

HUDK 4051: LEARNING ANALYTICS: PROCESS & THEORY

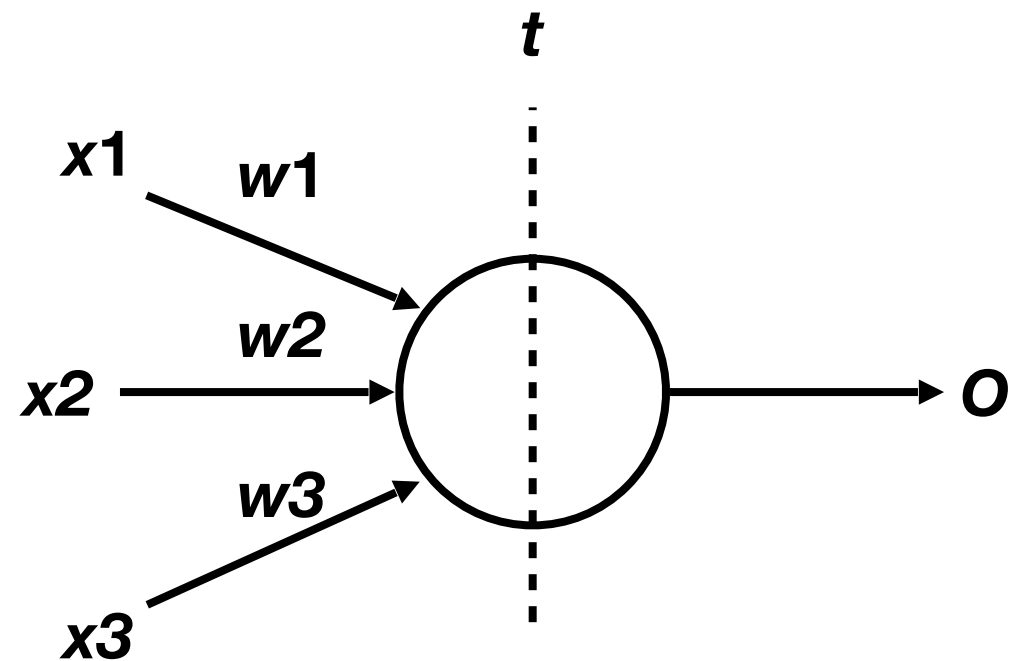
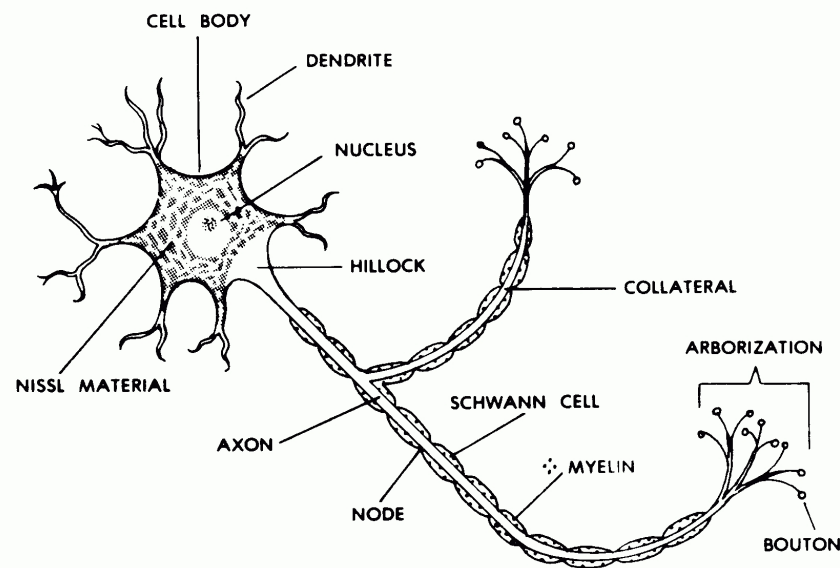
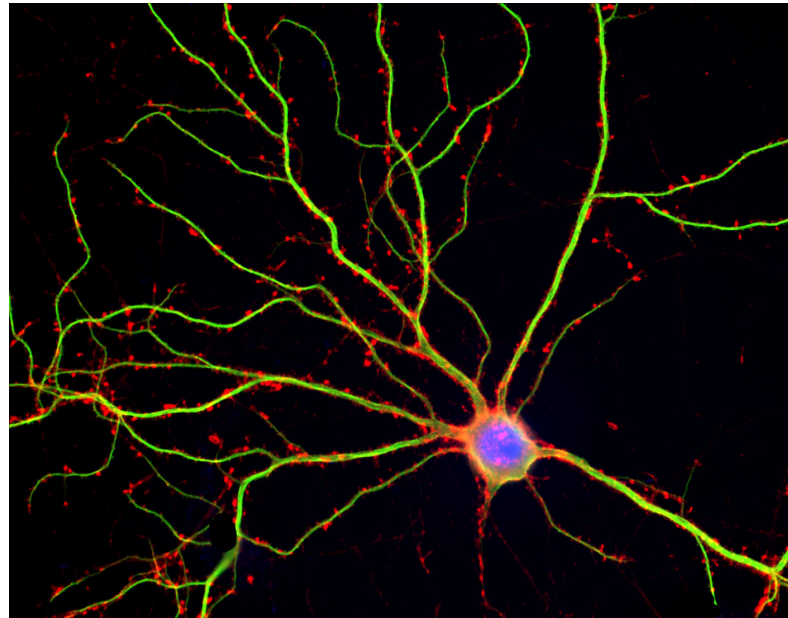
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Today

