we implemented an SVM with polynomial kernel following the formula  $(\gamma * x^Ty + r)^d$  where d is the degree of the polynomial and  $\gamma$  (gamma) is the scaling factor. The parameter C was chosen to take discrete values  $10^{-3}, 10^{-2}, 10^{-1}$  and 1 while  $\gamma$  and d took values 0.001, 0.01, 0.1, 1, 10 and 2, 3, 4 respectively. The results for each machine are shown below:

```
von classification Report with C: 0.01, gama: 0.01, degree: 2: relating accuracy: 53-05.

restriction line: 17.0903 seconds

restriction line: 17.0903 seconds

restriction line: 17.0903 seconds

restriction control separate with C: 0.001, gama: 0.001, degree: 2: restriction line: 17.0903 seconds

von Classification Report with C: 0.001, gama: 0.001, degree: 2: relating accuracy: 93-008

restriction line: 17.0403 seconds

von Classification Report with C: 0.001, gama: 0.001, degree: 2: relating accuracy: 93-008

restriction line: 17.0407 seconds

von Classification Report with C: 0.001, gama: 0.001, degree: 2: relating accuracy: 93-008

restriction line: 15.04097 seconds

von Classification Report with C: 0.001, gama: 0.01, degree: 1: relating accuracy: 93-008

restriction line: 15.04097 seconds

von Classification Report with C: 0.001, gama: 0.01, degree: 1: relating accuracy: 93-008

restriction line: 15.04097 seconds

von Classification Report with C: 0.001, gama: 0.01, degree: 1: relating accuracy: 93-008

restriction line: 15.04097 seconds

von Classification Report with C: 0.01, gama: 0.01, degree: 1: relating accuracy: 93-008

restriction line: 15.04097 seconds

von Classification Report with C: 0.01, gama: 0.01, degree: 1: relating accuracy: 93-008

restriction line: 15.04097 seconds

von Classification Report with C: 0.01, gama: 0.1, degree: 1: relating accuracy: 93-008

restriction line: 13.04097 seconds

von Classification Report with C: 0.01, gama: 0.1, degree: 1: relating accuracy: 93-008

restriction line: 13.04097 seconds

von Classification Report with C: 0.01, gama: 0.1, degree: 1: relating accuracy: 93-008

restriction line: 13.04097 seconds

von Classification Report with C: 0.01, gama: 0.1, degree: 1: relating accuracy: 93-008

restriction line: 13.04097 seconds

von Classification Report with C: 0.01, gama: 0.1, degree: 1: relating accuracy: 93-008

restriction line: 13.04097 seconds

von Classification Report with C: 0.01, gama: 0.1, degree: 1: relating accuracy: 93-008

restriction line: 1
```

Training accuracy: 78.18% [retting accuracy: 63.0% Execution time: 17.54466 seconds
Execution time: 17.54466 seconds
Training accuracy: 97.45% [retting accuracy: 97.45% [retting accuracy: 60.7% [retting accuracy: 60.7% [retting accuracy: 60.7% [retting accuracy: 90.80% [retting accuracy: 90.80% [retting accuracy: 90.80% [retting accuracy: 90.60% [retting

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degree: Execution
SM class
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SM Class
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SM Class
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SM Class
Training
Testing;
Execution

Training accuracy: 00.0%
lesting accuracy: 00.0%
execution time: 10.00003 seconds

NM Classification Report with C: 0.1, gamma: 0.001, degree: 3:
Training accuracy: 85.0%
execution time: 18.00013 seconds

NM Classification Report with C: 0.1, gamma: 0.001, degree: 4:
Training accuracy: 03.0%
execution time: 17.00703 seconds

NM Classification Report with C: 0.1, gamma: 0.01, degree: 2:
Training accuracy: 03.0%
Execution time: 97.78000 seconds

NM Classification Report with C: 0.1, gamma: 0.01, degree: 2:
Training accuracy: 03.0%
Execution time: 97.78000 seconds

NM Classification Report with C: 0.1, gamma: 0.01, degree: 3:
Training accuracy: 03.000
Execution time: 95.12000 seconds

NM Classification Report with C: 0.1, gamma: 0.01, degree: 3:
Training accuracy: 100.000

NM Classification Report with C: 0.1, gamma: 0.01, degree: 4:
Training accuracy: 100.000

