

# Using FEniCS and OpenFOAM for the simulation of conjugate heat transfer in a partitioned fashion

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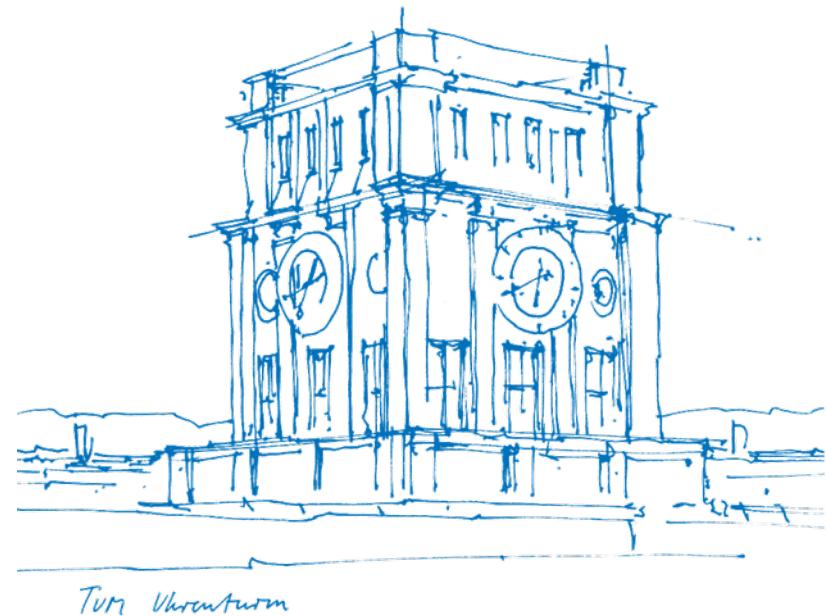
Department of Mechanical Engineering

Energy Technology

GAMM Annual 2019

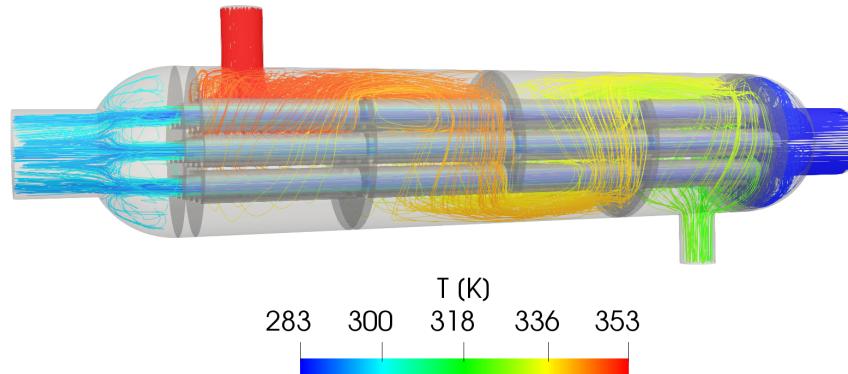
Vienna, Austria

February 19, 2019



# Partitioned Approach

Coupled Problem

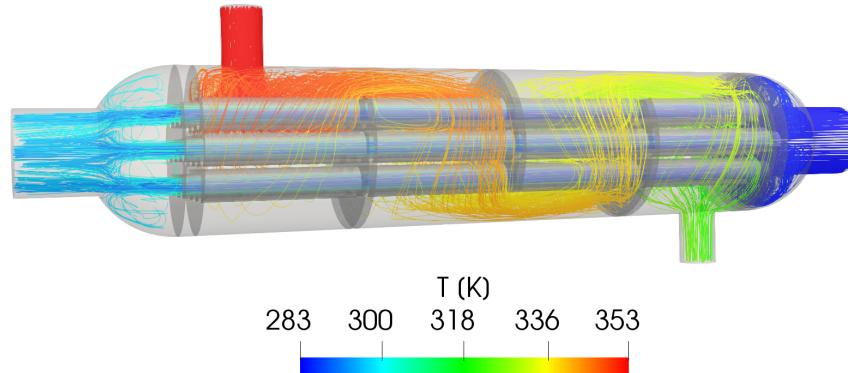


shell and tube heat exchanger using OpenFOAM and CalculiX<sup>1</sup>

<sup>1</sup>Figure from Rusch, A., Uekermann, B. *Comparing OpenFOAM's Intrinsic Conjugate Heat Transfer Solver with preCICE-Coupled Simulations. Technical Report*, 2018.

# Partitioned Approach

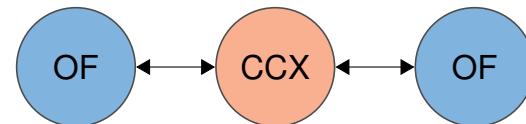
Coupled Problem



shell and tube heat exchanger using OpenFOAM and CalculiX<sup>1</sup>

Basic idea:

- reuse existing solvers
- combine single-physics to solve multi-physics
- only exchange "black-box" information



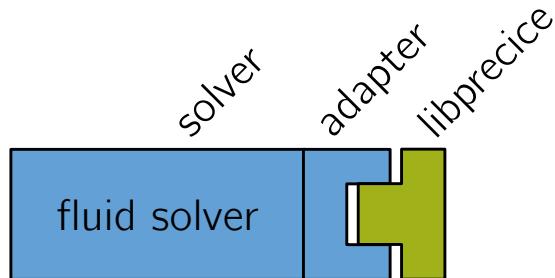
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# preCICE