- Artificial Neural Networks
 - Perceptron
 - Sigmoid Function
 - Back propagation
- Work time

Perceptron

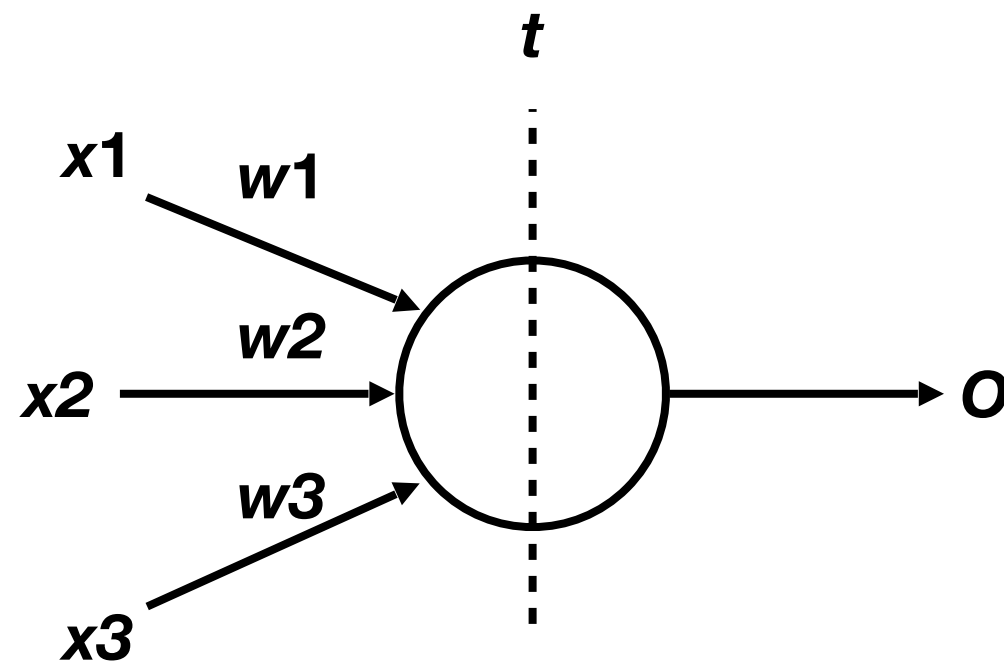
Perceptron



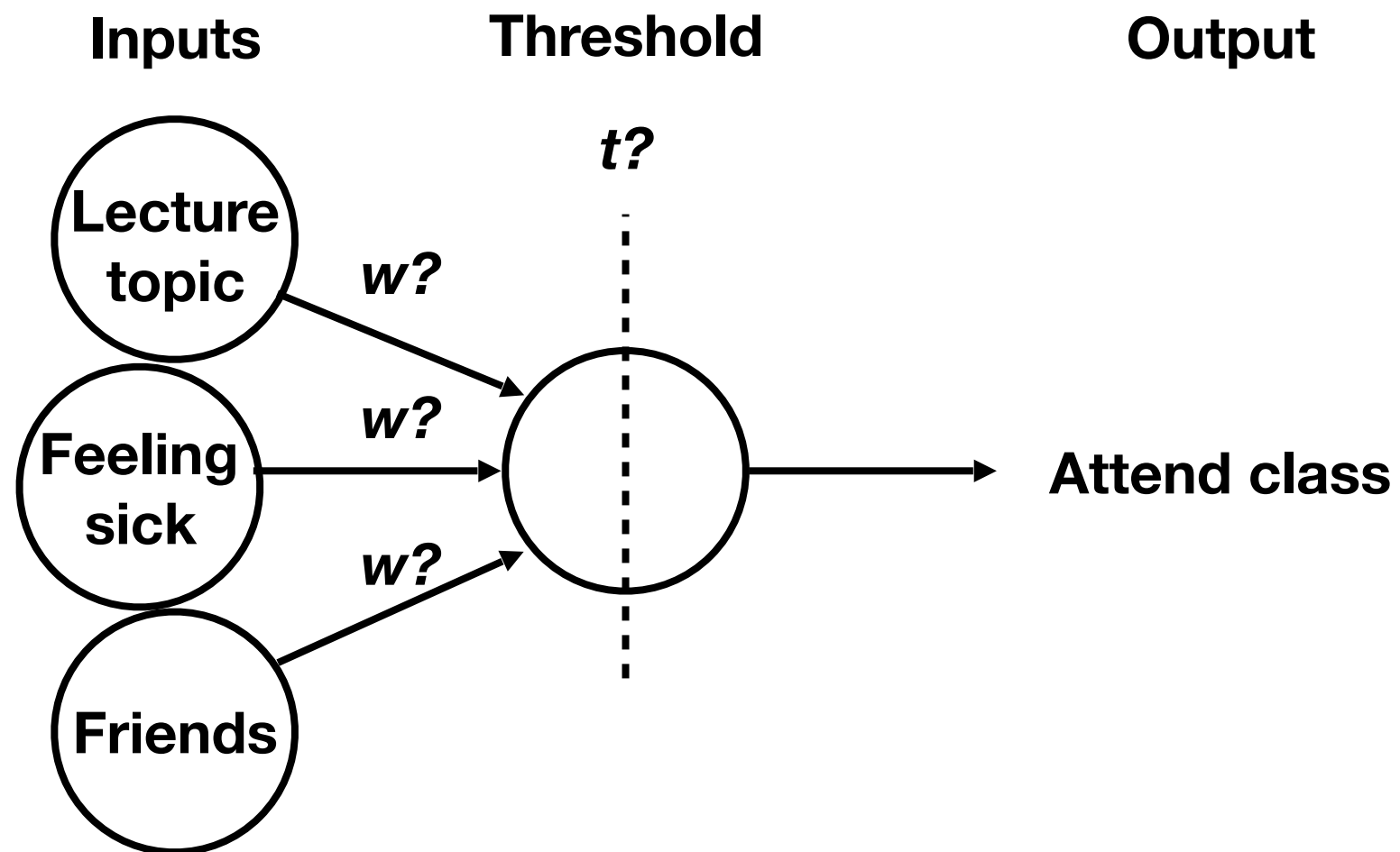
