

Red indicates the unsorted segment of the array.

SelectionSort Average and Worst $O(n^2)$

4 5 2 3 1

1 5 2 3 4

1 2 5 3 4

1 2 3 5 4

1 2 3 4 5

InsertionSort Average $O(n^2)$ and Worst $O(n^2)$

4 5 2 3 1

4 5 2 3 1

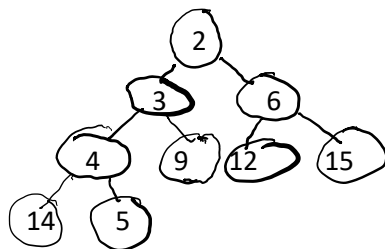
2 4 5 3 1

2 3 4 5 1

1 2 3 4 5

Heap-sort

9 6 5 14 4 12 15 3 2



9 6 5 14 4 12 15 3 2

parent = $i/2$; left = $i*2$; right = left+1

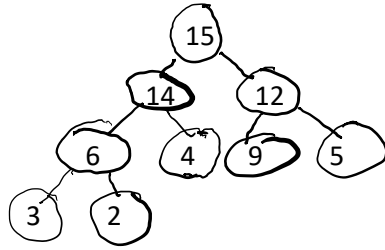
After inserting into the Priority Queue

	2	3	6	4	9	12	15	14	5	
0	1	2	3	4	5	6	7	8	9	10

	6	9	12	14	15					
0	1	2	3	4	5	6	7	8	9	10

2 3 4 5

We need a max-heap to sort into ascending order in the Heap-Sort.



9 6 5 14 4 12 15 3 2

parent = $i/2 - 1$; left = $i*2+1$; right = left+1

9	6	5	14	4	12	15	3	2		
0	1	2	3	4	5	6	7	8	9	10

After buildHeap

15	14	12	6	4	9	5	3	2		
0	1	2	3	4	5	6	7	8	9	10

Now remove and swap to end of the array to Sort

9	6	5	3	4	2	12	14	15		
0	1	2	3	4	5	6	7	8	9	10

The max-heap is in indices 0-5 and the sorted elements are in indices 6-8 after first 3 times through the loop. Note that the sorted segment increases and the heap (unsorted) segment decreases until the whole array is sorted.

$\text{ceiling}(\log(n+1)) \leq h \leq n$

$\{\} \Rightarrow \{\{\}\}$

$\{1\} \Rightarrow \{\{\}\{1\}\}$

$\{1,2\} \Rightarrow \{\{\}\{1\}\{2\}\{1,2\}\}$

$\{1,2,3\} \Rightarrow \{\{\}\{1\}\{2\}\{1,2\}\{3\}\{1,3\}\{2,3\}\{1,2,3\}\}$