A Plug-and-Play Coupling Library



LUND UNIVERSITY

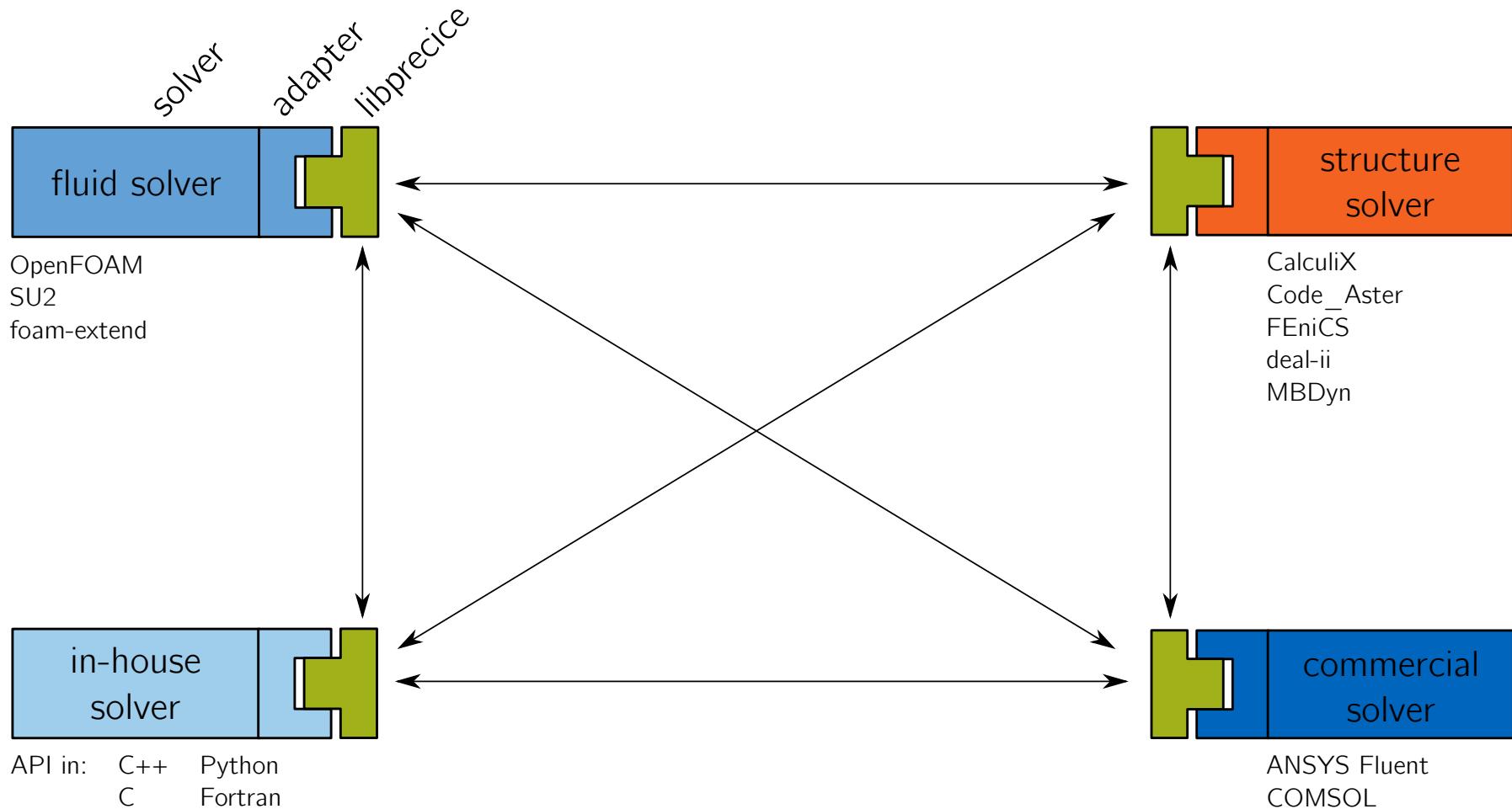


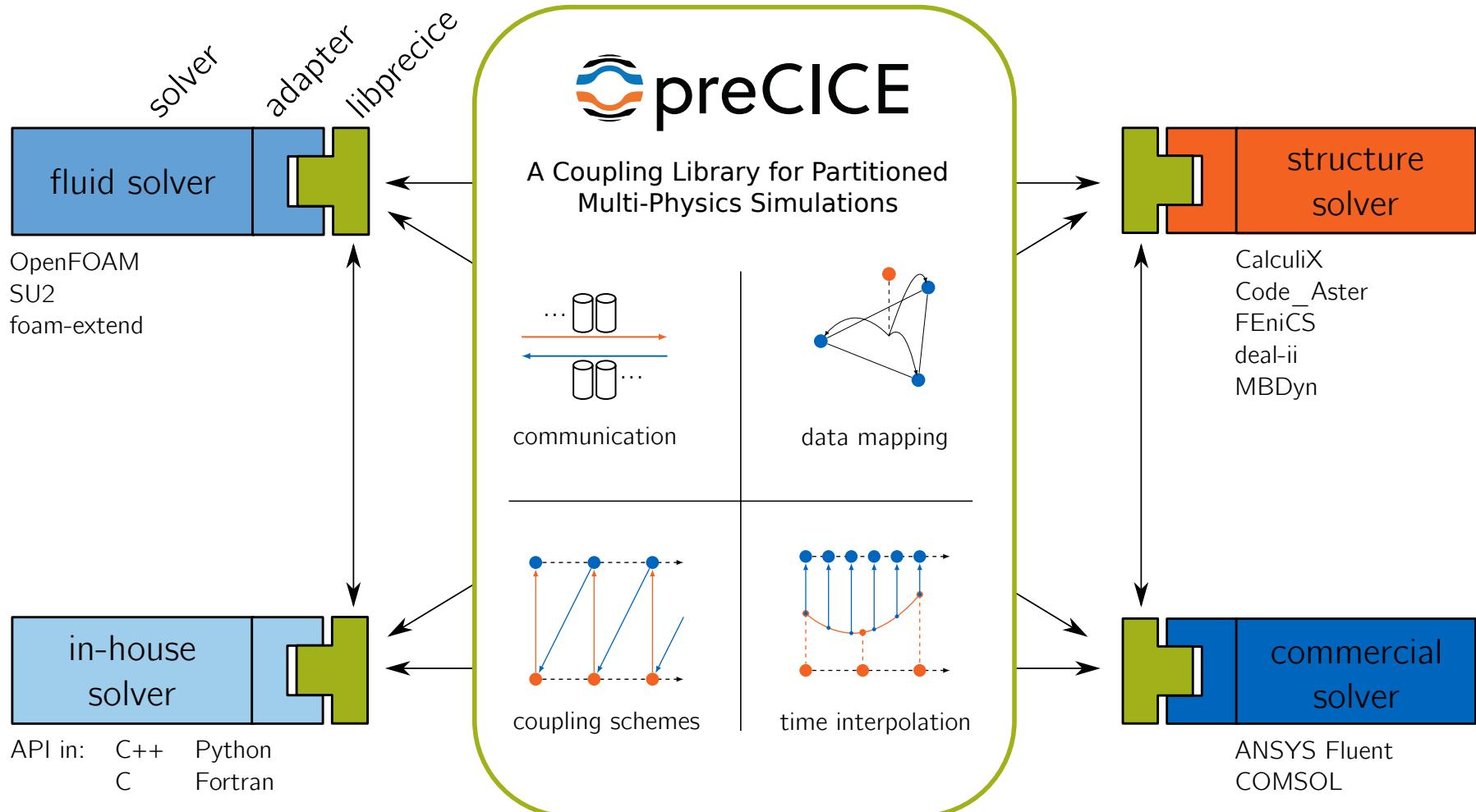
OpenFOAM  
SU2  
foam-extend

# preCICE

A Plug-and-Play Coupling Library







1. Scalability
2. Robust quasi-Newton coupling
3. Coupling of arbitrary many components  
*(arbitrary many = more than two)*
4. Minimally-invasive coupling
5. Open-source, community



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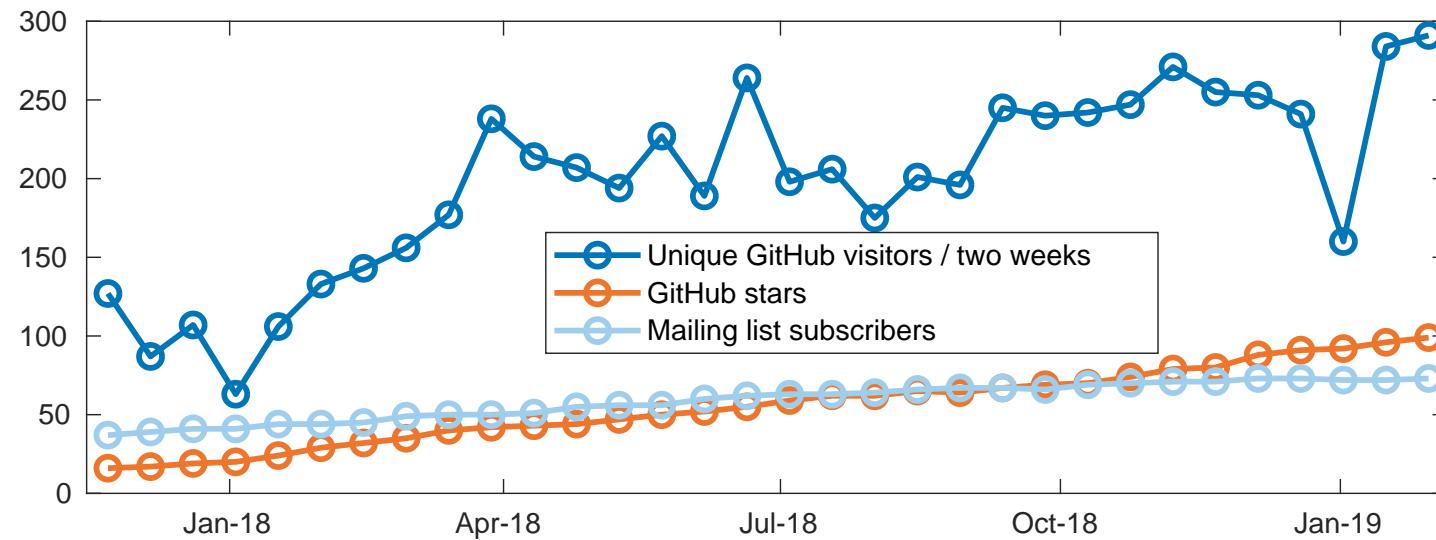
- Bernhard Gatzhammer, Klaudius Scheufele, Lucia Cheung, Alexander Shukaev, Peter Vollmer, Georg Abrams, Alex Trujillo, Dmytro Sashko, David Sommer, David Schneider, Richard Hertrich, Saumitra Joshi, Peter Meisrimel, Derek Risseeuw, Rafal Kulaga, Ishaan Desai ...