Frank Rosenblatt, 1957

Perceptron

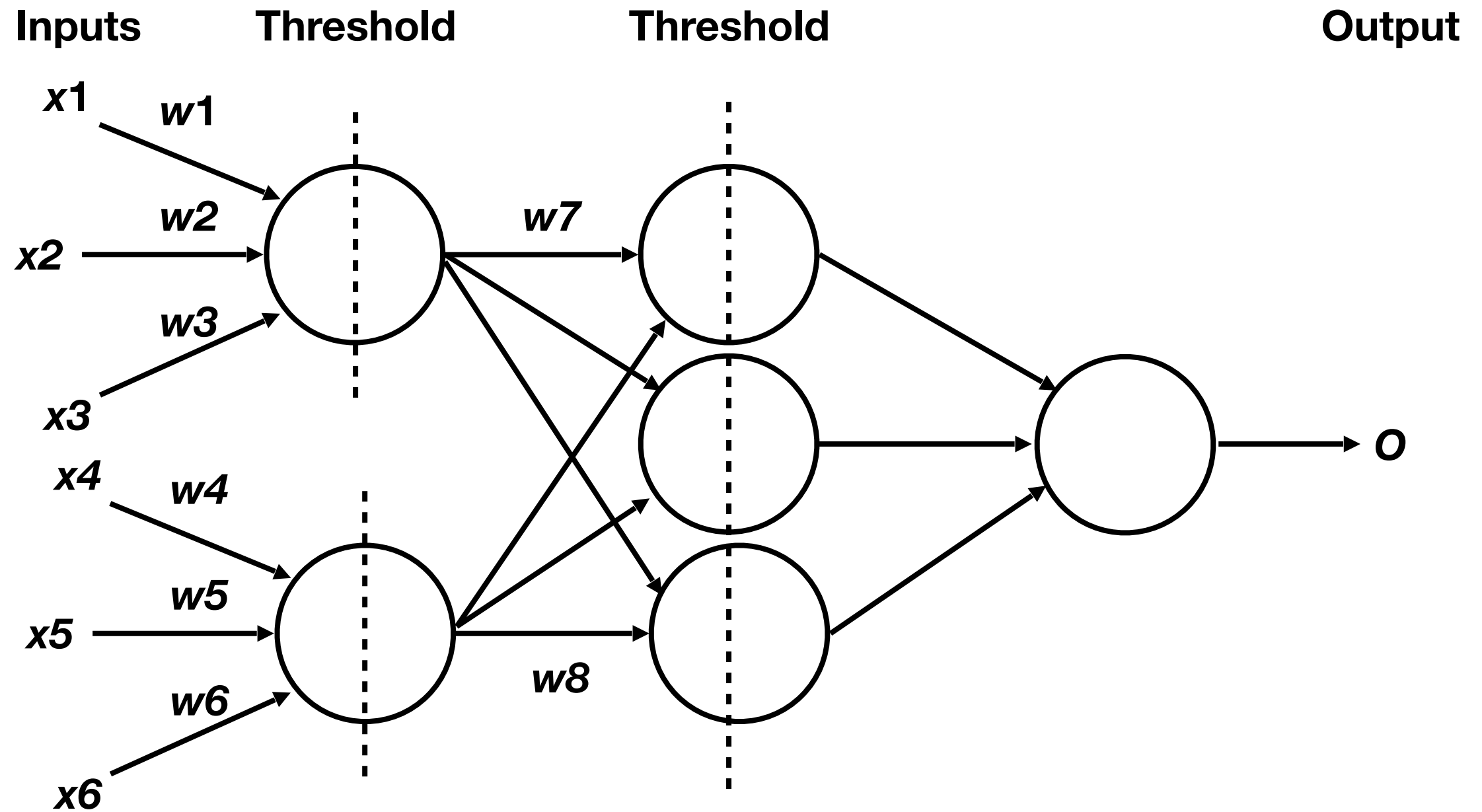
Inputs Threshold Output



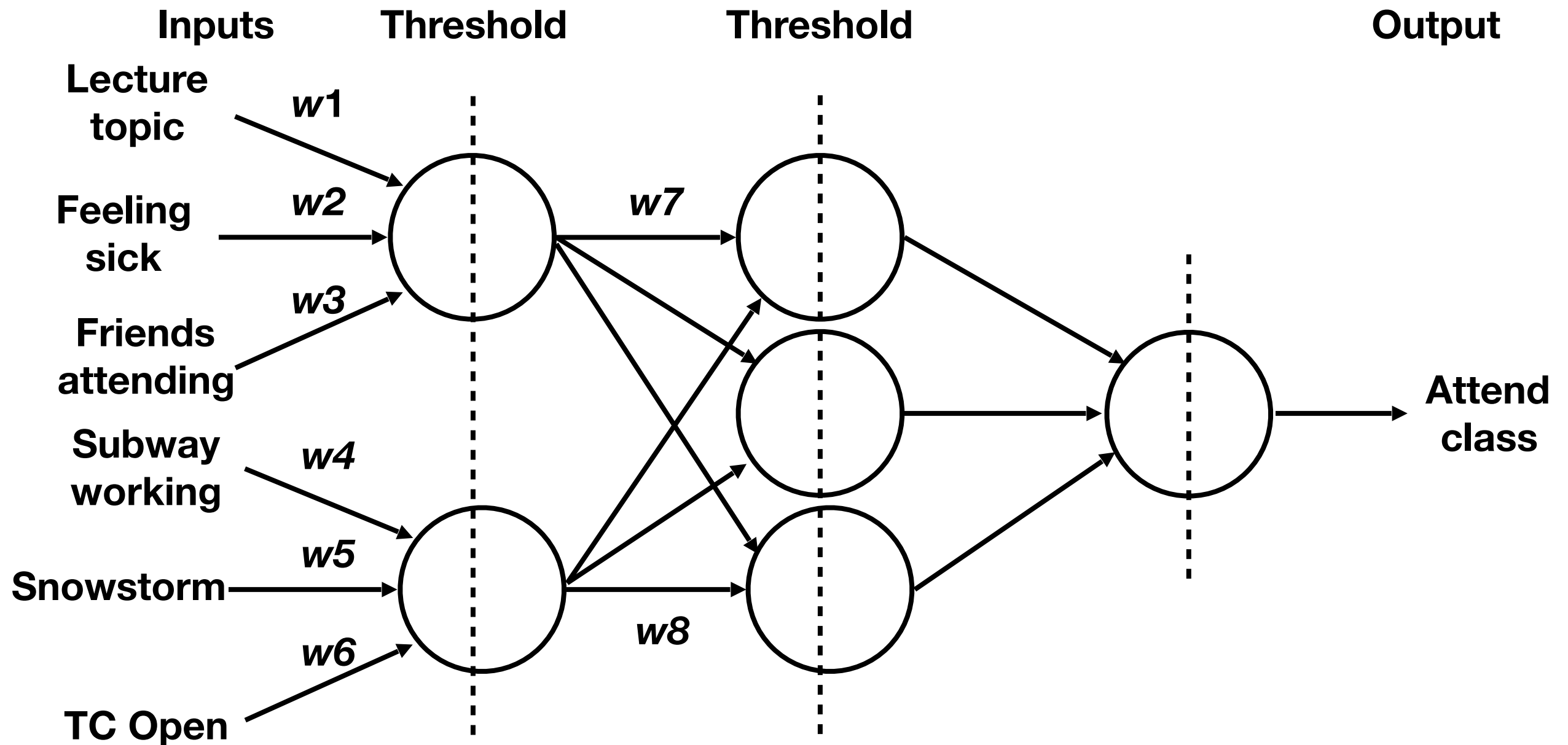
Perceptron



