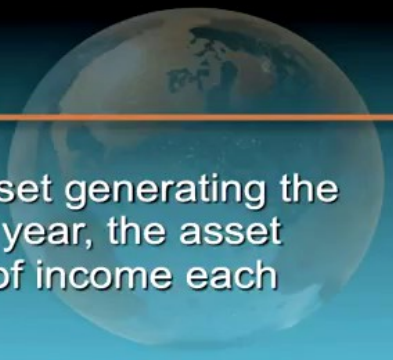




## **LECTURE TEN - PART FOUR**

## NPV In the Real World



- Suppose that instead of an asset generating the same amount of income each year, the asset generates a different amount of income each year.
- Instead of generating a stream of income from now to eternity, the asset generates a stream of income over a fixed period of time – maybe 5 years, maybe 10 years, maybe 50 years.

## **You Are a Textile Industry CEO**

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- Your company is considering replacing your old mechanical looms with a set of highly computerized looms.
- But these new machines won't come cheap.

## **The Price Tag: A Cool \$2 Million**

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- Note, however, that your chief economist forecasts that these new machines will increase revenues by \$500,000 for each of the five years of the service life of the looms.
- Also, at the end of five years, the machines will have a salvage value of another \$500,000.

## From This Data

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- It may seem pretty obvious that the company should make the investment.
- After all, while the machines will cost \$2 million, they will generate an even cooler \$3 million in revenues and salvage value over the five-year period.

## An Important Equation



- Let's not forget about the time value of money.
- And here's the formula you would use to calculate the net present value of this investment.

$$NPV = -(I_0) + \frac{N_1}{1+i} + \frac{N_2}{(1+i)^2} + \dots + \frac{N_t}{(1+i)^t} + \dots$$

$$\text{NPV} = -(I_0) + \frac{N_1}{1+i} + \frac{N_2}{(1+i)^2} + \dots + \frac{N_t}{(1+i)^t} + \dots$$

- $I_0$ : Initial investment at time period zero.
- $i$ : One-period market interest rate (assume at 15%).
- $N_1$ : Net receipts from investment in first period.
- $N_2$ : Net receipts in the second period, and so on.
- The sum of the initial investment and the stream of payments –  $N_1$ ,  $N_2$ , and so on – will have the present value NPV given by the formula.



## Here's The Math

$$\begin{aligned} \text{NPV} &= \boxed{-\$2\text{M}} + \overbrace{\frac{500\text{K}}{1.15} + \frac{500\text{K}}{1.15^2} + \frac{500\text{K}}{1.15^3} + \frac{500\text{K}}{1.15^4} + \frac{500\text{K}}{1.15^5}}^{\text{Income stream}} + \overbrace{\frac{500\text{k}}{1.15^5}}^{\text{Salvage value}} \\ &= -\$2\text{M} + \$1,924,664 \\ &= \boxed{-\$75,336} \end{aligned}$$



## When The NPV Is Negative

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- Your company should not make the investment.
- This is despite the fact that over the life of the investment, the investment will generate an undiscounted sum a full half million dollars greater than the initial investment!!!!

# Investment Is Interest-rate Sensitive!

## Question

What if the interest rate were 5%. Would your company now make the investment?

**Pause the presentation now if you want to try your hand at the math!**

**Yes, You Would Make The Investment!**

$$\begin{aligned} \text{NPV} &= -\$2\text{M} + \frac{500\text{K}}{1.05} + \frac{500\text{K}}{1.05^2} + \frac{500\text{K}}{1.05^3} + \frac{500\text{K}}{1.05^4} + \frac{500\text{K}}{1.05^5} + \frac{500\text{k}}{1.05^5} \\ &= \boxed{\$556,501} \end{aligned}$$

## From An Intuitive Perspective

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- The higher the interest rate, the more one has to discount the revenue stream.
- This, in turn, reduces the present value of the revenue stream and vice versa.