- LSM & STS, U Siegen, Germany
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- SCpA, CIRA, Italy
- Cardiothoracic Surgery, UFS, South Africa
- A\*STAR, Singapore
- NRG, Petten, The Netherlands
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- Mechanical and Aeronautical Eng., University of Manchester, UK
- University of Strathclyde, Glasgow, UK
- FAST, KIT, Germany
- AIT, Vienna, Austria

- IAG, University of Stuttgart, Germany
- CTTC UPC, Barcelona, Spain
- Amirkabir U. of Technology, Iran

### Upcoming:

- GRS, Garching, Germany
- MTU Aero Engines, Munich, Germany
- Numerical Analysis, Lund, Sweden
- Helicopter Technology & Astronautics, TUM, Germany
- ATA Engineering Inc., USA
- BITS Pilani, India
- Aviation, MSU Denver, USA





## Plug and play?

- OpenFOAM and FEniCS
- Test case: flow over plate
- Literature results: Vynnycky

# The Solvers

OpenFOAM®<sup>1</sup>

## Software

- open-source (GPLv3)
- widely used for CFD
- ready-to-use solvers
- C++, Libraries with C++ API
- can be used for HPC
- main: [openfoam.com](http://openfoam.com) (ESI/OpenCFD)
- also popular: [openfoam.org](http://openfoam.org)  
(The OpenFOAM Foundation)

## An FVM framework for PDEs

- CFD, Heat Transfer, ...
- Meshing
- Solving
- Post-Processing
- ...

The screenshot shows the OpenFOAM User Guide website. At the top, it says "OpenFOAM" and "The open source CFD toolbox" with the ESI logo. Below is a navigation bar with links: Home, Products, Services, Download, Code, Documentation, Community, Governance, News, About us, Contact, Jobs, Legal, and [prev] [next]. A "FOLLOW US ON twitter" button is also present. The left sidebar has a "User Guide" section with a "Contents" tree:

- 1 Introduction
- ± 2 OpenFOAM cases
- ± 3 Running applications
- ± 4 Mesh generation and conversion
- ± 5 Models and physical properties
- ± 6 Solving
- ± 7 Post-processing
- ± A Reference Index

On the right, the "Chapter 1 Introduction" is displayed. It describes the guide's purpose and the structure of OpenFOAM. A large diagram titled "Open Source Field Operation and Manipulation (OpenFOAM) C++ Library" illustrates the software's architecture. It shows three main components: Pre-processing, Solving, and Post-processing, which interact with various utilities like Meshing Tools, User Applications, Standard Applications, ParaView, and others like EnSight. Below the diagram, there is a caption: "Figure 1.1: Overview of OpenFOAM structure." Further down, there are sections for file structure, running applications, mesh generation, models, solving, and post-processing, each with a brief description and a link to chapter 2.

## OpenFOAM User Guide<sup>2</sup>

<sup>1</sup> OPENFOAM® is a registered trade mark of OpenCFD Limited, producer and distributor of the OpenFOAM software via [www.openfoam.com](http://www.openfoam.com).

<sup>2</sup>OpenFOAM User Guide: <https://www.openfoam.com/documentation/user-guide/>

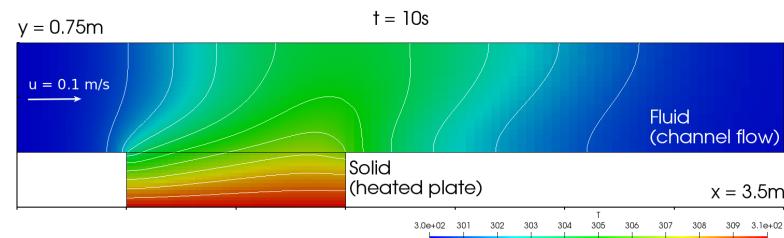
# The Solvers

preCICE Tutorials using OpenFOAM

On [www.precice.org/resources](http://www.precice.org/resources) (step-by-step):

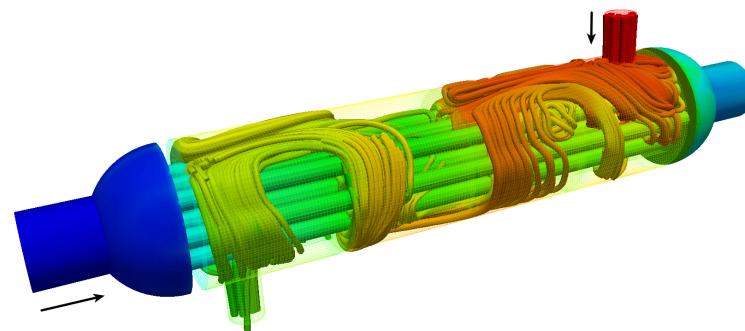
## Flow above a heated plate

- Demo in `precice/openfoam-adapter`
- `buoyantPimpleFoam` + `laplacianFoam`
- Learn how to use the OpenFOAM adapter



## Shell-and-Tube Heat Exchanger

- Larger case in `precice/tutorials`
- `buoyantSimpleFoam` (x2) + CalculiX
- Learn how to do multi-coupling



# The Solvers

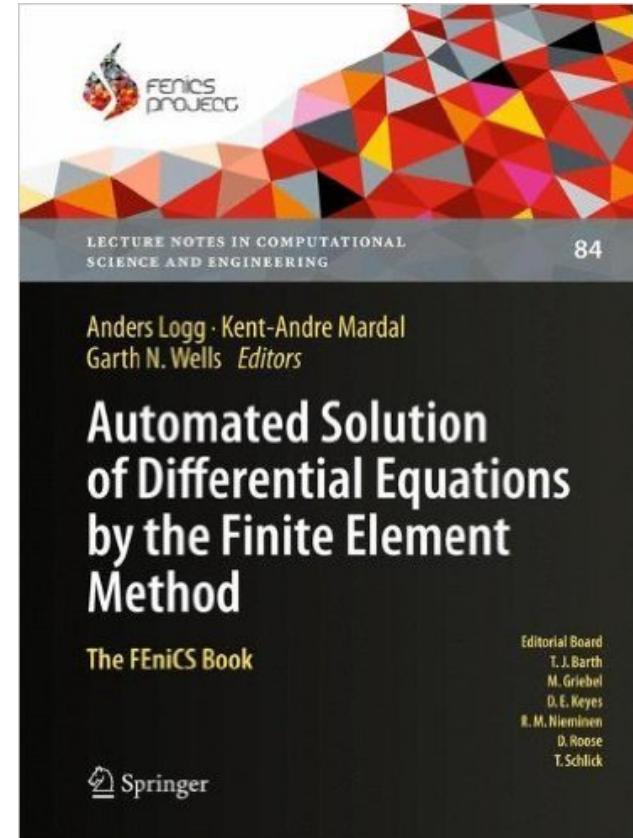
FEniCS<sup>1</sup>

## Software

- open-source (LGPLv3)
- extensive documentation
- Python and C++ API
- can be used for HPC
- [www.fenicsproject.org](http://www.fenicsproject.org)

## Computing platform for solving PDEs

- Definition of weak forms
- Finite Element basis functions
- Meshing
- Solving
- ...