Perceptron



Perceptron



Logic

- From the perceptron we can create a NAND gate
- From a NAND gate can create all other logic units (AND, NOR, etc.)
- See Nielson 2016*

Bias

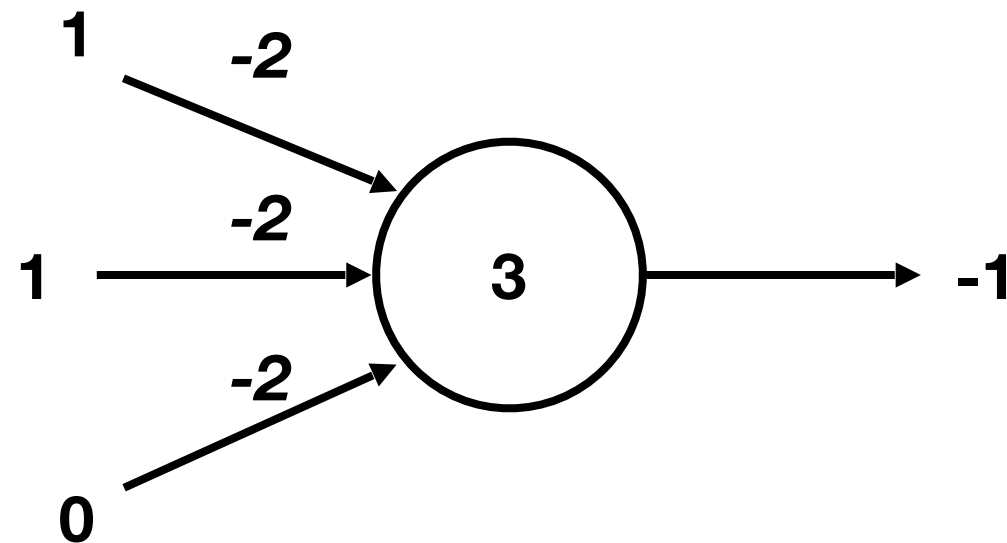
- Another way to describe the threshold
- Negative threshold
- More convenient for notation
- Describes how easy it is to get make the perceptron “fire”

