

Hash Tables

♦ Hash tables are a highly efficient implementation of the Dictionary ADT
■ What are its disadvantages?

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## Wholeness Statement

A dictionary allows users to assign keys to elements then to access or remove those elements by key. An ordered dictionary maintains an order relation among keys allowing access to adjacent keys while supporting efficient implementation of the dictionary ADT. Science of Consciousness: Each of us has access to the source of thought which is a field of perfect order, balance, and efficiency.

Ordered Dictionaries

News are assumed to come from a total order, i.e., the keys can be sorted.
Specification of iterator operations:
keys()
Returns an iterator of the keys in sorted order
values()
Returns the element of the items in key-sorted order
items()
Returns the (k, e) items in sorted order by key (k) of the item
What would the running time be for creating these iterators for a Lookup Table from yesterday?
Constraint is that iteration through the items must take O(n) time where n is the number of items in the dictionary

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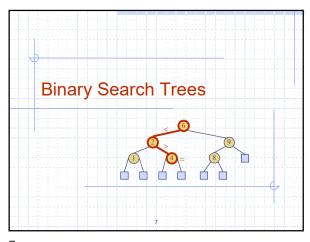
Overview

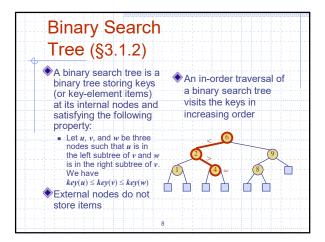
Multi-Way Search Trees (§3.3.1)

(2,4) Trees (§3.3.2)

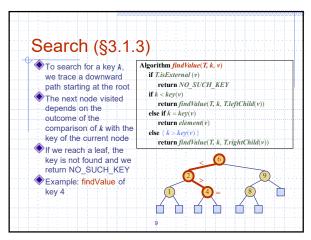
AVL Trees (§3.2)

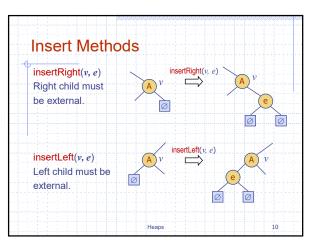
Red-Black Trees (§3.3.3) (Tomorrow)



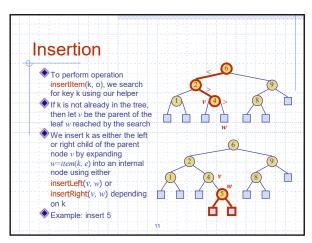


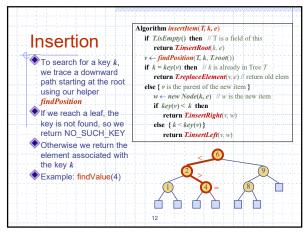
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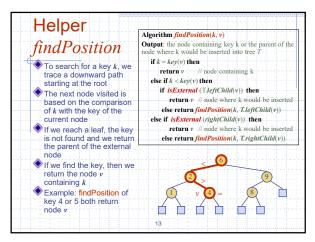


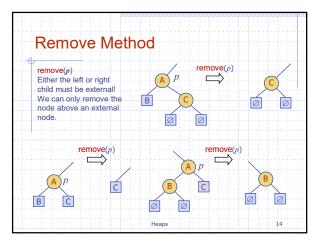
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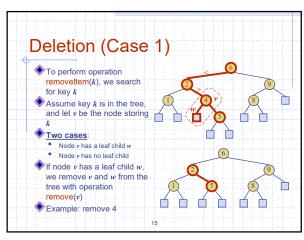


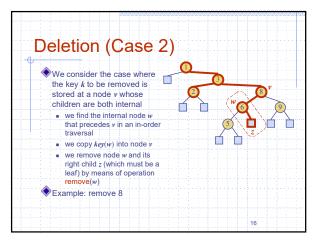


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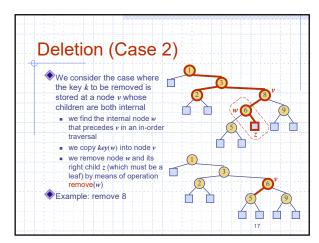