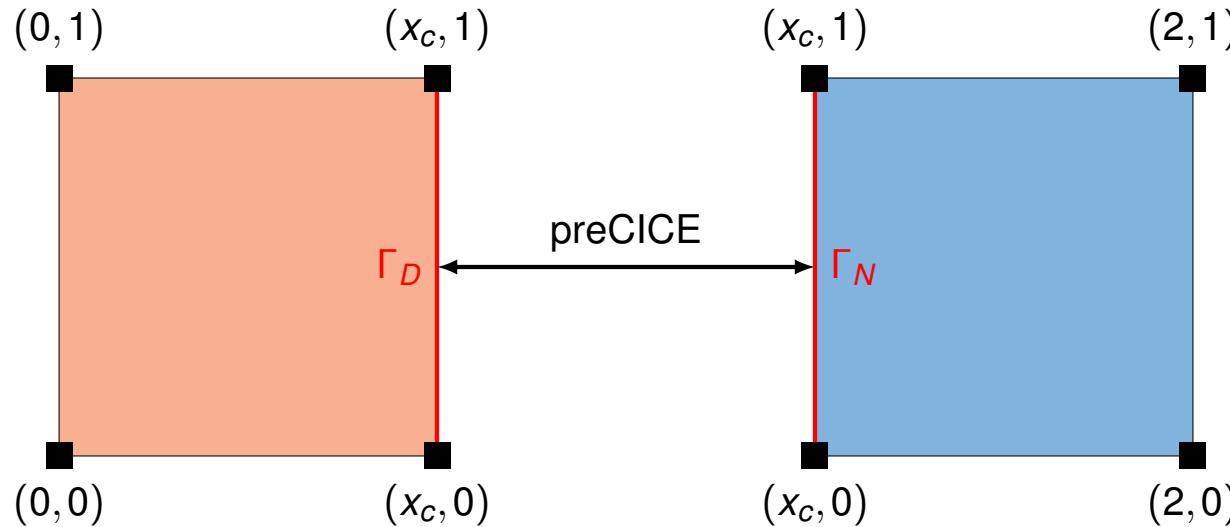
FEniCS book<sup>2</sup>

<sup>1</sup>Alnaes, M. S., et al. (2015). *The FEniCS Project Version 1.5*.

<sup>2</sup>Logg, A., Mardal, K. A., & Wells, G. N. (2012). *Automated solution of differential equations by the finite element method*.

# The Solvers

Toy problem: Partitioned Heat Equation



Partitioned heat equation / transmission problem already discussed in literature (e.g.<sup>1</sup> or <sup>2</sup>).

- in precice/tutorials
- today: only use left half of the domain + FEniCS adapter
- for details see <sup>3</sup>.

<sup>1</sup>Monge, A. (2018). Partitioned methods for time-dependent thermal fluid-structure interaction. Lund University.

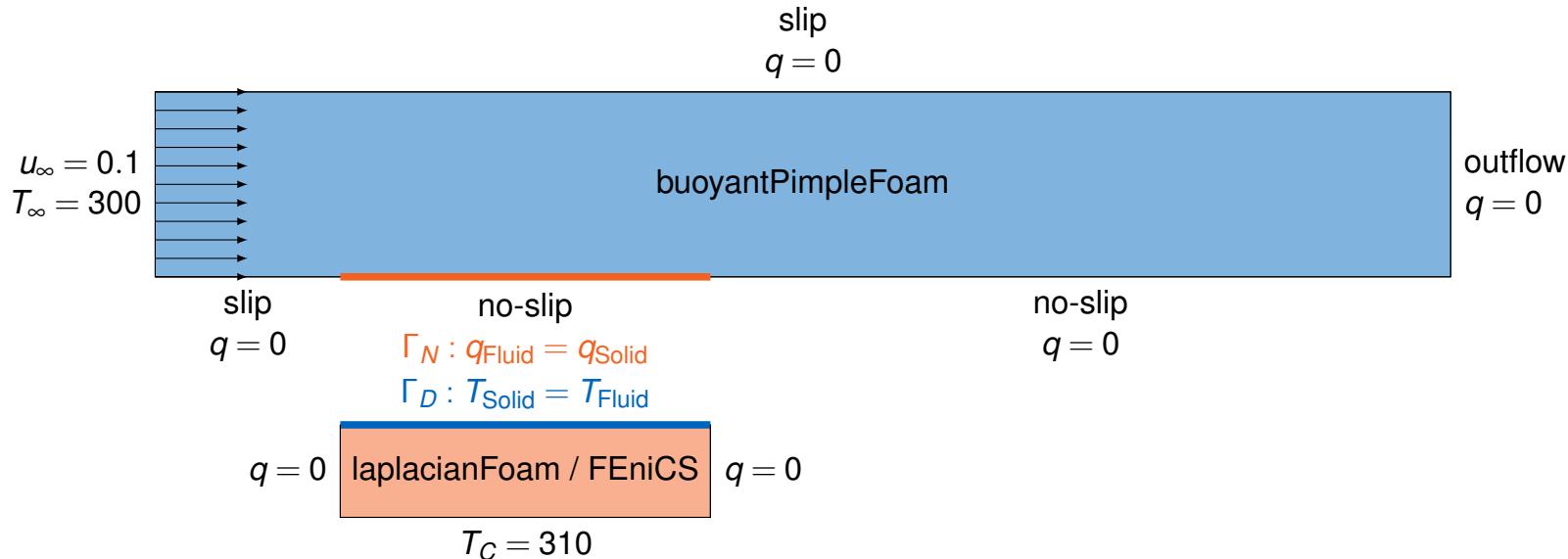
<sup>2</sup>Toselli, A., & Widlund, O. (2005). Domain Decomposition Methods - Algorithms and Theory (1st ed.).

<sup>3</sup>Rüth, B. et al. (2018). Solving the Partitioned Heat Equation Using FEniCS and preCICE. GAMM CSE Workshop 2018.

# Flow over plate

preCICE tutorial <sup>1</sup>

## Boundary conditions and geometry



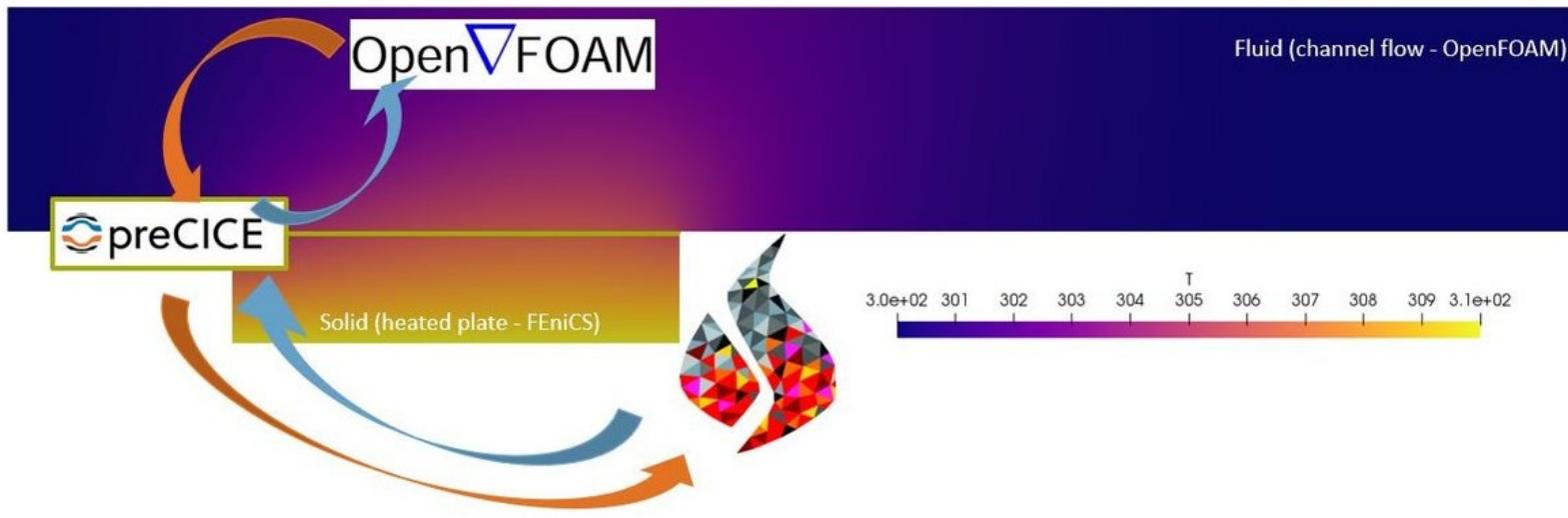
## Additional parameters

- $\lambda = 0.25$  = plate width/plate length
- $\Pr = 0.01$
- $\text{Re} = \rho u_\infty d / \mu = 500$  (use characteristic length  $d$  = plate length)
- $k_s = k_f$  (thermal conductivities)

