Can an employee treat part-time, fixed-time and agency workers less favourably when is comes to working conditions than full-time and permanent workers?

No, never.

Yes, for part-time and fixed-time workers if the employer can show objective grounds for the difference in treatment, but not for agency workers.

Well done!

Yes, if the employer can show objective grounds for the difference in treatment.