

# Lists

COMP 2210 – Dr. Hendrix



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[http://en.wikipedia.org/wiki/List\\_\(computing\)](http://en.wikipedia.org/wiki/List_(computing))

“In computer science, a **list** or *sequence* is an abstract data structure that implements an **ordered collection of values**”

### Ordered ...

{	By element value	Self-ordered lists (sorted)
	By absolute position (index number)	Indexed lists (sequence)
	By relative position (front, rear, after)	Non-indexed lists (“bullet” list)
<hr/>		
	By time of insertion	Temporal lists (stacks, queues)
	By priority	Priority queues

## Define: List according to the text and me

### Chapter 4 – Unordered List

*Aren't all lists ordered? Isn't that the point?*

“An unordered list is a linear collection of entries whose relative positions with respect to one another is irrelevant.”

*Order is independent of element value and is decided by the client.*

1. Auburn
2. TCU
3. Oregon
4. Stanford
5. Ohio State

- Milk
- Eggs
- Bread
- Cheetos
- Pizza

### Chapter 5 – Ordered List

*What's a key?*

“An ordered list is a linear collection of entries in which the entries are arranged in either ascending or descending order of keys.”

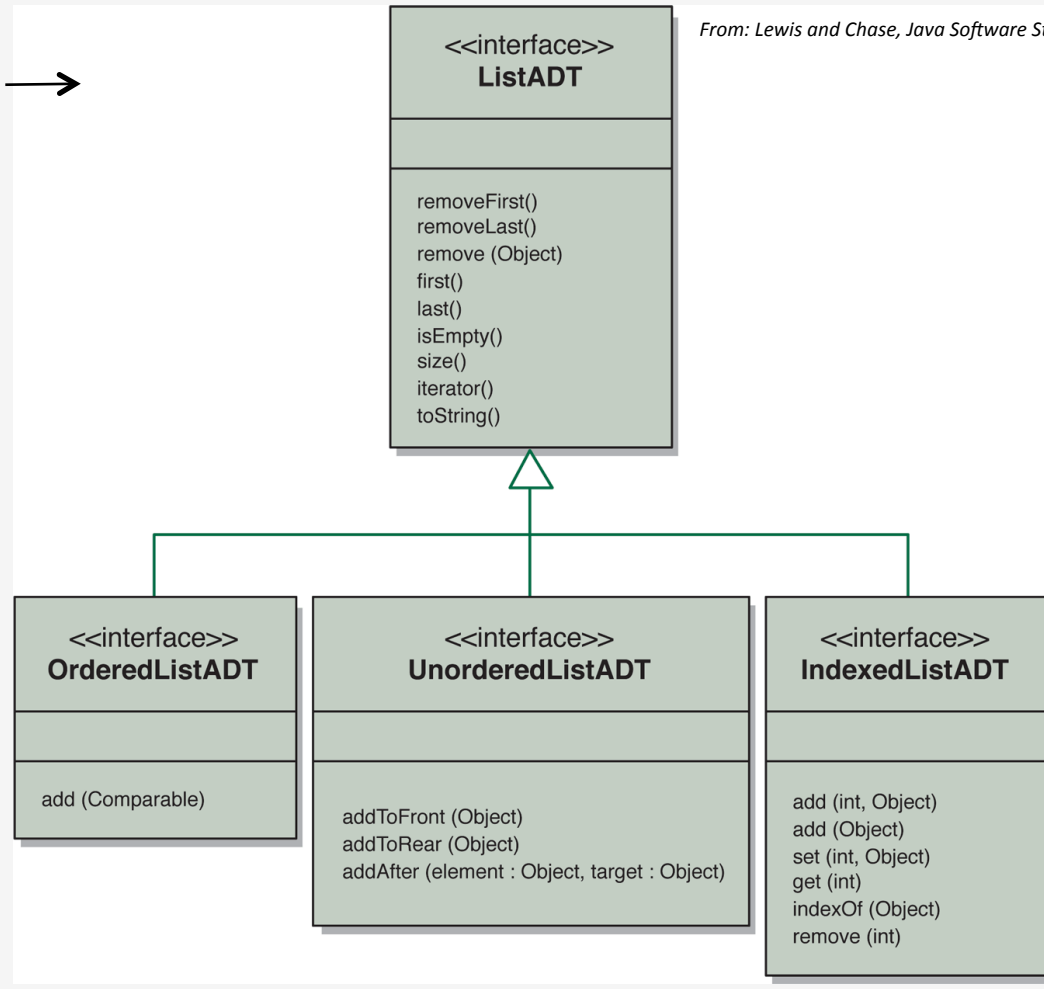
*Order is completely determined by element value and is not (arbitrarily) decided by the client.*