<sup>1</sup>Cheung Yau, L. (2016). Conjugate Heat Transfer with the Multiphysics Coupling Library preCICE.

# Flow over plate

OpenFOAM-OpenFOAM vs. OpenFOAM-FEniCS



## OpenFOAM-OpenFOAM

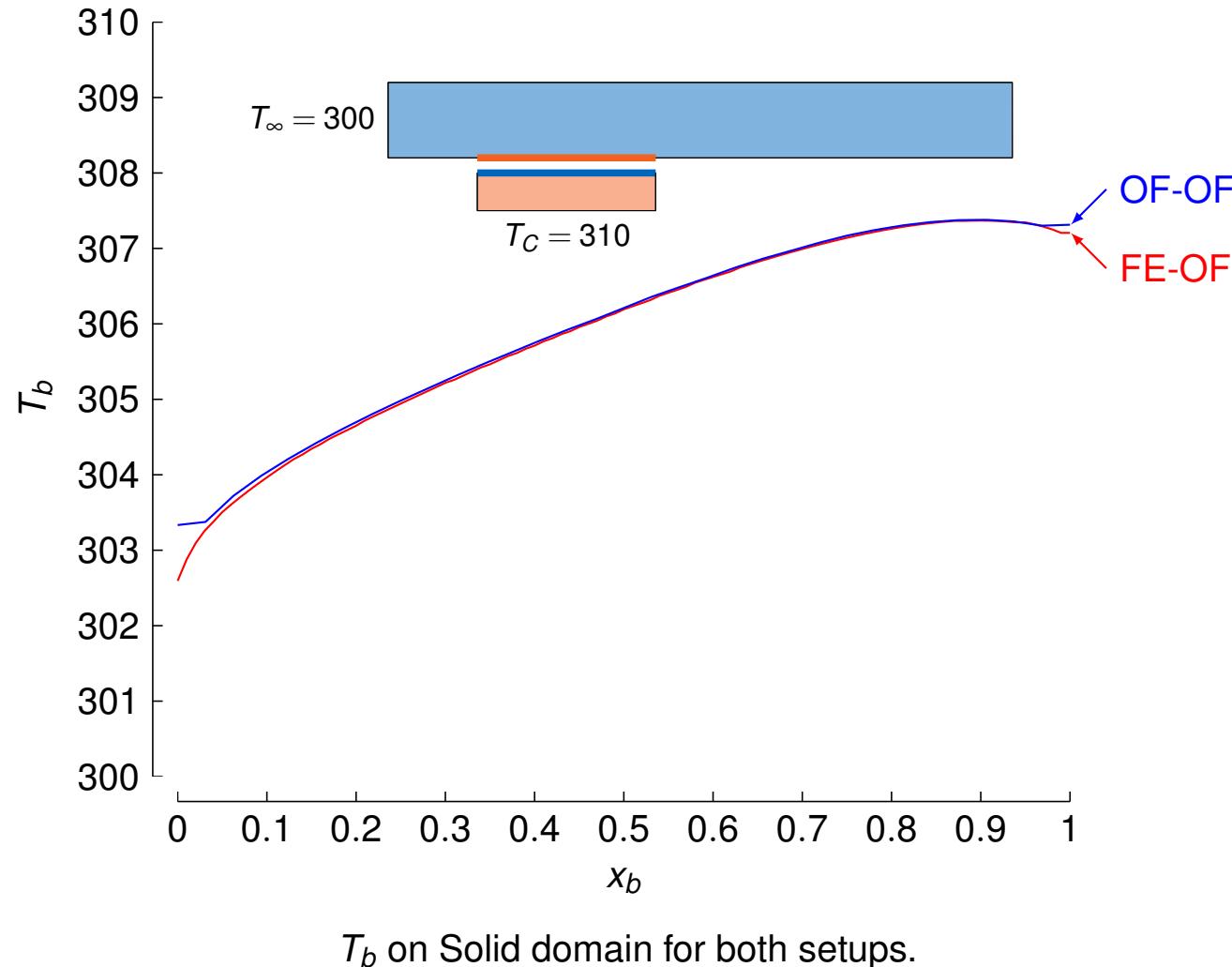
- Fluid from [openfoam-adapter/tutorials](#)
- Solid from [openfoam-adapter/tutorials](#)
- `precice-config.xml` from [openfoam-adapter/tutorials](#)

## OpenFOAM-FEniCS

- Fluid from [openfoam-adapter/tutorials](#)
- Solid/heat.py from [precice/tutorials](#)
- `precice-config.xml` from [openfoam-adapter/tutorials](#)