NM Classification Report with C: 0.1, gamma: 0.01, degree: 4:
Training accuracy: 100.000

Testing accuracy: 100.000

Testi

C = 0.1

From these results we can

observe that the higher the values of C,  $\gamma$  and d the higher the possibility the difference between training accuracy and test accuary is big, which leads to overfitting. For example, by setting C=  $10^{-3}$  while keeping gamma at either  $10^{-3}$  or  $10^{-2}$  and degree at 2 we are getting a balanced model. But if we set the value of gamma at  $10^{-1}$  the model overfits immediately. The same applies for gamma =  $10^{-2}$  and a degree of 3 or higher class. Also we can observe from the other 3 figures that when C gets higher our model gets more strict in the increament of the other 3 parameters before it overfits.

The execution time for each model that didn't overfit is around 14 to 17 seconds while the ones who overfit are having a wide range between 16 to 56

In conclusion, the best testing accuracy we achieved preventing our model from overfitting is **61.25%** by setting  $C = 10^{-1}$ ,  $\gamma = 10^{-3}$  and d=2 with an execution time of around **15 seconds** 

#### Code

Similarly to linear kernel, scikit learn library provides all the required functions to implement a polynomial kernel SVM model. We also used nested for loops to produce different models with a wide range of values for each parameter

```
C = [0.001, 0.01, 0.1, 1]
G = [0.001, 0.01, 0.1, 1, 1]
G = [0.001, 0.01, 0.1, 1, 1, 1]
G = [0.001, 0.01, 0.1, 1, 1, 1]
GOERE = [2, 3, 4]  # Add degrees for the polynomial kernel
for 1 in C:
    for j in G:
    for d in DIGMES:
        star Lime: time, perf counter()
        svm_model = DK(kernel=poly', gammarj, C=i, degree=d)
        svm_model.fit(x_train.pea, y_train)
        y_train.pred = svm_model.predict(x_train.pea)
        train.pred = svm_model.predict(x_train.pea)
        train.pred = svm_model.predict(x_train.pred)
        y_pred = svm_model.predict(x_tra
```

#### c) Radial basis Function (RBF) kernel

## Results:

In that case, we implemented an SVM model using Radial basis function as kernel with a formula the below formula:  $K(xi,xj)=\exp(-\gamma\|xi-xj\|^2)$  where  $\gamma$  determines the spread of the kernel. The parameter C and  $\gamma$  was chosen to take discrete values  $10^{-5},10^{-4},10^{-3},10^{-2}$  and  $10^{-1}$ . The results for each machine are shown below:

```
ONE Clearification Report with C1 ie-05, games 1e-05; 
Training Accuracy; 58-126 
Training Accuracy; 58-126 
Training Accuracy; 58-126 
Training Accuracy; 58-126 
Training Accuracy; 59-135 
Carection Line: 22-0509 seconds 
One Clearification Report with C1 ie-05, games: 0.0001; 
Training Accuracy; 59-526 
Training Accuracy; 59-526 
Training Accuracy; 58-726 
Training Accuracy; 59-726 
Training Accuracy; 59-726 
Teacting Ac
```

C=0.00001

```
OWN CLASSIFICATION Report with C. 0.4001, games: 10-05; Trabalan Accessing 9-55.

Trabalan Accessing 9-55.

Trabalan Accessing 9-55.

See Classification Report with C. 0.4001, games: 0.4001; Trabalan Accessing 9-93.

Texting Accessing 9-93.

Texting Accessing 9-93.

Texting Accessing 9-93.

Texting Accessing 9-93.

See Classification Report with C. 0.4001, games: 0.4001; Trabalan Accessing 9-93.

See Classification Report with C. 0.4001, games: 0.401; Trabalan Accessing 9-56.

See Classification Report with C. 0.4001, games: 0.401; Trabalan Accessing 1-10-000; Trabalan Accessing 1-10-0000; Trabalan Accessing 1-10-0000; Trabalan Accessing 1-10-000
```