Adams, John, 2, 1797-1801  
Adams, John Q., 6, 1825-1829  
Arthur, Chester, 21, 1881-1885  
Buchanan, James, 15, 1857-1861  
Bush, George HW, 41, 1989-1993

## Designing a list collection

No add method at this level →

*Different kinds of lists would have to support different kinds of add methods.*



Adams, John, 2, 1797-1801  
Adams, John Q., 6, 1825-1829  
Arthur, Chester, 21, 1881-1885  
Buchanan, James, 15, 1857-1861  
Bush, George HW, 41, 1989-1993

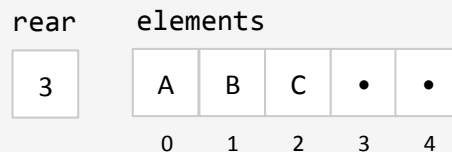
- Milk
- Eggs
- Bread
- Cheetos
- Pizza

1. Auburn
2. TCU
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5. Ohio State

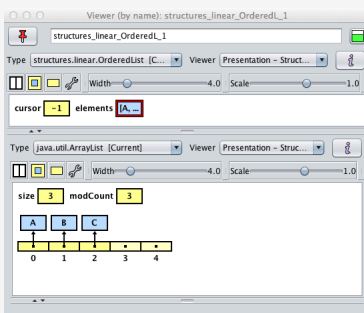
## Implementation choices

### Array-based

- Keep elements left-justified (anchored at 0, no gaps)
- Keep a size counter (can serve as a rear marker)

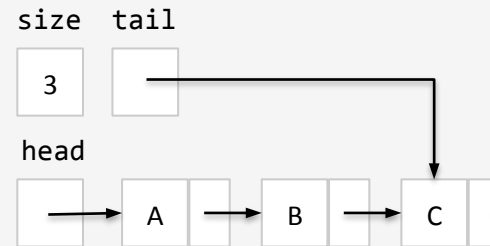


- Use an internal `java.util.ArrayList`
- Keep a “cursor” field to implement iteration.

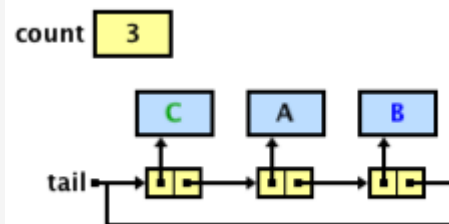


### Node-based

- Singly-linked
- Not circular, no dummy
- Keep both a front and rear pointer
- Keep a size counter



- Singly-linked
- Circular, no dummy
- Keep only a rear pointer
- Keep a size counter



2210

VText

## array-based implementation

## Implementing a list collection: Arrays, add method

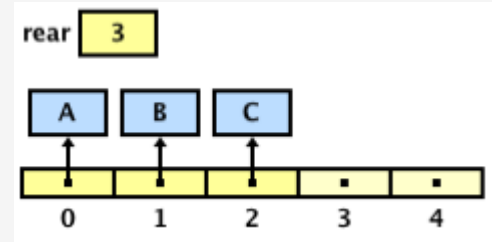
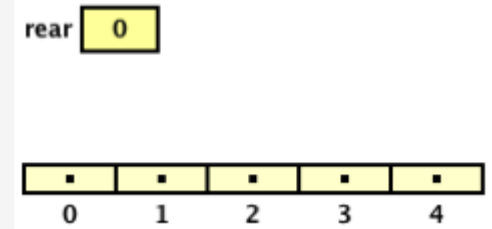
```
public class ArrayIndexedList<T> implements IndexedList<T>
{
    private T[] elements;
    private int rear;
    ...
}
```

```
ArrayIndexedList<String> = new ArrayIndexedList<String>(5);
```

```
alist.add("A");
alist.add("B");
alist.add("C");
```

```
alist.add(1, "D");
```

```
public void add (int index, T element)
{
    ...
}
```