Notation

Inputs

Bias

Output



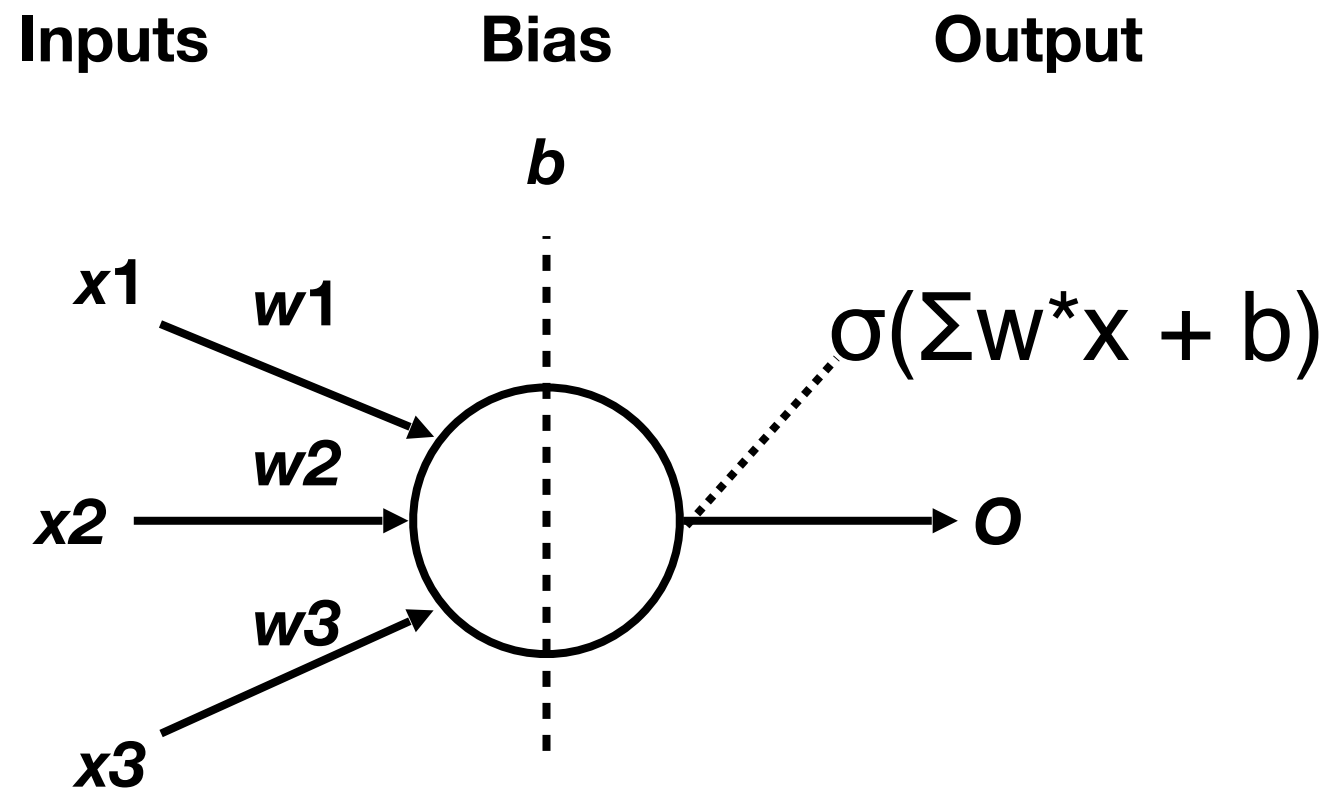
$$(1) \cdot -2 + (1) \cdot -2 + (0) \cdot -2 + 3 = -1$$

Sigmoid Neurons

Sigmoid Neurons

- Want to build a learning algorithm
- Could change b or w
- BUT that will cause very large changes
- Network will never “fix”
- Solution: “smooth” the output