C=0.0001

```
OWC Classification Report with C: 0.001, gamma: 1e-05; training Accuracy: 36.20% [Festing Accura
```

```
C=0.001
```

```
own classification (sport with c: 0.01, gamma: 1e-05: training Accuracy: 38.26% Testing Accuracy: 38.26% Testing Accuracy: 38.26% Securion times: 27.5667 Securion time: 27.5667 Securion Securion times: 29.5667 Securion Securior Securior
```

```
C=0.01
```

```
Own Classification Report with C. 0.1, games in CO. Testing Accounty Volume Classification (Accounty Volume Classification Classification Report with Co. 0.1, games 0.0001) and Classification Report with Co. 0.1, games 0.0001 recting Accounty Classification Report with Co. 0.1, games 0.0001 recting Accounty Co. 0.0007 seconds Unit Co. 0.0007 seconds Classification Report with Co. 0.1, games 0.0001 relating Accounty Co. 0.0007 seconds Classification Report with Co. 0.1, games 0.0011 relating Accounty Unit Co. 0.0007 seconds Unit
```

<u>In conclusion</u>, from these results we can clearly see that no matter the value of C, our model overfits for gamma equal or higher than  $10^{-2}$  as the training accuracy reaches 100%. The best test accuracy we achieved in a balanced model (without overfitting or underfitting) is **61.95%** with C=0.1 and gamma= $10^{-4}$  at **21.8 seconds** 

## <u>Code</u>

Similarly to the two previous kernel, scikit learn library provides all the required functions to implement a polynomial kernel SVM model. We also used nested for loops to produce different models for different values of C and  $\gamma$ 

```
C = [0.00001, 0.0001, 0.001, 0.01, 0.1]
GAMMA = [0.00001, 0.0001, 0.001, 0.01, 0.1]

for i in C:
    for j in GAMMA:
        start_time = time.perf_counter()
        svm_model = SVC(kernel='rbf', gamma=j, C=i)
        svm_model.fit(x_train_pca, y_train)
        y_train_pred = svm_model.predict(x_train_pca)
        train_accuracy = accuracy_score(y_train, y_train_pred)
        y_pred = svm_model.predict(x_test_pca)
        test_accuracy = accuracy_score(y_test, y_pred)
        end_time = time.perf_counter()
        execution_time = end_time - start_time

    print(f"\nsvM Classification Report with C: {i}, gamma: {j}:")
    print(f"Training Accuracy: {train_accuracy * 100:.2f}%")
    print(f"Testing Accuracy: {test_accuracy * 100:.2f}%")
    print(f"Execution time: {execution_time:.5f} seconds")
```

## III. EXAMPLES OF RIGHT AND WRONG CLASSIFICATION

Correctly Classified (Dog) Real: 1, Predicted: 1



Fig 1: Right class using **linear** kernel  $C=10^{-1}$ 

Real: 1. Predicted: 0

Wrongly Classified (Dog)



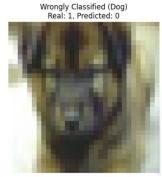


Fig2: Wrong class using **linear** kernel  $C=10^{-1}$ 

## IV. VS MLP NETWORK

In that section we are comparing our SVM models with a multilayer perceptron neural network (MLP) with one hidden layer which uses hinge loss to calculating the training loss. We produced an initial model using ChatGPT and used it as a starting point to produce our model.

## A) Code explanation

First of all, we are loading up the set of libraries we are willing to use and creating our model. The first layer is an input layer with an input shape equal to the shape of x train pca extracted by the first cell, a hidden layer of 256 neurons (each using a leaky relu as an activation function) and an output layer of one neuron using softmax as an activation function

```
yReLU(alpha=0.01),
e(1, activation='sigmoid')
```

Then, we are setting up our training parameters choosing "Adam" as optimizer with a learning rate of 10<sup>4</sup> and a "hinge loss" to calculate the loss.

```
nodel.compile(optimizer=Adam(learning_rate=0.0001), loss=hinge, metrics=['accuracy'])
```

From there, we are ready to train our model using a variable learning rate and running it for 25 epochs with a batch size equal to 32. Finally, we are printing out the required info for each epoch and our final model accuracy.

## B)Writers adjusments

The initial ChatGPT's model was lead to overfitting really fast and with a bad accuracy around 50%. In order to improve that we chose to tweak or add a lot of parameters which are shown below:

- Replaced SGD optimizer with Adam
- Added 256 neurons instead of initial 64 for more precise calculation and used Leaky relu instead of **relu** to prevent some neurons to remain 0
- In the output layer we chose to use Softmax activation function instead of linear which rised significantly our models accuracy
- Replaced the initial learning rate of 0.01 with a variable one that starts from 10<sup>-4</sup> and reduced by 25% after 8th epoch while we also reduced by half the epochs from 50 to 25. In that way we avoided overfiting on the training process.