## Implementing a list collection: Arrays, add method

```
public class ArrayIndexedList<T> implements IndexedList<T>
{
    private T[] elements;
    private int rear;
    ...
}
```

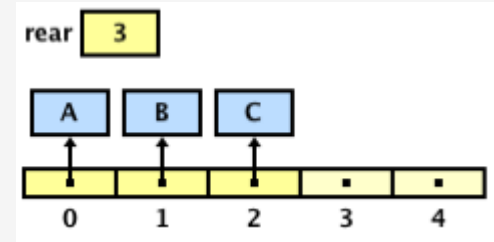
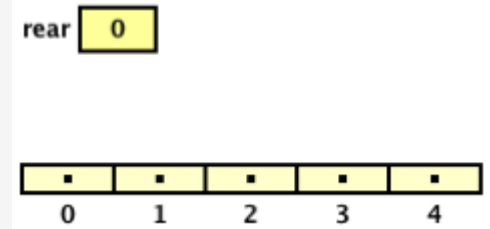
```
ArrayIndexedList<String> = new ArrayIndexedList<String>(5);
```

```
alist.add("A");
alist.add("B");
alist.add("C");
```

```
alist.add(1, "D");
```

```
public void add (int index, T element)
{
    if ((index < 0) || (index > size()))
    {
        throw new IndexOutOfBoundsException();
    }
}
```

} *Validate index*





## Implementing a list collection: Arrays, add method

```
public class ArrayIndexedList<T> implements IndexedList<T>
{
    private T[] elements;
    private int rear;
    ...
}
```

```
ArrayIndexedList<String> = new ArrayIndexedList<String>(5);
```

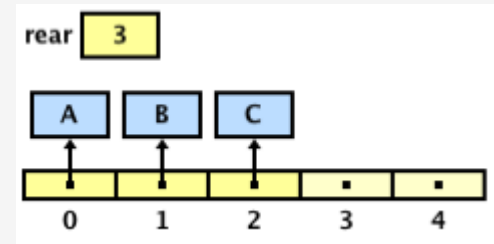
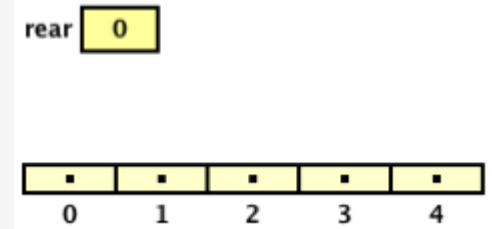
```
alist.add("A");
alist.add("B");
alist.add("C");
```

```
alist.add(1, "D");
```

```
public void add (int index, T element)
{
    if ((index < 0) || (index > size()))
    {
        throw new IndexOutOfBoundsException();
    }
    if (isFull())
    {
        expandCapacity();
    }
}
```

} Validate index

} Check if full



## Implementing a list collection: Arrays, add method

```
public class ArrayIndexedList<T> implements IndexedList<T>
{
    private T[] elements;
    private int rear;
    ...
}
```

```
ArrayIndexedList<String> = new ArrayIndexedList<String>(5);
```

```
alist.add("A");
alist.add("B");
alist.add("C");
```