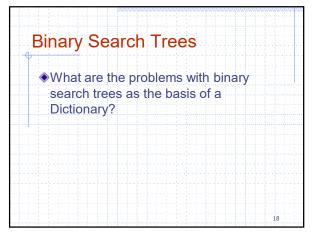




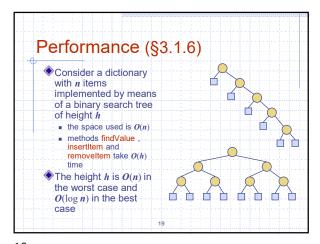


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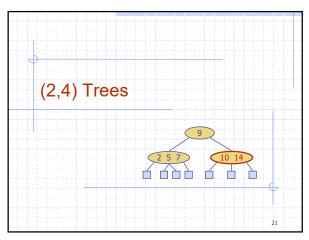


Main Point

1. A binary search tree is a binary tree with the property that the value at each node is greater than the values in the nodes of its left subtree (child) and less than the values in the nodes of its right subtree. When implemented properly, the operations (search, insert, and remove) can be efficiently accomplished in O(log n).

Such data structures reflect the following SCI principles: law of least action, principle of diving, perfect order.

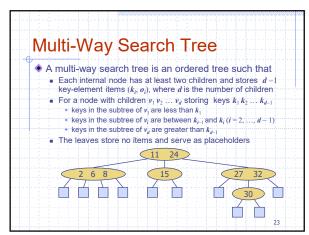
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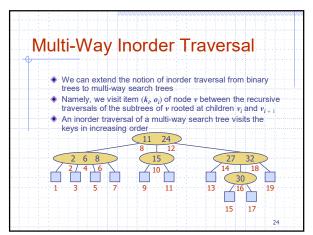


Outline and Reading

Multi-way search tree (§3.3.1)
Definition
Search
(2,4) tree (§3.3.2)
Definition
Search
Insertion
Deletion
Comparison of dictionary implementations

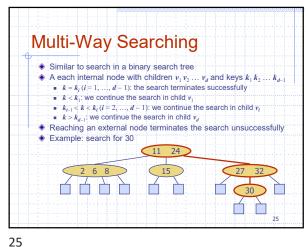
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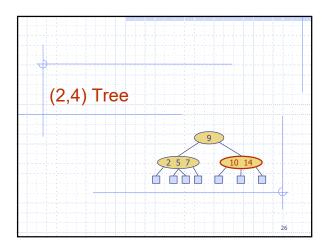




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**B-Trees** 

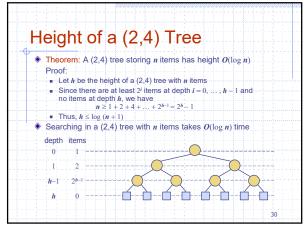
- ♠ A B-Tree is a balanced multi-way search tree, i.e., all leaves are at the same depth
- ◆ B-Trees are used to implement a file structure that allows random access by key as well as sequential access of keys in sorted order
- The size (maximum number of keys) of a node in a B-Tree file structure is determined by the size of a sector of a track of a disk file (also called a physical block)
- ◆ A (2,4) Tree is a special case of a B-Tree in which each node can contain 1, 2, or 3 keys

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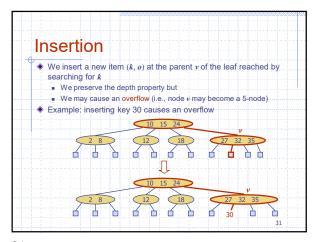
(2,4) Tree A (2,4) tree (also called 2-4 tree or 2-3-4 tree) is a multi-way search tree with the following properties Node-Size Property: every internal node has at most four children Depth Property: all the external nodes have the same depth Depending on the number of children, an internal node of a (2.4) tree is called a 2-node, 3-node or 4-node

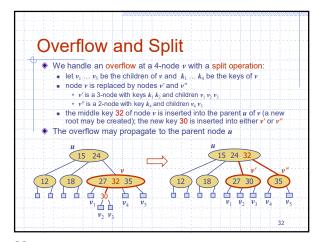
Why (2-4) Trees? ◆A Red-Black tree is an implementation of a (2-4) Tree in a binary tree data structure ♦ If you understand the (2-4) Tree implementation, you will more easily understand what is done and why in a Red-Black Tree to keep it balanced You will appreciate that it's easier and more efficient in space and time to implement a Red-Black Tree than a (2-4) Tree 28