By making the above tweaks we eliminated overfiting and achieved a test accuracy around 62.85% in 19.9 seconds of training time as shown below. This MPL model is better than all of the previous SVM models

Epoch 1/25											
313/313	1s 2ms/st	ep - accura			0.9881	<ul> <li>val_accuracy:</li> </ul>		val_loss:		learning_rate:	1.0000e-04
Epoch 2/25											
313/313	1s 2ms/st	ep - accura				<ul> <li>val_accuracy:</li> </ul>	0.6005 -	val_loss:	0.9098 -	learning_rate:	1.0000e-04
Epoch 3/25											
	1s 2ms/st		cy: 0.6132		0.8982	<ul><li>val_accuracy:</li></ul>	0.6060 -	val_loss:	0.9016 -	learning_rate:	1.0000c-04
Epoch 4/25											
	1s 2ms/st	ep - accura	cy: 0.6316		0.8811	<ul> <li>val_accuracy:</li> </ul>	0.6100 -	val_loss:	0.8974 -	learning_rate:	1.00000-04
Epoch 5/25											
	1 <b>s</b> 2ms/st		cy: 0.6303		0.8955	<ul> <li>val_accuracy:</li> </ul>	0.6115 -	val_loss:	0.8935 -	learning_rate:	1.0000e-04
Epoch 6/25											
	1s 2ms/st		су: 0.6460		0.8752	<ul><li>val_accuracy:</li></ul>	0.6145 -	val_loss:	0.8909 -	learning_rate:	1.0000e-04
Epoch 7/25											
	is 2ms/st	ep - accura	cy: 0.6570		0.8626	<ul><li>val_accuracy:</li></ul>	0.6175 -	val_loss:	0.8886 -	learning_rate:	1.0000e-04
Epoch 8/25											
	1s 2ms/st	ep - accura	су: 0.6682		0.8571	<ul><li>val_accuracy:</li></ul>	0.6175 -	val_loss:	0.8877 -	learning_rate:	1.0000e-04
Epoch 9/25											
	1s 2ms/st	ep - accura	су: 0.6633		0.8443	<ul> <li>val_accuracy:</li> </ul>	0.6190 -	val_loss:	0.8870 -		1.0000e-04
Epoch 10/25											
	is 2ms/st	ep - accura	cy: 0.6718		0.8556	<ul> <li>val_accuracy:</li> </ul>	0.6195 -	val_loss:	0.8858 -	learning_rate:	7.5000e-05
Epoch 11/25											
	1s Zms/st	ep - accura	cy: 0.6757		0.8409	<ul> <li>val_accuracy:</li> </ul>	0.6180 -	val_loss:	0.8858 -		7.5000e-05
Epoch 12/25 313/313											
	15 ZMS/ST	ep - accura	су: ө.6699	- 1055:	0.8484	<ul> <li>vai_accuracy:</li> </ul>	0.61/5 -	vai_ioss:	0.8846 -		7.50000-05
Epoch 13/25											
 Epoch 25/25											
	to Sector		0 7204		0.0017		0.6205	unl losse	0.0753	learning rate:	7 5000- 05
Training time: 19.93 seconds	LS ZMS/SU	ep - accura	.y. 0.7284		0.801/	- vai_accuracy:		vai_1055:		rearning_rate:	7.30000-05
Model Accuracy, 63 064											

# V. VS CNN AND KNN

In that section of the project we are comparing our SVM model outputs with the ones we executed in a previous project for Nearest Centroid Classifier (NCC) and K-Nearest Neighbors (KNN). We tweaked a bit the code to apply only for the two desired classes of our dataset (Cad and Dog) and not for all the classes. The results are shown below:

```
KNN (k=1) Accuracy: 0.5895

KNN (k=1) Execution Time: 0.0871 seconds

KNN (k=3) Accuracy: 59.6000%

KNN (k=3) Execution Time: 0.0543 seconds

NCC Accuracy: 57.9000%

NCC Execution Time: 0.0274 seconds
```

<u>In conclusion</u> as the accuracy for each model is 57.9% and 59.6% our SVM model remains better with an exchange of execution time