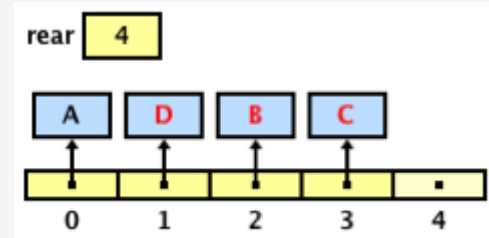
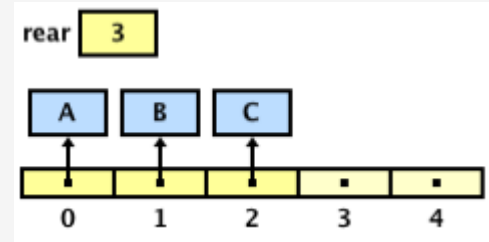
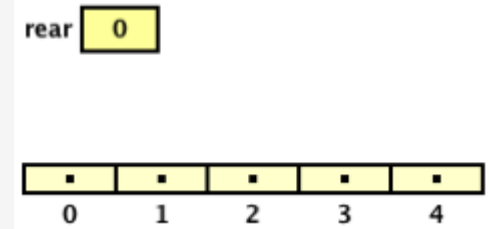
```
alist.add(1, "D");
```

```
public void add (int index, T element)
{
    if ((index < 0) || (index > size()))
    {
        throw new IndexOutOfBoundsException();
    }
    if (isFull())
    {
        expandCapacity();
    }
    shiftRight(index);
    elements[index] = element;
    rear++;
}
```

} Validate index

} Check if full

} Insert new element

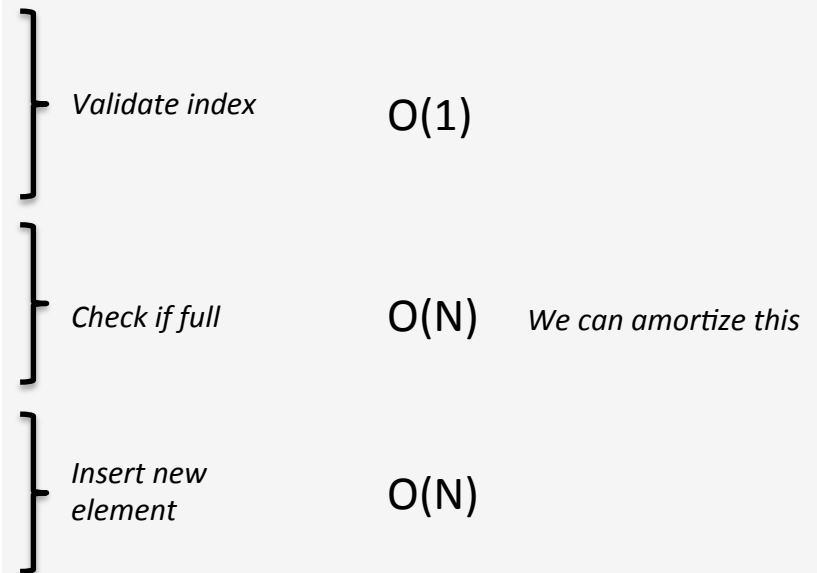


## Arrays, add method – time complexity

```
public class ArrayIndexedList<T> implements IndexedList<T>
{
    private T[] elements;
    private int rear;
    ...
}
```

```
public void add (int index, T element)
{
    if ((index < 0) || (index > size()))
    {
        throw new IndexOutOfBoundsException();
    }
    if (isFull())
    {
        expandCapacity();
    }
    shiftRight(index);
    elements[index] = element;
    rear++;
}
```

**The add method is  $O(N)$ .**



### Two important points:

- (1)  $\left\{ \begin{array}{l} \text{expandCapacity() should not be called often.} \\ \text{Use "repeated doubling."} \\ \text{Consider a reduceCapacity() for remove.} \end{array} \right.$

- (2)  $\left\{ \begin{array}{l} \text{The physical insertion is } O(1). \\ \text{Having to shift elements is } O(N). \\ \text{This is unavoidable with order.} \end{array} \right.$