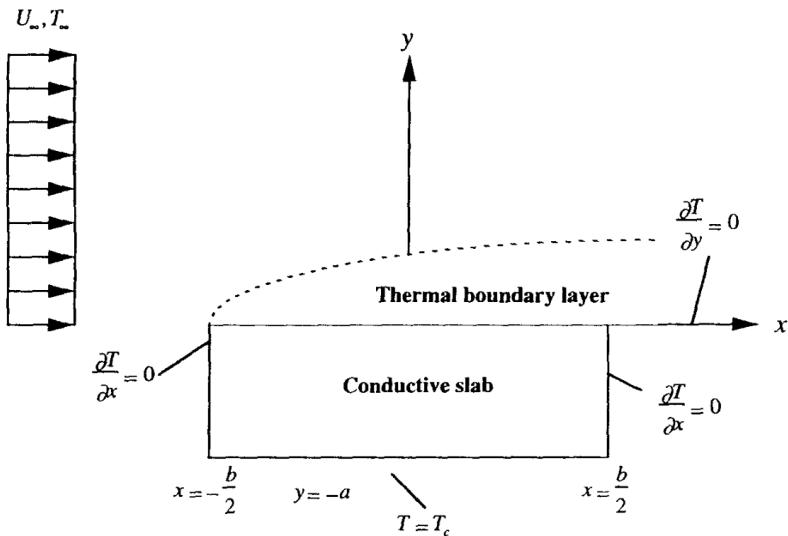
# Flow over plate

OpenFOAM-OpenFOAM vs. OpenFOAM-FEniCS

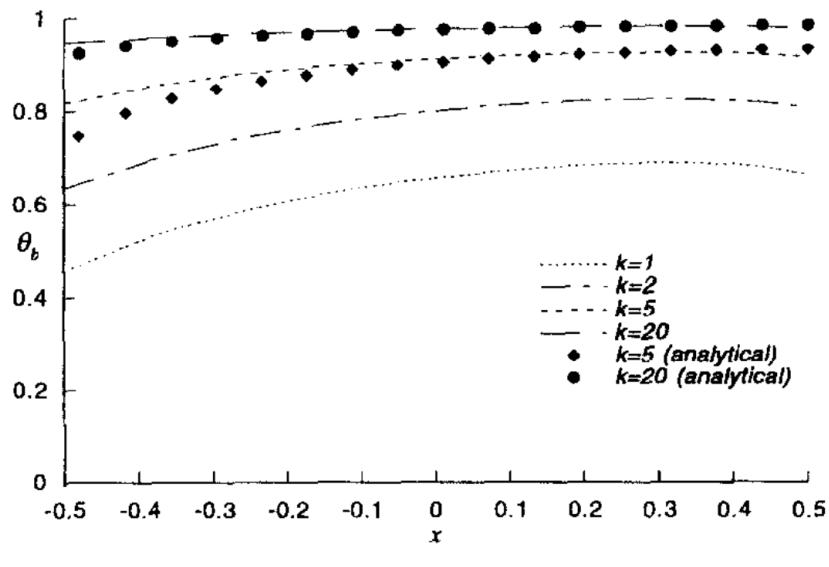


# Comparison to literature

Vynnycky<sup>1</sup>



Problem setup from <sup>1</sup>



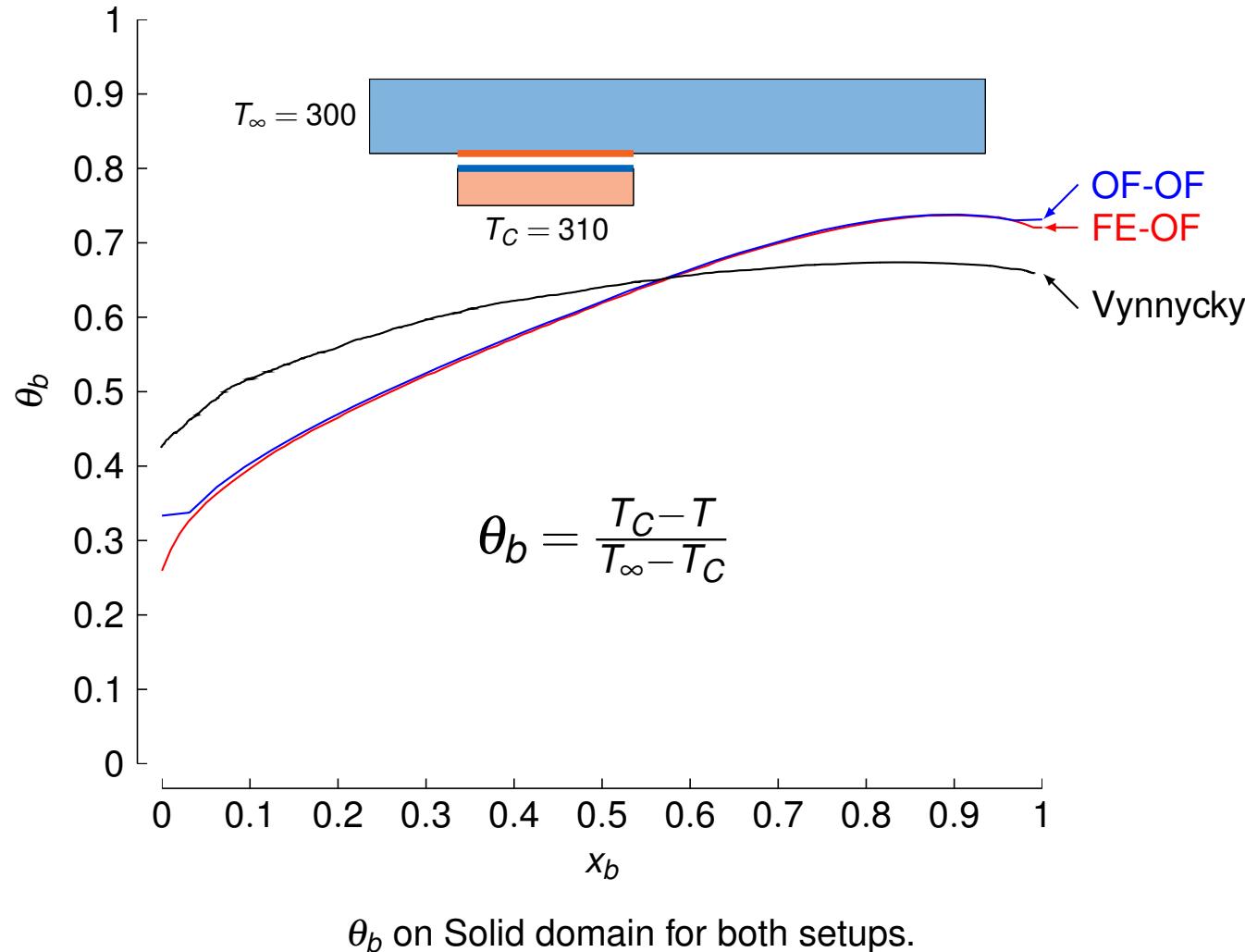
Results from <sup>1</sup>

$$Re = 500, Pr = 0.01, \lambda = 0.25$$

<sup>1</sup>Vynnycky, M., et al. (1998). Forced convection heat transfer from a flat plate: the conjugate problem.