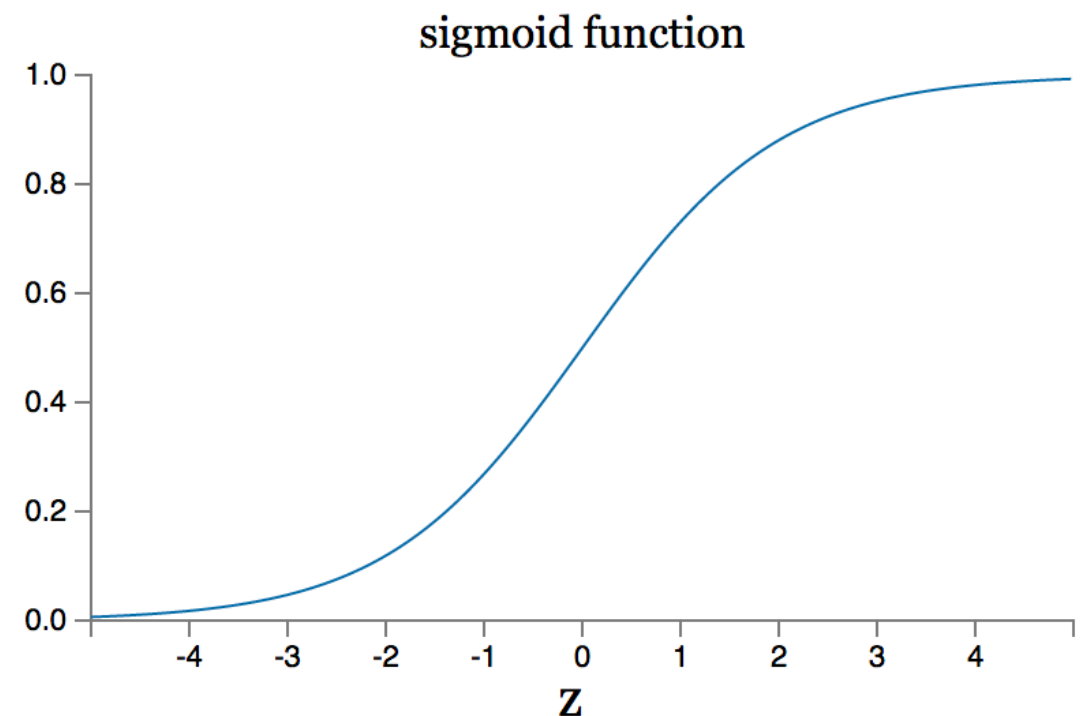
Sigmoid Neurons



Sigmoid Neurons

- Sigmoid function
“smooths” the output
- Makes changing w
and b less sudden and
more predictable
- Could use lots of other
functions...

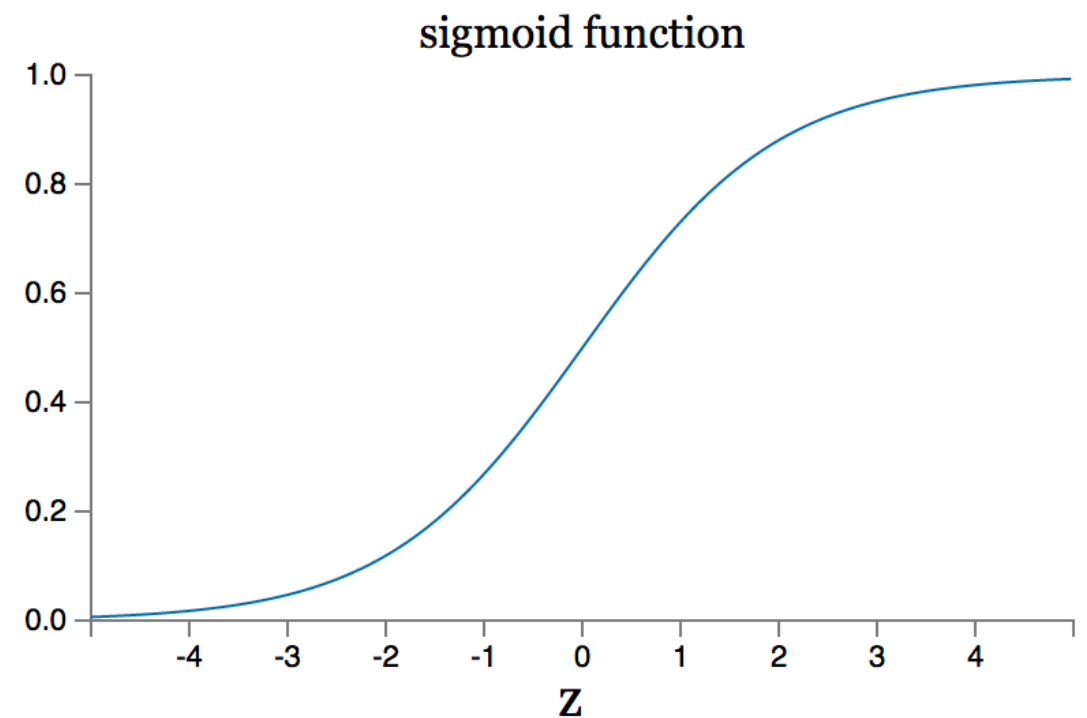
$$\sigma(z) \equiv \frac{1}{1 + e^{-z}}.$$



Sigmoid Neurons

- Perceptrons have 0/1 output
- Sigmoid neurons have 0 - 1 output (eg. 0.1, 0.6778, etc.)
- How to interpret sigmoid neuron output?