## node-based implementation

## Implementing a list collection: Nodes, add method

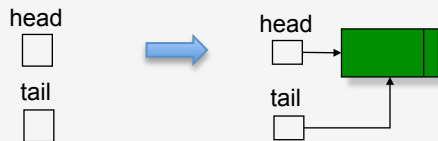
```
public class LinkedListIndexedList<T> implements IndexedList<T>
{
    private Node<T> head;
    private Node<T> tail;
    private int size;
    ...
}
```

size **0** tail **null**

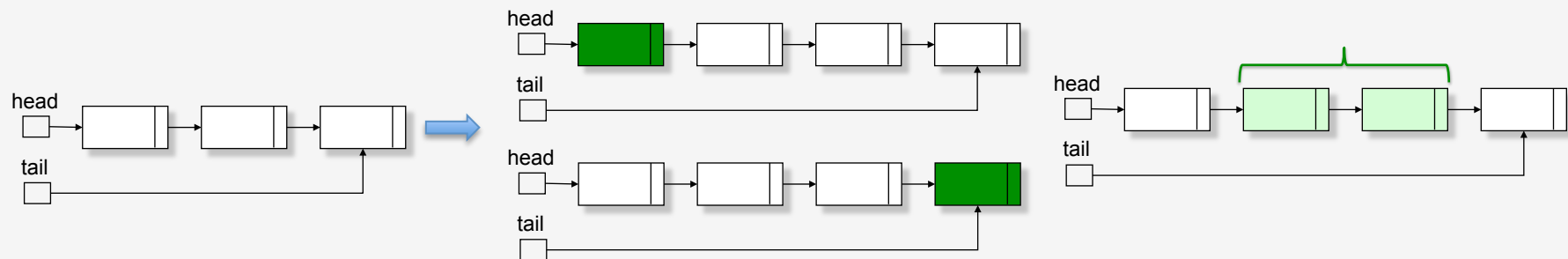
head

```
public void add (int index, T element)
```

### Empty



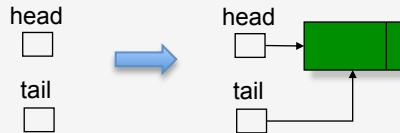
### Not empty



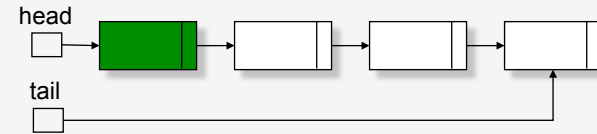
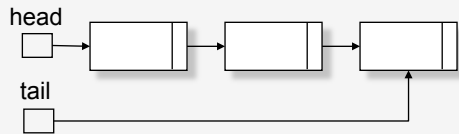
## Implementing a list collection: Nodes, add method

*Four cases to consider for add*

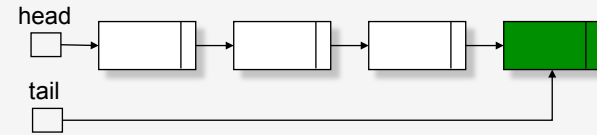
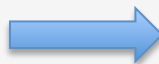
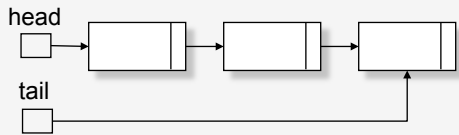
**Empty**



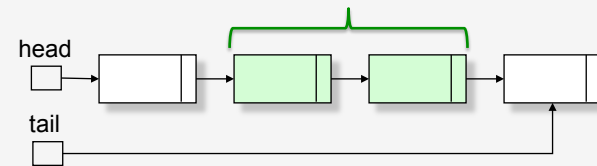
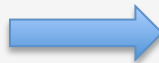
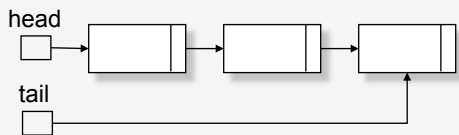
**Non-Empty, index == 0**