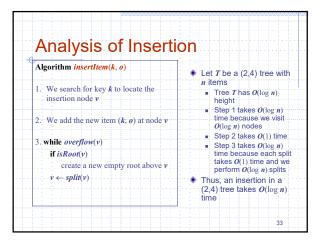
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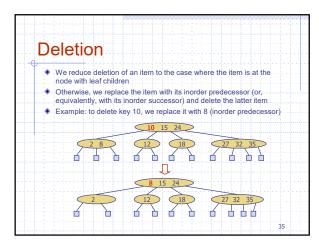


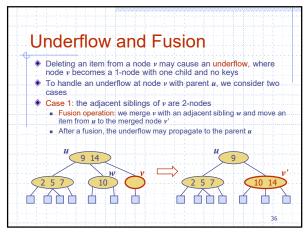
Example:

Insert the following into an initially empty 2-4 tree in this order:

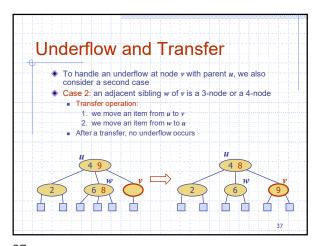
(16, 5, 22, 45, 2, 10, 18, 30, 50, 12, 1, 33)

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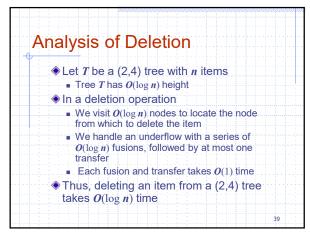


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**Analysis of Deletion** Algorithm deleteItem(k) ◆ Let T be a (2,4) tree with n items
■ Tree T has O(log n) 1. We search for key k and locate the height deletion node v Step 1 takes  $O(\log n)$  time because we visit  $O(\log n)$  nodes 2. while underflow(v) do Step 2 takes  $O(\log n)$  time because each fusion takes O(1) time if isRoot(v) change the root to child of v; return if  $a \ sibling(v) = u$  is a 3- or 4-node and we perform  $O(\log n)$  fusions transfer(u, v); return Thus, a deletion in a (2,4) else {both siblings are 2-nodes} tree takes  $O(\log n)$  time fusion(u, v) {merge v with sibling u}  $v \leftarrow parent(v)$ 

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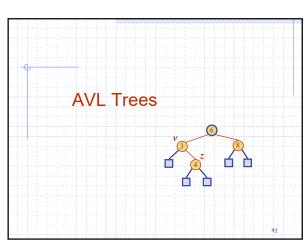
Main Point

3. By introducing some flexibility in the data content of each node, all leaf nodes of a (2,4) Tree can be kept at the same depth.

Stability and adaptability are fundamentals of progress and evolution in nature.

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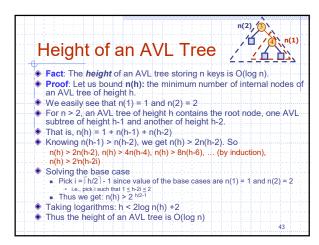
AVL Tree Definition

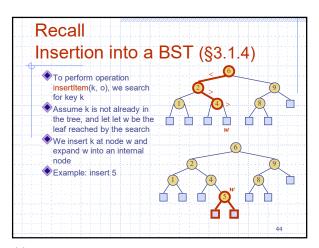
AVL trees are balanced.

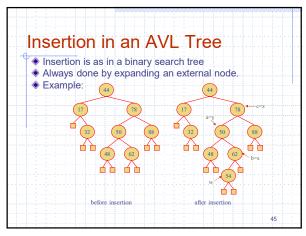
An AVL Tree is a binary search tree such that for every internal node v of T, the heights of the children of v can differ by at most 1.