$$\sigma(z) \equiv \frac{1}{1 + e^{-z}}.$$

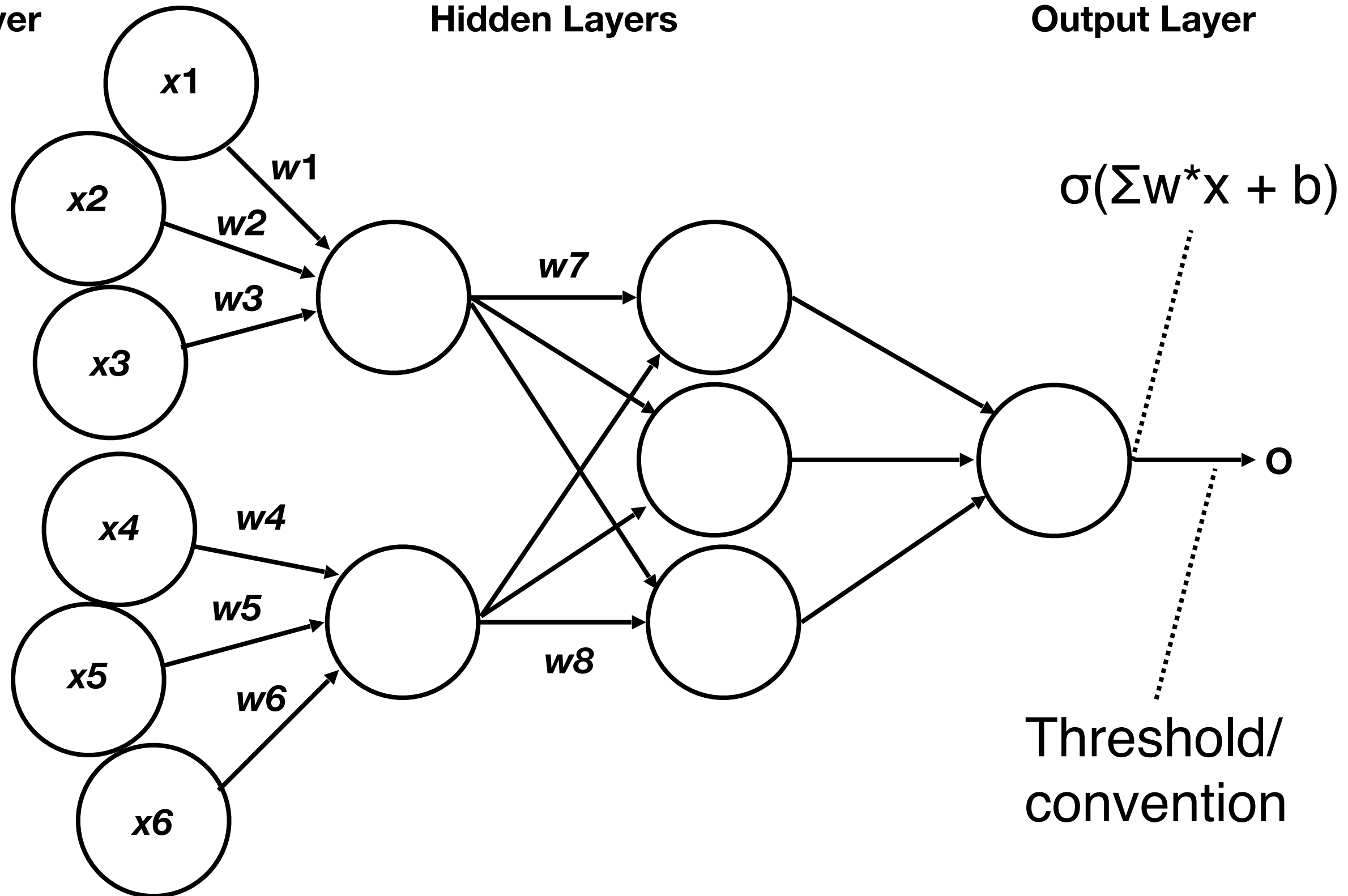


Complete Feedforward Network

Input Layer

Hidden Layers

Output Layer



How many Hidden Layers?

- No foolproof method
- The only method is really trial and error
- Heuristics:
 - Theory based starting point?
 - Number of inputs and outputs?

Exercise

Back Propagation

- Need a way to minimize error
- Error is defined by a cost function
- Then we imagine error as a surface that needs to be “searched” for the minimum