**Non-Empty, index == size()**



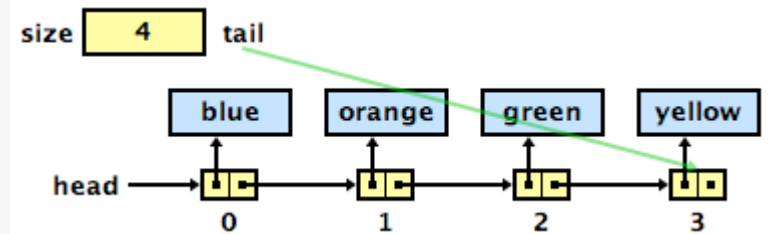
**Non-Empty, index in the middle**



## Implementing a list collection: Nodes, add method

*Validate index, allocate memory*

```
public void add (int index, T element)
{
    if ((index < 0) || (index > size))
    {
        throw new IndexOutOfBoundsException();
    }
    LinearNode<T> temp = new LinearNode<T>(element);
    if (isEmpty())
    {
        head = temp;
        tail = temp;
    }
    else if (index == 0)
    {
        temp.setNext(head);
        head = temp;
    }
    else if (index == size)
    {
        tail.setNext(temp);
        tail = temp;
    }
    else
    {
        LinearNode<T> p = head;
        for (int i = 0; i < index-1; i++)
        {
            p = p.getNext();
        }
        temp.setNext(p.getNext());
        p.setNext(temp);
    }
    size++;
}
```



**index < 0 || index > 4**

```
list.add(-1, "red");
```

-----

Exception in evaluation thread  
java.lang.IndexOutOfBoundsException

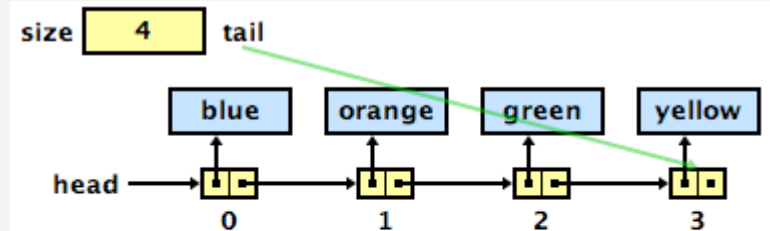
```
list.add(10, "red");
```

-----

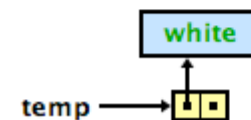
Exception in evaluation thread  
java.lang.IndexOutOfBoundsException

**index >= 0 && index <= 4**

```
list.add(2, "white");
```



Local Variable Node References



## Implementing a list collection: Nodes, add method

*Add to an empty list*

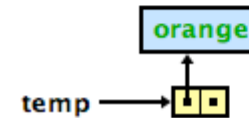
```
public void add (int index, T element)
{
    if ((index < 0) || (index > size))
    {
        throw new IndexOutOfBoundsException();
    }
    Node<T> temp = new Node<T>(element);
    if (isEmpty())
    {
        head = temp;
        tail = temp;
    }
    else if (index == 0)
    {
        temp.setNext(head);
        head = temp;
    }
    else if (index == size)
    {
        tail.setNext(temp);
        tail = temp;
    }
    else
    {
        Node<T> p = head;
        for (int i = 0; i < index-1; i++)
        {
            p = p.getNext();
        }
        temp.setNext(p.getNext());
        p.setNext(temp);
    }
    size++;
}
```

```
list.add(0, "orange");
```