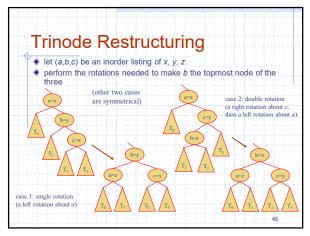
An example of an AVL tree where the heights are shown next to the nodes:

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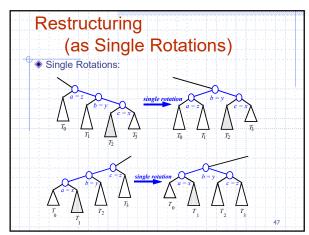


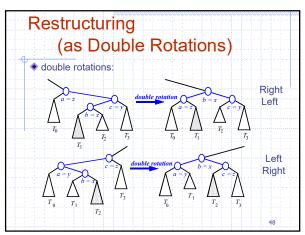




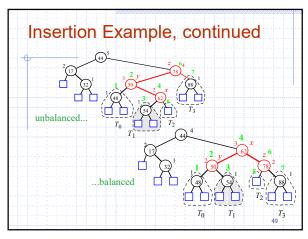


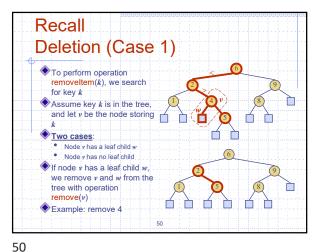
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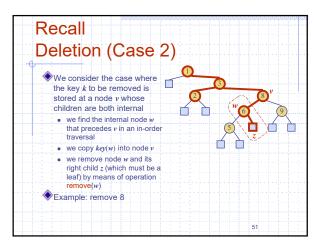


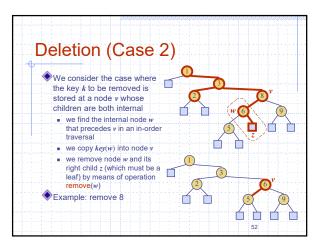


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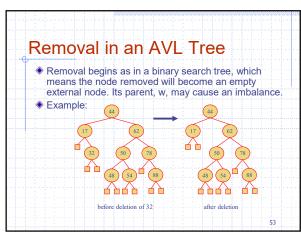


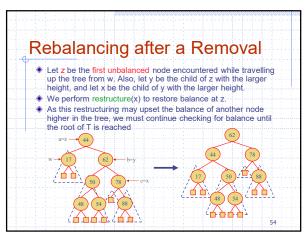






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## Running Times for AVL Trees a single restructure is O(1) using a linked-structure binary tree find is O(log n) height of tree is O(log n), no restructures needed insert is O(log n) nitial find is O(log n) Restructuring up the tree, maintaining heights is O(log n) remove is O(log n) initial find is O(log n) Restructuring up the tree, maintaining heights is O(log n) Restructuring up the tree, maintaining heights is O(log n)

Advantages of
Binary Search Trees

When implemented properly, BST's

perform insertions and deletions faster
than can be done on Linked Lists

perform any find with the same efficiency
as a binary search on a sorted array

keep all data in sorted order (eliminates the
need to sort)

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## Main Point

2. The elimination of the worst case behavior of a binary search tree is accomplished by ensuring that the tree remains balanced, that is, the insert and delete operations do not allow any leaf to become significantly deeper than the other leaves of the tree. Science of Consciousness: Regular experience of pure consciousness during the TM technique reduces stress and restores balance in the physiology. The state of perfect balance, pure consciousness, is the basis for balance in activity.

Connecting the Parts of Knowledge with the Wholeness of Knowledge

- In a (2,4) tree, each node has 2, 3, or 4 children and all leaf nodes are at the same depth so search, insertion, and deletion are efficient, O(log n).
- The insert and delete operations in a (2,4) tree are carefully structured so that the activity at each node promotes balance in the tree as a whole. Each node contributes to the dynamic balance by giving and receiving keys during key transfer and the splitting and fusion of nodes.

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- 3. Transcendental Consciousness is the state of perfect balance, the foundation for wholeness of life, the basis for balance in activity.

  4. Impulses within Transcendental Consciousness:
  The dynamic natural laws within this unbounded field.
- The dynamic natural laws within this unbounded field create and maintain the order and balance in creation.

  Wholeness moving within itself: In Unity
- Wholeness moving within itself: In Unity Consciousness, one experiences the dynamics of pure consciousness that gives rise to the laws of nature, the order and balance in creation, as nothing other than one's own Self.