# Comparison to literature

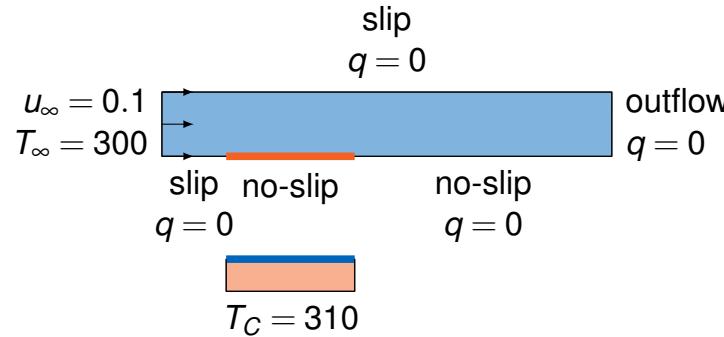
preCICE vs. Vynnycky



# Comparison to literature

Different Setups

Cheung<sup>1</sup> vs. Vynnycky<sup>2</sup>



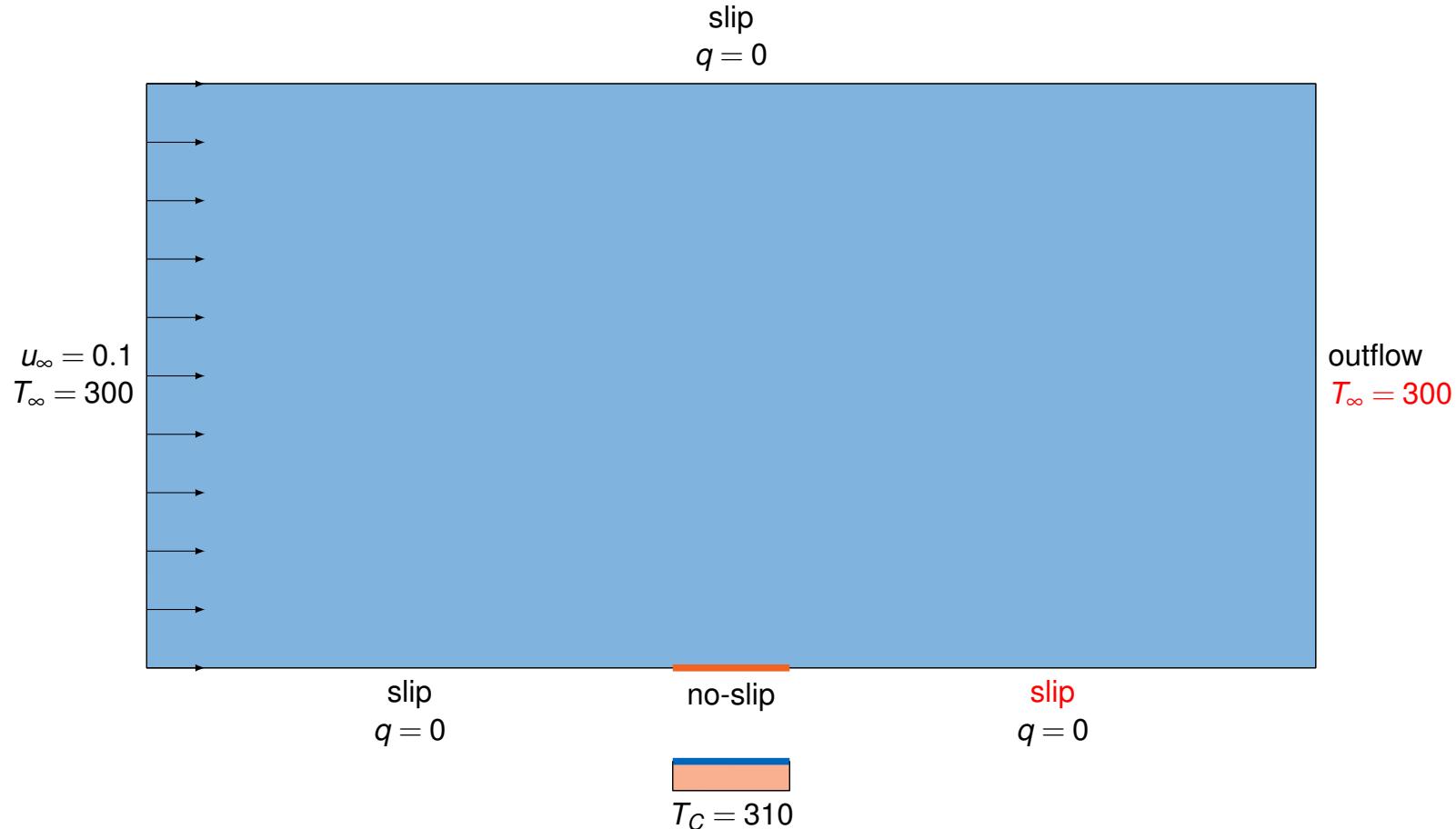
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# Summary & Outlook

## FEniCS + OpenFOAM

- FEniCS or OpenFOAM are used for heat equation in solid domain
  - `heat.py` is only a proof-of-concept
  - `laplacianFoam` more advanced
- OpenFOAM's `buoyantPimpleFoam` solves flow + energy transport in fluid domain.
- preCICE couples the solvers with identical `precice-config.xml`
- Tutorial can be found at  
[github.com/precice/tutorials/CHT/flow-over-plate/buoyantPimpleFoam-fenics](https://github.com/precice/tutorials/CHT/flow-over-plate/buoyantPimpleFoam-fenics)

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## Quantitative assessment

- good agreement of FEniCS + OpenFOAM with OpenFOAM + OpenFOAM
- analytic solution and simulation do not match

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<sup>1</sup>Logg, A., Mardal, K. A., & Wells, G. N. (2012). *Automated solution of differential equations by the finite element method. Lecture Notes in Computational Science and Engineering*.

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## Outlook

- more FEniCS tutorials (FEniCS + X)
- FEniCS-based solvers as CBC.Block, CBC.RANS and CBC.Solve<sup>1</sup>
- Reproducing Vynnycky's results ([github.com/precice/tutorials/issues/22](https://github.com/precice/tutorials/issues/22))

<sup>1</sup>Logg, A., Mardal, K. A., & Wells, G. N. (2012). *Automated solution of differential equations by the finite element method. Lecture Notes in Computational Science and Engineering*.

# Summary



**Flexible:** Couple your own solver with any other

**Easy:** Add a few lines to your code

**Ready:** Out-of-the box support for many solvers

**Fast:** Fully parallel, peer-to-peer, designed for HPC

**Stable:** Implicit coupling, accelerated with Quasi-Newton

**Multi-coupling:** Couple more than two solvers

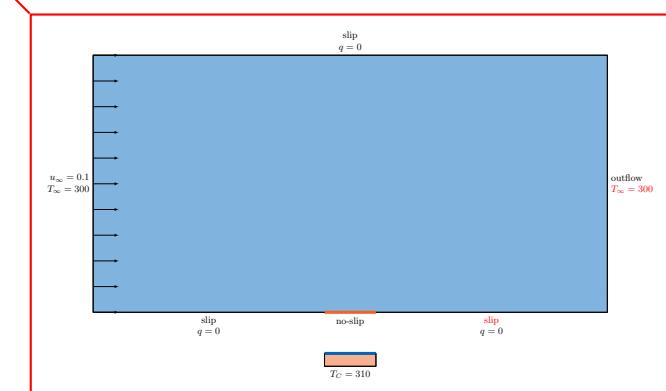
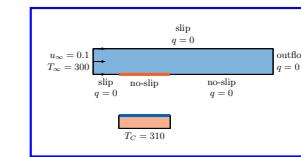
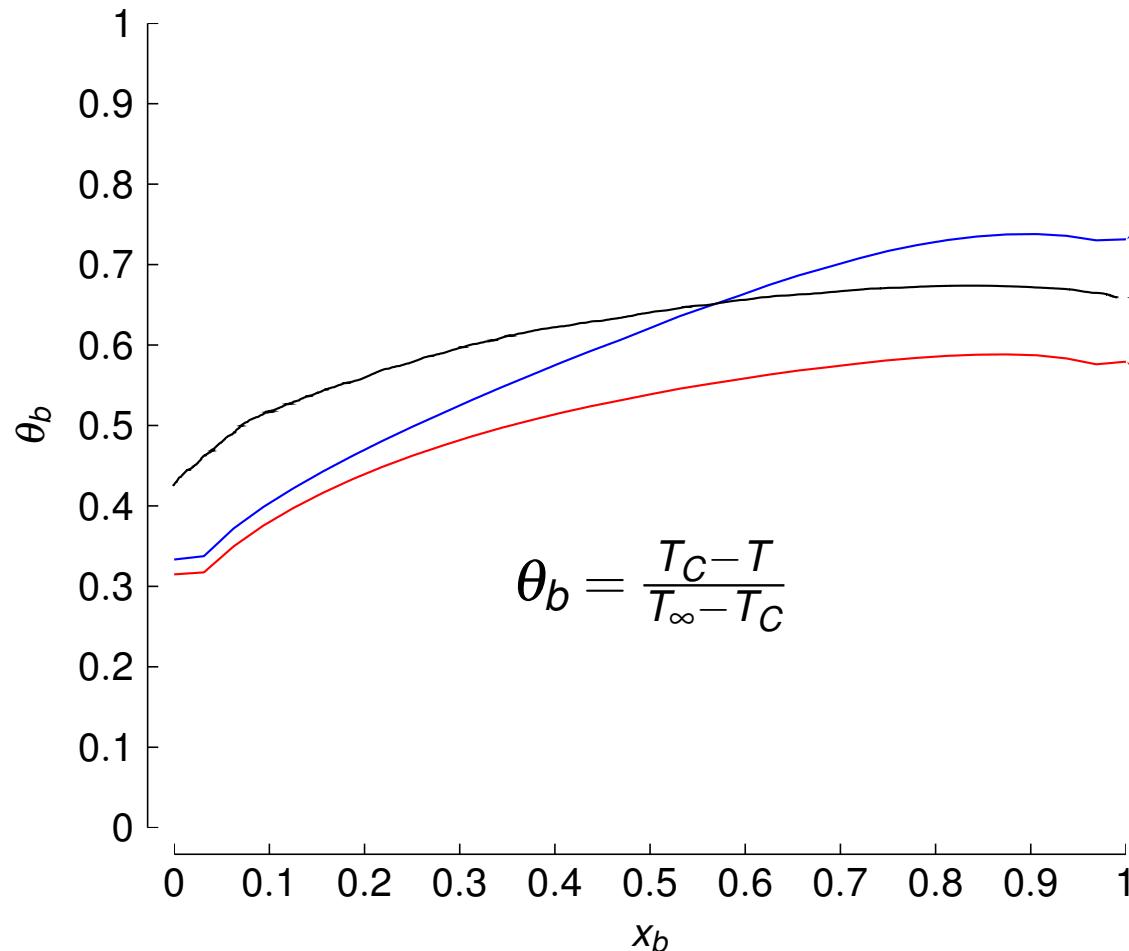
**Free:** LGPL3, source on GitHub

