

```

Algorithm sum(L)
    if L.isEmpty() then return 0
    return sumHelper(L, L.first())

```

```

Algorithm sumHelper(L, p)
    if L.isLast(p) then
        return p.element()
    s := sumHelper(L, L.after(p))
    return s + p.element()

```

```

Algorithm sum(T)
    if T.isEmpty() then return 0
    return sumHelper(T, T.root())
Algorithm sumHelper(T, p)
    if T.isExternal(p) then
        return 0
    lsum := sumHelper(T, T.leftChild(p))
    rsum := sumHelper(T, T.rightChild(p))
    return lsum + rsum + p.element()

```

$$\frac{z}{b} = \frac{a \log_b x}{b} = \left(\frac{\log_b x}{b} \right)^a$$

$$b^z = x^a$$

$$\log_b b^z = \log_b x^a$$

$$z = \log_b x^a$$

5 → false

3 → false

```

Algorithm isEven(n)
    if n = 0 then
        return true
    return ! isEven(n-1)
Algorithm isEven(n)
    if n = 0 then
        return true
    if n = 1 then
        return false
    return isEven(n-2)

```

```

Algorithm findSmallestHelper(T, p)
    if T.isExternal(p) then
        return +infinity
    Lmin := findSmallestHelper(T, T.leftChild(p))
    Rmin := findSmallestHelper(T, T.rightChild(p))
    return MIN(MIN(Lmin, Rmin), p.element())

```

```

Algorithm shuffle(S)
    last := S.size()
    while last > 1 do
        r := randomInt(last)
        last := last - 1
        S.swapElements(S.atRank(r), S.atRank(last))

```

```

Algorithm shuffleRec(S)
    last := S.size()
    shuffleHelper(S, last)

```

```

Algorithm shuffleHelper(S, last)
    if last > 1 then
        r := randomInt(last)
        last := last - 1
        S.swapElements(S.atRank(r), S.atRank(last))
        shuffleHelper(S, last)

```

```

Algorithm findSmallerKeys(T, x)
    S := new Sequence
    if T.isEmpty() then return S
    findSmallerHelper(T, T.root(), x, S)
    return S

```

```

Algorithm findSmallerHelper(T, p, x, S)
    if T.isExternal(p)  $\vee$  p.element() > x then
        return
    findSmallerHelper(T, T.leftChild(p), x, S)
    S.insertLast(p.element())
    findSmallerHelper(T, T.rightChild(p), x, S)

```

$() \Rightarrow ()$

$(1, 2) \Rightarrow (), (2), (1), (1, 2)$

$(1, 2, 3) \Rightarrow (), (3), (2), (2, 3), (1), (1, 3), (1, 2), (1, 2, 3)$

Algorithm powerSet(S)

```
R := new Sequence
if S.isEmpty() then
    R.insertLast(S)
    return R
e := S.remove(S.last())
R1 := powerSet(S)
for each sub in R1.elements() do
    R.insertLast(sub)
    sub2 := copy(sub)
    sub2.insertLast(e)
    R.insertLast(sub2)
return R
```

Algorithm powerSet(S)

```
if S.isEmpty() then
    R := new List
    S.insertLast(R)
    return S
e := S.remove(S.last())
R := powerSet(S)
return powerSetHelper(R, R.first(), e)
```

Algorithm powerSetHelper(R, p, e)

```
sub := copy(p.element())
sub.insertLast(e)
R.insertAfter(p, sub)
if R.isLast(p) then
    return R
return powerSetHelper(R, R.after(p), e)
```