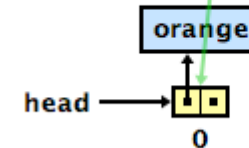
size **0** tail **null**

head

Local Variable Node References



size **1** tail



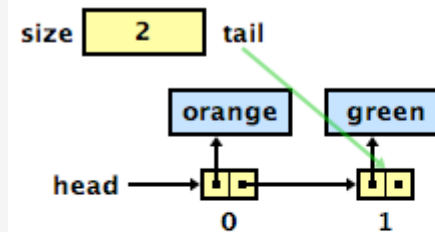


## Implementing a list collection: Nodes, add method

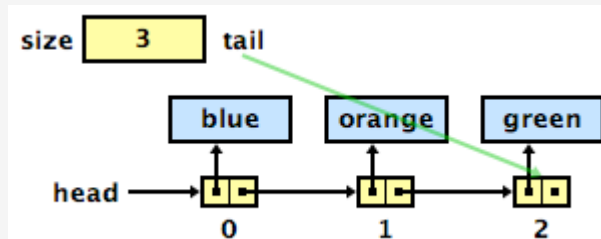
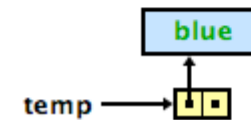
*Add to a non-empty list at index 0*

```
public void add (int index, T element)
{
    if ((index < 0) || (index > size))
    {
        throw new IndexOutOfBoundsException();
    }
    Node<T> temp = new Node<T>(element);
    if (isEmpty())
    {
        head = temp;
        tail = temp;
    }
    else if (index == 0)
    {
        temp.setNext(head);
        head = temp;
    }
    else if (index == size)
    {
        tail.setNext(temp);
        tail = temp;
    }
    else
    {
        Node<T> p = head;
        for (int i = 0; i < index-1; i++)
        {
            p = p.getNext();
        }
        temp.setNext(p.getNext());
        p.setNext(temp);
    }
    size++;
}
```

```
list.add(0, "blue");
```



Local Variable Node References

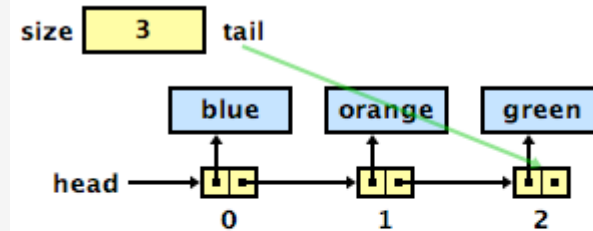


## Implementing a list collection: Nodes, add method

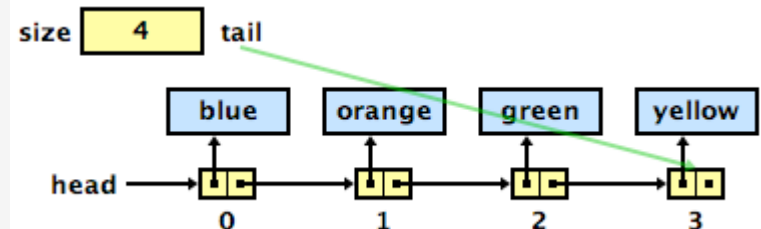
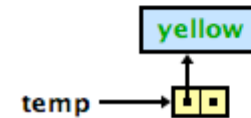
*Add to a non-empty list at index size()*

```
public void add (int index, T element)
{
    if ((index < 0) || (index > size))
    {
        throw new IndexOutOfBoundsException();
    }
    Node<T> temp = new Node<T>(element);
    if (isEmpty())
    {
        head = temp;
        tail = temp;
    }
    else if (index == 0)
    {
        temp.setNext(head);
        head = temp;
    }
    else if (index == size)
    {
        tail.setNext(temp);
        tail = temp;
    }
    else
    {
        Node<T> p = head;
        for (int i = 0; i < index-1; i++)
        {
            p = p.getNext();
        }
        temp.setNext(p.getNext());
        p.setNext(temp);
    }
    size++;
}
```

```
list.add(list.size(), "yellow");
```