- [www.precice.org](http://www.precice.org)
- [github.com/precice](https://github.com/precice)
- [@precICE\\_org](https://twitter.com/precICE_org)
- Mailing-list, Gitter
- Literature Guide on wiki



# Study on Vynnycky setup

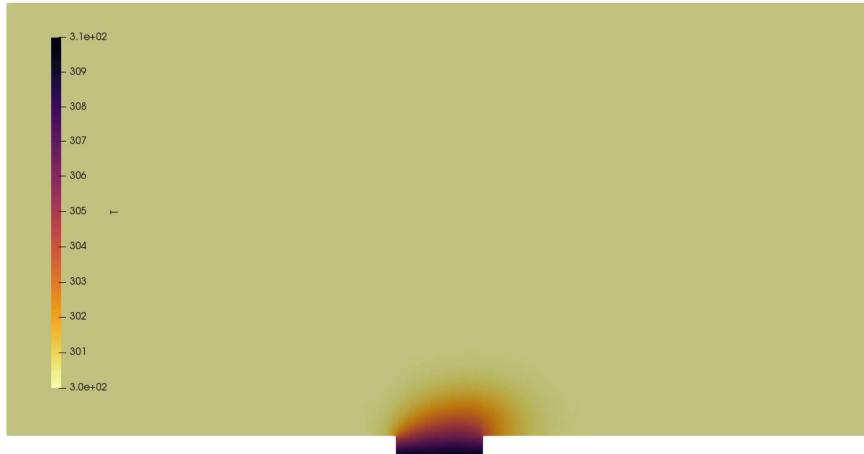
Different geometry & boundary conditions



Where does the shift come from?

# Study on Vynnycky setup

Different  $T_\infty$



$$T_C = 310, T_\infty = 300$$



$$T_C = 310, T_\infty = 25$$

How to set  $T_C$  and  $T_\infty$ ?

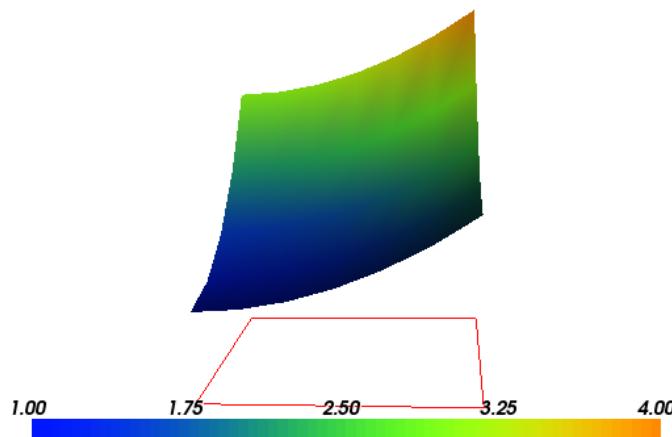
# Heat Equation in FEniCS

## Heat Equation

$$\frac{\partial u}{\partial t} = \Delta u + f \text{ in } \Omega$$
$$u = u_0(t) \text{ on } \partial\Omega$$

**Analytical Solution**, if  $f = \beta - 2 - 2\alpha$  we get

$$u = 1 + x^2 + \alpha y^2 + \beta t.$$



Solution of Poisson equation. Figure from <sup>1</sup>.

## Discretization

- **implicit Euler:**

$$\frac{u^k - u^{k-1}}{dt} = \Delta u^k + f^k$$

- **trial space:**

$$u \in V_h \subset V = \{v \in H^1(\Omega) : v = u_0 \text{ on } \partial\Omega\}$$

- **test space:**

$$v \in \hat{V}_h \subset V = \{v \in H^1(\Omega) : v = 0 \text{ on } \partial\Omega\}$$

- **weak form:**

$$\int_{\Omega} (u^k v + dt \nabla u^k \cdot \nabla v) dx = \int_{\Omega} (u^{k-1} + dt f^k) v dx$$

**Remark:** Tutorial from the FEniCS book<sup>1</sup>

<sup>1</sup> Langtangen, H. P., & Logg, A. (2016). *Solving PDEs in Python - The FEniCS Tutorial I* (1st ed.).

# Heat Equation in FEniCS

Geometry:  $\Omega, \partial\Omega, \Gamma_D, \Gamma_N$

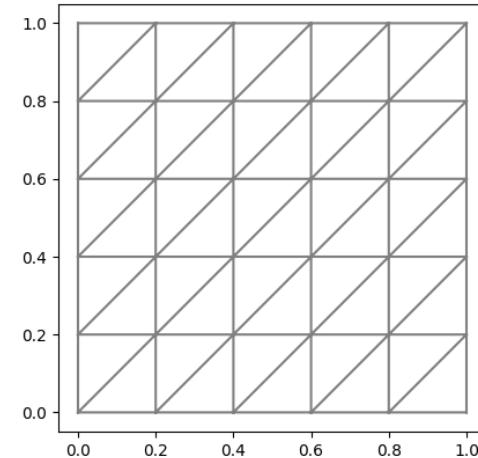
```
class RightBoundary(SubDomain):
    def inside(self, x, on_boundary):
        tol = 1E-14
        if on_boundary
            and near(x[0], x_r, tol):
                return True
        else:
            return False

class Boundary(SubDomain):
    def inside(self, x, on_boundary):
        if on_boundary:
            return True
        else:
            return False

p0 = Point(0, 0)
p1 = Point(1, 1)
```

Mesh:  $\Omega_h$

```
nx = 5
ny = 5
mesh = RectangleMesh(p0, p1,
                     nx, ny)
```



Mesh created with FEniCS

# Heat Equation in FEniCS

Function Space:  $V_h \subset V = \{v \in H^1(\Omega)\}$

```
V = FunctionSpace(mesh, 'P', 1)
```

Expressions:  $u = 1 + x^2 + \alpha y^2 + \beta t$  and  $f = \beta - 2 - 2\alpha$

```
u_D = Expression('1 + x[0]*x[0] + alpha*x[1]*x[1] + beta*t', ..., t=0)
f = Constant(beta - 2 - 2 * alpha)
```

Boundary Conditions:  $u \in V_h \subset V = \{v \in H^1(\Omega) : v = u_D \text{ on } \partial\Omega\}$  and  $v \in \hat{V}_h \subset V = \{v \in H^1(\Omega) : v = 0 \text{ on } \partial\Omega\}$

```
bc = DirichletBC(V, u_D, Boundary)
u = TrialFunction(V)
v = TestFunction(V)
```

Initial Condition:  $u^0 = u(t = 0)$

```
u_n = interpolate(u_D, V)
```

# Heat Equation in FEniCS

Variational Problem:  $\int_{\Omega} (u^k v + dt \nabla u^k \cdot \nabla v) dx = \int_{\Omega} (u^{k-1} + dt f^k) v dx$

```
F = u * v * dx + dt * dot(grad(u), grad(v)) * dx - (u_n + dt * f) * v * dx
a, L = lhs(F), rhs(F)
```

Time-stepping and simulation loop:  $\frac{u^k - u^{k-1}}{dt} = \Delta u^k + f^k$

```
u_np1 = Function(V)
t = 0
T = 1
dt = .1
u_D.t = t + dt

while t < T:
    solve(a == L, u_np1, bc)
    t += dt
    u_D.t = t + dt
    u_n.assign(u_np1)
```