Local Variable Node References



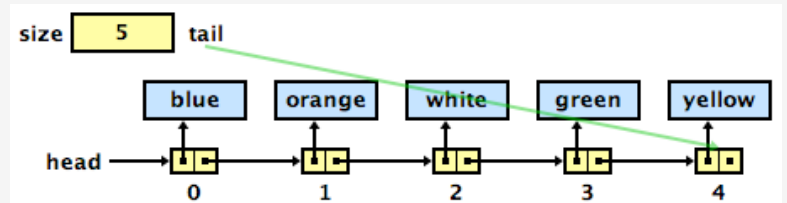
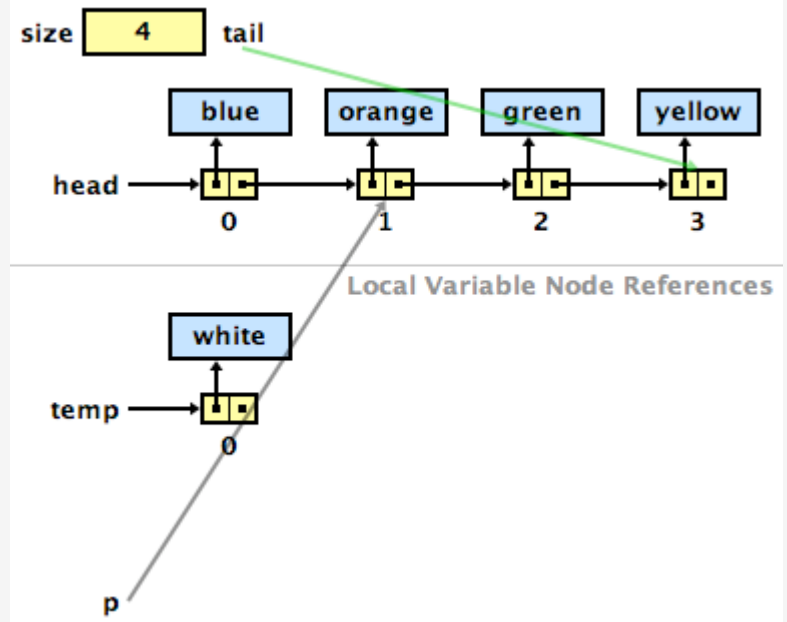
## Implementing a list collection: Nodes, add method

*Add to a non-empty list in the middle*

```
public void add (int index, T element)
{
    if ((index < 0) || (index > size))
    {
        throw new IndexOutOfBoundsException();
    }
    Node<T> temp = new Node<T>(element);
    if (isEmpty())
    {
        head = temp;
        tail = temp;
    }
    else if (index == 0)
    {
        temp.setNext(head);
        head = temp;
    }
    else if (index == size)
    {
        tail.setNext(temp);
        tail = temp;
    }
    else
    {
        Node<T> p = head;
        for (int i = 0; i < index-1; i++)
        {
            p = p.getNext();
        }
        temp.setNext(p.getNext());
        p.setNext(temp);
    }
    size++;
}
```

*Slightly  
different  
traversal  
pattern*

```
list.add(2, "white");
```



## Nodes, add method – time complexity

```
public void add (int index, T element)
{
    if ((index < 0) || (index > size))
    {
        throw new IndexOutOfBoundsException();
    }
    Node<T> temp = new Node<T>(element);
    if (isEmpty())
    {
        head = temp;
        tail = temp;
    }
    else if (index == 0)
    {
        temp.setNext(head);
        head = temp;
    }
    else if (index == size)
    {
        tail.setNext(temp);
        tail = temp;
    }
    else
    {
        Node<T> p = head;
        for (int i = 0; i < index-1; i++)
        {
            p = p.getNext();
        }
        temp.setNext(p.getNext());
        p.setNext(temp);
    }
    size++;
}
```

Complexity analysis for the `add` method:

- The first `if` block (checking index bounds) is  $O(1)$ .
- The `isEmpty()` check and the first `if` block (index == 0) are  $O(1)$ .
- The `else if` block (index == size) is  $O(1)$ .
- The `else` block (traversing the list) is  $O(N)$ .

**The add method is  $O(N)$ .**

### Important point:

The physical insertion is  $O(1)$ .

Finding where the new element goes is  $O(N)$ .

## performance comparison

## Performance analysis

	Indexed List		Non-indexed List		Self-ordered List	
method	Array	Nodes	Array	Nodes	Array	Nodes
remove(element)	O(N)	O(N)	O(N)	O(N)	O(N)	O(N)
addAfter(element, target)	•	•	O(N)	O(N)	•	•
add(element)	O(1)	O(1)	•	•	O(N)	O(N)
add(index, element)	O(N)	O(N)	•	•	•	•
get(index)	O(1)	O(N)	•	•	•	•
indexOf(element)	O(N)	O(N)	•	•	•	•

Tell me why ...



Can we do better...



If we could use binary search on a node-based structure, then add() and remove() would be  $O(\log N)$  – a huge improvement!

*Stay tuned ... this is exactly where we're headed.*